Temporal Interpretation, Discourse Relations and Common Sense Entailment*

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Abstract

This paper presents a formal account of how to determine the discourse relations between propositions introduced in a text, and the relations between the events they describe. The distinct natural interpretations of texts with similar syntax are explained in terms of defeasible rules. These characterise the effects of causal knowledge and knowledge of language use on interpretation. Patterns of defeasible entailment that are supported by the logic in which the theory is expressed are shown to underly temporal interpretation.

1 The Problem of Temporal Relations

An essential part of text interpretation involves calculating the relations between the events described. But sentential syntax and compositional semantics alone don’t provide the basis for doing this. The sentences in (1) and (2) have the same syntax, and so using compositional semantics one would predict that the events stand in similar temporal relations.

(1) Max stood up. John greeted him.
(2) Max fell. John pushed him.

But in (1) the order in which the events are described matches their temporal order, whereas in (2) descriptive order mismatches temporal order. At least, these are the natural interpretations of (1) and (2) unless the reader has information to the contrary. Similarly, the syntax of the sentences in texts (3) and (4) are similar, but the natural interpretations are different.

(3) Max opened the door. The room was pitch dark.
(4) Max switched off the light. The room was pitch dark.

The event and state in (3) temporally overlap, whereas in (4) they do not. An adequate account of temporal interpretation must capture these distinctions.

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2 The Goals

Previous treatments of tense in Discourse Representation Theory (DRT) have investigated temporal relations in narrative texts like (1), (3) and (4) (Kamp and Rohrer 1983, Partee 1984, Hinrichs 1986). Dowty (1986) has explored the semantics of narrative text in an interval-based framework. These theories characterise tense as a tripartite relation between event time, reference time and speech time. The reference time is anaphoric (cf. Reichenbach 1947): the forward movement of time in (1) is encoded in the logical form of the clauses through the forward movement of their reference times. In the case of DRT, statives don’t invoke forward movement of reference times, and thus a distinction between (1) and (3) is achieved.

None of these theories attempt to account for the apparent backward movement of time in (2), and in texts like (5).

(5) The council built the bridge. The architect drew up the plans.

Moreover, they are unable to explain why the natural interpretations of (3) and (4) are different. We aim to extend these theories to solve the above problems. We will show that temporal relations must be calculated on the basis of semantic content, knowledge of causation and knowledge of language use, as well as sentential syntax and compositional semantics. Consequently, temporal interpretation will not be determined by relations between reference times, where those relations are encoded in a logical form built from syntax alone. This is in sharp contrast to the traditional DRT interpretation of tense.

We’ll argue that the basis for distinguishing (1) and (2) is a piece of defeasible causal knowledge relating falling and pushing, which is lacking for standing up and greeting: the knowledge is defeasible in the familiar sense that it is subject to exception. More generally, we’ll suggest that defeasible reasoning underlies the interpretation of text: A defeasible logic is one where, informally, $\Gamma$ defeasibly implies $\phi$ just in case from knowing only $\Gamma$ one would infer $\phi$. Thus conclusions following from a set of premises need not follow from a superset. We’ll show that this type of logic provides a suitable system of inference for modelling the interactions between the Gricean pragmatic maxims and the world knowledge used to calculate temporal structure during interpretation.

Fixing $NL$ interpretation in a defeasible reasoning system has been proposed before. In the realm of temporal interpretation, it has been defended by Hobbs (1979, 1985) and Dahlgren (1988). In certain respects, the approach developed in the current paper refines that outlined by Hobbs and Dahlgren. They encode world knowledge (WK) and linguistic knowledge (LK) in a declarative framework, and use this to determine the preferred interpretations of text. Our approach is similar in this respect. The main difference, in fact, lies in the utilization of a constrained representation of defeasible knowledge, in which the underlying relation of logical consequence yields the interactions required.

In Hobbs’ and Dahlgren’s theories as they stand, it is not clear that the requisite notion of logical consequence could be defined, since the laws that need to interact in certain specific ways are not related in any obvious way. In particular, conflict can arise among the knowledge sources that they recruit during interpretation, and on occasion this conflict must be resolved. But since the resolution of conflict lacks logical justification, the interaction among the various
knowledge sources appears arbitrary. We maintain that the only way of putting the reader’s knowledge to work is to place it in the context of a logical language, for which a notion of logical consequence can be defined. Unlike Hobbs and Dalgren, we will place the reader’s knowledge in a logic where its implications can be precisely calculated.

(Lascarides 1992) and (Lascarides and Oberlander 1993a) calculate temporal structure by using WK and LK represented in terms of defeasible laws. But they dealt only with the temporal structure derived from two consecutive sentences in a text. And (Lascarides and Oberlander 1993a) didn’t choose among the candidate logics which one should be used to calculate temporal structure. Here, we supply a logic that supports the inferences discussed in (Lascarides and Oberlander 1993a). Indeed, the theory presented here can be viewed as an extension of that in (Lascarides 1992) and (Lascarides and Oberlander 1993a) in several ways. First, we suggest an analysis of the pluperfect that explains why (1) and (6) are different.

(6) Max stood up. John had greeted him.

And secondly, we calculate the relation between sentences separated by intervening material, such as the relation between (7a) and (7e) in the text below:

(7) a. Guy experienced a lovely evening last night.
   b. He had a fantastic meal.
   c. He ate salmon.
   d. He devoured lots of cheese.
   e. He won a dancing competition.

In order to extend coverage to texts like (7) we assume, in line with (Hobbs 1985, Grosz and Sidner 1986, Thompson and Mann 1987, Scha and Polanyi 1988), that constraints must be imposed on which sentences in a text can be related to form text segments, and that these constraints are to be characterised in terms of hierarchical discourse structure. We therefore not only calculate the temporal structure of the events described in a text. We also investigate how WK and LK affect the interactions between discourse structure and temporal structure within very simple discourses. This is an important extension of the work in (Lascarides 1992), where only event relations were calculated, making it impossible to analyse extended texts like (7).

The basic model of discourse structure we explore is one where units of a discourse are linked by discourse or rhetorical relations modelled after those proposed by Hobbs (1985). These discourse relations determine the hierarchical structure of the discourse, and hence the structural constraints on which sentences can attach together to form text segments. Because we’re concerned only with temporal aspects of interpretation, we consider here only certain discourse relations that are central to temporal import. These are listed below, where the clause $\alpha$ appears in the text before $\beta$:

- $\textit{Explanation}(\alpha, \beta)$: the event described in $\beta$ explains why $\alpha$’s event happened (perhaps by causing it); e.g., text (2).
• *Elaboration*(α, β): β’s event is part of α’s (perhaps by being in the preparatory phase); e.g., text (5).\(^1\)

• *Narration*(α, β): The event described in β is a consequence of (but not strictly speaking caused by) the event described in α; e.g., text (1).

• *Background*(α, β): The state described in β is the ‘backdrop’ or circumstances under which the event in α occurred (no causal connections but the event and state temporally overlap); e.g., text (3).

• *Result*(α, β): The event described in α caused the event or state described in β; e.g., text (4).

*Explanation* is in a sense the dual to *Result*; they both invoke causation, but the latter matches the textual and temporal orders of the events whereas the former doesn’t. Both *Result* and *Narration* encode that textual order matches temporal order, but only the former relation induces a causal link between the events. We will provide an account of how these relations constrain the hierarchical structure of text, and we will supply logical mechanisms for inferring the relations from the reader’s knowledge resources. It should be emphasised that this is not an exhaustive list of discourse relations: extensive classifications of discourse relations are offered in (Hobbs 1985, Thompson and Mann 1987, Schä and Polanyi 1988, Asher 1993). Here, since we are concerned with the temporal aspects of NL interpretation, we restrict our attention to the above relations.

The theory presented here lies at the intersection between formal semantics and computational linguistics. The relevance to formal semantics lies in our extension of existing DRT treatments of tense to solve the problems described. The extension will involve augmenting the DRT framework with the rhetorical relations mentioned above. We use this DRT-based theory of discourse structure so that direct comparisons with theories of tense in formal semantics can be made. But our account will be simpler than previous DRT treatments, in that we will not consider the role of temporal connectives in structuring discourse (but see Lascarides and Oberlander (1993b) for a proposed treatment in our framework). With regard to computational linguistics, we refine the proposal that defeasible reasoning underlies NL interpretation. We do this by examining in detail how a well defined notion of nonmonotonic consequence can be used to calculate precisely the interactions between semantic content, causal knowledge and pragmatic maxims. However, we offer no implementation, and we largely ignore communicative goals and intentions (cf. Grøsz and Sidner 1986, Cohen, Morgan and Pollack 1991).

3 The Basic Story

A logic will be suitable for calculating temporal interpretation only if it supports all the patterns of inference we need to calculate temporal and rhetorical relations. These inferences are listed below; we motivate each one by a particular example. For simplicity, most of these

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\(^1\)We assume Moens and Steelman’s (1988) tripartite structure of events, where an event consists of a preparatory phase, a culmination and a consequent phase.
examples will involve inferring temporal relations rather than discourse ones; the latter will be dealt with upon full formalisation.

Some formal notation is useful in order to clarify the logical structure of the inferences. We assume \( A \models B \) represents “\( B \) nonmonotonically follows from \( A \)” and \( A \models B \) represents “\( B \) monotonically follows from \( A \)”\(^{3}\). \( \phi > \psi \) is a gloss for the default rule “if \( \phi \), then normally \( \psi \)” and \( \phi \rightarrow \psi \) is a gloss for “if \( \phi \), then (indefeasibly) \( \psi \)”\(\). We should stress that this formal notation is intended to be theory-neutral at this stage, for we simply wish to survey which patterns of inference we require from the logic. Thus for now, one can consider \( \phi > \psi \) to be syntactic sugar for the way defaults are represented in default logic (i.e. \( \phi, M / \psi \), where \( M \) is the consistency operator), in autoepistemic logic (i.e. \( L \phi \land \neg L \psi \rightarrow \psi \), where \( L \) is the modal autoepistemic operator), in circumscription (i.e. \( \phi \land \neg abnormal_n(\phi) \rightarrow \psi \), where \( abnormal_n \) is an abnormality predicate), or in conditional logic (i.e. \( \phi > \psi \), where \( > \) is a modal connective). The two notions of entailment, i.e. \( \models \) and \( \vdash \), can equally be regarded as syntactic sugar for the different notions of entailment supported in these various logics.

### 3.1 Defeasible Modus Ponens

Defeasible Modus Ponens is the following nonmonotonic inference:\(^{2}\)

- **Defeasible Modus Ponens**
  \[ \phi > \psi, \phi \models \psi \]
  
  E.g., Birds normally fly, Tweety is a bird \( \models \) Tweety flies

We will show how it underlies the interpretation of text (1).

Intuitively, it’s sometimes the case that the only information available to an interpreter regarding temporal structure is textual order. This is the case when no information about the temporal order of events is derivable from \( wk \) and \( lk \), linguistic context, or syntactic clues like a change in tense, words like because, or adverbials. In such cases we claim the descriptive order of events typically matches temporal order. As explained in (Lascarides 1992) and (Lascarides and O&berlander 1993a), this claim is in line with Grice’s (1975) Maxim of Manner, where it is suggested that text should be orderly. One way of interpreting this is that events should be described in the right order. Furthermore, Dowty (1986) claims that in some genres at least, the author typically describes events in the order of their discovery or perception, resulting in descriptive order matching temporal order. Our claim is that this \( lk \) plays a key role in interpreting (1). This is because in (1) it is indeed the case that the only information available for calculating temporal structure is textual order.

We represented this temporal information conveyed by textual order as a combination of two rules; one defeasible and one indefeasible.

- **Narration**
  If the clause \( \beta \) currently being processed is to be attached by a discourse relation to the clause \( \alpha \) that’s part of the text processed so far, then normally, \( Narration(\alpha, \beta) \) holds.

\(\)

\(^{2}\)We ignore quantification and variables here, because the logic we ultimately use will be propositional.
• **Axiom on Narration**
  
  If $Narration(\alpha, \beta)$ holds, and $\alpha$ and $\beta$ describe the eventualities $e_1$ and $e_2$ respectively, then $e_1$ occurs before $e_2$.

Narration exploits the dynamic processing of discourse familiar in DRT, where text structure is built by processing the successive sentences, and the information $\beta$ portrayed in the current sentence must be added to some part $\alpha$ of the previous discourse. We define the constraints on which parts of the previous discourse are available for attachment below. Suffice for now to say that in a two sentence text like (1), the only part of the previous discourse to which the second sentence can attach is the first sentence.

Since $\beta$ is to be attached to $\alpha$, $\alpha$ must have been in the text before $\beta$, and thus the textual order of $\alpha$ and $\beta$ is coded in Narration’s antecedent. Thus Narration and its Axiom together convey the information that textual order matches temporal order, unless there’s information to the contrary. The idea that Gricean-style pragmatic maxims should be represented as defeasible rules has already been suggested in (Joshi, Webber and Weischedel 1984). Here, we’ve argued that the defeasible law Narration is a manifestation of Grice’s Maxim of Manner. It is defeasible because there are exceptions, e.g., text (2).

Suppose that the logical forms of the sentences in (1) are respectively $\alpha$ and $\beta$; they describe the events $e_1$ of Max standing up and $e_2$ of John greeting him, but they do not impose any conditions on the relations between $e_1$ and $e_2$. Then Narration and its axiom can contribute to the interpretation of (1), providing the reader’s KB contains the following:

(a) $\alpha$ and $\beta$ (so the reader believes the author is sincere)
(b) $\beta$ is to be attached to $\alpha$ by a discourse relation (so the reader believes the text is coherent)
(c) The interpretation of the discourse so far (so interpretation is incremental, and the preceding discourse is taken as fixed).
(d) All defeasible WK, such as causal laws, and all defeasible LK, such as Narration.
(e) All indefinite knowledge, like the Axiom on Narration and that causes precede effects.
(f) The laws of logic.

Defeasible Modus Ponens captures the preferred reading of (1) with respect to this KB:

(i) The premises of Narration are verified by the KB (assumption (b)).
(ii) The consequent of Narration is consistent with the KB.
(iii) (i) and (ii) form the premises of Defeasible Modus Ponens; $Narration(\alpha, \beta)$ is inferred.
(iv) Therefore, by the Axiom on Narration, Max standing up precedes John greeting him.

It must be stressed that this line of reasoning doesn’t represent a psychologically plausible account of human text processing. Assumption (f) alone prevents us from making such claims. Nonetheless, the above reasoning predicts the correct analysis of (1) with respect to the reader’s knowledge about the context, language use and the world.
3.2 The Penguin Principle

The Penguin Principle is the following pattern of inference:

- **Penguin Principle**
  \[ \phi \rightarrow \psi, \phi \vdash \neg \chi, \psi \vdash \chi, \phi \not\vdash \neg \chi \]
  
  E.g., Penguins are birds, penguins normally don’t fly, birds normally fly, Tweety is a penguin \( \not\vdash \) Tweety doesn’t fly

The antecedent to two defeasible laws are verified, and the conclusions to both cannot hold in a consistent KB. In this sense, the rules conflict. The antecedent to one of the laws entails the antecedent to the other; in this sense, it is more specific. We want a defeasible logic to validate the inference in which the more specific rule is preferred. It will play a central role in resolving conflict among the reader’s knowledge resources.

We now show how the Penguin Principle contributes to the interpretation of (2). First, we describe the relevant defeasible rules. By assumption (b) on the KB, an interpreter will infer a discourse connection between the sentences in a two-sentence text like (2). From the way we understand the discourse relations to which we limit ourselves in this paper, a discourse relation between two clauses entails one of the following relations between the *eventualities* (i.e. events and states) described: either one is a consequence of the other, one is part of (i.e. in the preparatory phase of) the other, they stand in causal relations, or they temporally overlap. For brevity, we state that if one of the above relations holds between two eventualities \( e_1 \) and \( e_2 \), then \( e_1 \) and \( e_2 \) are *e-connected*. Since the reader infers that the sentences in (1) and (2) are discourse related, he infers that the events they describe are e-connected. In the case of (2), there is \( \text{wK} \) gained from perception and experience, that relates falling and pushing in a particular way:

- **Push Causal Law**
  
  If \( e_1 \) where \( x \) falls and \( e_2 \) where \( y \) pushes \( x \) are e-connected, then normally, \( e_2 \) causes \( e_1 \).

There is also indefeasible knowledge that causes precede effects:

- **Causes Precede Effects**
  
  If \( e_1 \) causes \( e_2 \), then (indefeasibly) \( e_2 \) does not precede \( e_1 \).

The Push Causal Law is a *defeasible* law. Unlike Dahlgren’s (1988) probabilistic laws, it should *not* be read as pushing usually cause fallings. Indeed, we would claim that such a law would be far-fetched. For there will be plenty of pushings that don’t cause fallings; and there may well be plenty of fallings that cause pushings. Rather, the Push Causal Law states that *if* a pushing and falling are e-connected, *then* although both causal directions may be permissible, one normally prefers one to the other.\(^3\)

\(^3\)We are not concerned here with the metaphysics or meaning of causality. Suffice to say for now that our representation of causal relations is compatible with many of the current theories on causality. We also leave open the question of how these causal laws are acquired; suffice to say that they do not represent implausible knowledge.
The Causal Law may seem very ‘specific’. It could potentially be generalised, perhaps by re-stating \( e_1 \) as \( x \) moving and \( e_2 \) as \( y \) applying a force to \( x \), and then having appropriate connections between pushings and applying force, and fallings and movement to interpret (2). A proposal for generalising causal knowledge in this way is discussed in Asher and Lascarides (1993). We’re concerned here, however, with making the case for exploiting \( w_k \) and \( t_k \) in a logical framework to drive temporal interpretation, and this case can be made while glossing over generalisations like these. So we do so here.

There is no similar law for standing up and greeting; if one knows that a standing up and a greeting are \( c \)-connected but one knows nothing more, then it’s not possible to conclude, even tentatively, exactly how the events are related. Our claim is that the Push Causal Law forms the basis for the distinction between (1) and (2).

In interpreting (2), there is conflict among the applicable knowledge resources, specifically between Narration and the Causal Law; given Narration’s Axiom and Causes Precede Effects, the consequents of both laws can’t hold in a consistent KB. Given that the natural interpretation of (2) in the ‘null’ context is one where the pushing caused the falling, this conflict must be resolved in that context in favour of the Causal Law.

In nonmonotonic logics, conflict between defeasible rules is resolvable if one is more specific than the other, cf. the Penguin Principle. We wish to provide a principled theory of how knowledge conflict is resolved during NLI interpretation, and so we should ensure a Penguin Principle is formed in these cases. It’s done like this: Given that constituents related by a discourse relation describe events that are \( c \)-connected, we can restate the Push Causal Law as follows, making its antecedent entail that of Narration:

- **Push Causal Law**

  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes an event \( e_1 \) of \( x \) falling and \( \beta \) describes an event \( e_2 \) of \( y \) pushing \( x \), then normally, \( e_2 \) causes \( e_1 \).

The new version of the Push Causal Law expresses a mixture of defeasible \( w_k \) and \( t_k \), for it asserts that given the sentences are discourse-related somehow there is a \( c \)-connection between the events, and given the kinds of events they are, the second event described caused the first, if things are normal.

This new statement of the Causal Law ensures that together with Narration and the above contents of the reader’s KB, the premises of a Penguin Principle are formed. \( \alpha \) and \( \beta \) are now respectively the logical forms of the sentences in (2) rather than (1); the antecedents to the Causal Law and Narration are verified; these rules conflict and the more specific rule—the Causal Law—wins, resulting in an inference that the pushing caused the falling. This deals with the temporal structure of (2). We’ll subsequently show that inferring the discourse structure of (2) also involves a Penguin Principle; in fact the inferences about temporal structure and discourse structure will be interleaved during interpretation.

To ensure that logic resolves the conflict in the right way when interpreting (2) with respect to the above context, we have essentially had to tailor the representation of causal knowledge to the particular task at hand, namely linguistic interpretation. For we have had to explicitly represent how the information is presented in the text in the ‘causal’ rule, in order to achieve the right logical interactions with other knowledge resources. Causal laws represented as “an
event $e_1$ of type $a$ normally causes an event $e_2$ of type $b$" would not bear the right logical relation to the available $\text{LK}$ concerning textual order.

The result is a representation scheme that is nonmodular: WK and $\text{LK}$ are mixed. Such a scheme has been viewed in computational linguistics to be undesirable. One reason for rejecting nonmodular approaches is that it makes it difficult to derive the laws from more fundamental knowledge resources in a systematic way. Asher and Lascarides (1993) address this problem, and show how lexical semantics can be used to generalise laws like the Push Causal Law, and suggest how they can be derived systematically. This is beyond the scope of this paper, however. We are not concerned with how the laws in the KB are acquired systematically. Rather, our purpose here is to investigate which logic provides the suitable inference regime for calculating temporal structure and discourse structure; and on this point we make the following claim. WK and $\text{LK}$ can give conflicting messages about how to interpret discourse. This has two consequences. First, the logical consequence relation must be able to resolve conflict, and it can do this only if the conflict laws are logically related. So second, this requires the causal knowledge to be represented in the nonmodular way we’ve suggested. Otherwise, conflicting defaults don’t stand in the required relation of logical specificity.

The version of the Penguin Principle we’ve assumed here is one where the antecedent of the default rules are related by an indefeasible conditional. Intuitively, the same conclusion should follow when the indefeasible conditional is replaced by a defeasible one (cf. Asher and Morreau 1991). We haven’t as yet found an example of discourse attachment that requires this version of the Penguin Principle however, and so we don’t use a logic that supports it.

3.3 The Nixon Diamond

Conflict among defeasible rules is not resolvable when the antecedents of the rules aren’t related. We refer to this (lack of) inference as the Nixon Diamond:

- **Nixon Diamond**
  
  \[ \phi > \chi, \psi > \neg \chi, \phi, \psi \models \chi \text{ (or } \neg \chi) \]

  Quakers are normally pacifists, Republicans normally are non-pacifists, Nixon is a Quaker and a republication \models \neg \text{Nixon is a pacifist}/Nixon is a non-pacifist.

We argue that the Nixon Diamond provides the key to textual incoherence, as in (8).

(8) ?Max won the race. He was home with the cup.

The appropriate KB when interpreting (8) verifies the antecedent of Narration. In addition, we claim that the following laws hold:

- **Win Law**
  
  If $e_1$ is Max winning, and $e_2$ is Max being at home, then normally, these eventualities don’t overlap.

- **States Overlap**
  
  If the clause $\beta$ is to be attached to the clause $\alpha$, and $\beta$ describes a state $s$, then normally $s$ overlaps the eventuality $e$ described by $\alpha$. 

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The Win Law captures the wk that if Max wins the race and if Max is at home, then these events don’t temporally overlap, if things are normal. In other words, it is unusual for the finish line of the race to be at the winner’s house. Note that the Win Law doesn’t require the antecedent to assert that the event and state are connected, nor in turn does it require the clauses that describe these eventualities to be discourse related. For the intuition this law captures is that the event and state don’t normally temporally overlap, regardless of whether they are connected or not.

States Overlap, on the other hand, is defeasible l.k. This law can be seen as a manifestation of Grice’s Maxim of Relevance, as suggested in Lascarides (1992). The argument goes as follows. An NIL text describes a portion of the time line, with events and states occurring on it. Let’s call this a situation. To construct a full picture of the situation, the interpreter must infer the relative occurrences of the states and the culminations of events, including where states start and stop. Since culminations are punctual (holding at points of time), their relative order is inferred from rules like Narration, which models describing things in the order of perception as explained earlier. But states are extended, and the order of perception of states does not fully determine where the states start relative to the other eventualities. So order of perception is insufficient for determining where a state starts.

There are several linguistic mechanisms which can be used to indicate where a state starts. The author could explicitly refer in the text to what caused the state, and so from the law that causes precede effects, the interpreter will know the relative place where the state starts, cf. text (4). Alternatively, the author can use temporal adverbials to say where a state starts. But (3) shows that these two mechanisms are not enough: how do we determine where states start in text that do not feature adverbials or causes? States Overlap is then a vital mechanism for determining where a state starts relative to other eventualities described in text. It basically says that if there is no “explicit” indication of where the state starts—via the mention of causes or the use of temporal adverbials—then the start of the state is assumed to be before the situation that the text is concerned with occurs, resulting in overlap given the relation between textual order and order of perception. States Overlap asserts that (unless there’s indication to the contrary) the point where a state starts is before the situation that the text describes, rather than part of it; and in that it’s not part of the situation, it is irrelevant. Thus States Overlap models the following in accordance with Grice’s Maxim of Relevance: the start of a state is relevant only if it is marked as such.

Assume that the reader’s KB is as usual, save that α and β are now respectively the logical forms of the sentences in (8). Then the antecedents to States Overlap, the Win Law and Narration are all verified. By the general principle that the more specific default law overrides the less specific one when they conflict, the rule of Narration is deemed irrelevant here; States Overlap is more specific. States Overlap and the Win Law also conflict, but their antecedents aren’t logically related. Hence as in the Nixon Diamond, we fail to infer any conclusion about the temporal relation between the eventualities described, leading to incoherence.

3.4 Closure on the Right

Closure on the Right is a monotonic inference of the following form:
• Closure on the Right
  \( \phi > \psi, \psi \rightarrow \chi \models \phi > \chi \)
  
  E.g., Lions normally walk, walkers (indefensibly) have legs \( \models \) lions normally have legs.

The theory of discourse attachment we propose requires this inference for several technical reasons, as will be clear in the appendix. It is also used, in conjunction with the Nixon Diamond, to account for discourse popping. Consider again text (7).

(7)   a. Guy experienced a lovely evening last night.
   b. He had a fantastic meal.
   c. He ate salmon.
   d. He devoured lots of cheese.
   e. He won a dancing competition.

Intuitively, (7c,d) elaborate (7b), but (7e) does not. Thus (7e) should not attach to (7d) to form a text segment. Rather, (7e) should be related by (7b) by \textit{Narration}. But (7d) and (7e) are consecutive sentences, and by our assumptions on the KB they will verify the antecedent to Narration. So something must block Narration’s consequent. This is achieved as follows: In line with Scha and Polanyi (1988), we assume that if a text segment is narrative, it cannot also be an elaboration. Thus Rule 1 is part of the reader’s KB:

• Rule 1
  If \textit{Narration}(\(\alpha, \beta\)) holds, then (indefensibly) \(\lnot \text{Elaboration}(\alpha, \beta)\) holds.

Rule 1 together with Narration and Closure on the Right produce Rule 2:

• Rule 2
  If \(\beta\) is to be attached to \(\alpha\) with a discourse relation, then normally, \(\lnot \text{Elaboration}(\alpha, \beta)\) holds.

The following defeasible law captures the intuition that if a clause \(\gamma\) is to attach with \textit{Narration} to a clause \(\beta\) that elaborates \(\alpha\), then \(\gamma\) must also elaborate \(\alpha\):

• Rule 3
  If \textit{Elaboration}(\(\alpha, \beta\)) and \(\lnot \text{Elaboration}(\alpha, \gamma)\) hold, then normally \(\lnot \text{Narration}(\beta, \gamma)\) holds.

Suppose that the logical forms of (7b), (7d) and (7e) are respectively \(\alpha, \beta\) and \(\gamma\). Suppose furthermore that in accordance with intuitions, the reader has inferred \textit{Elaboration}(\(\alpha, \beta\)). Then according to assumption (c) above, this is part of the contents of the KB. The task now is to attach \(\gamma\) to the preceding discourse. By Rule 2 with \(\alpha\) and \(\gamma\) substituted in the schema, we infer \(\lnot \text{Elaboration}(\alpha, \gamma)\). Thus from Rule 3 one would infer \(\lnot \text{Narration}(\beta, \gamma)\). But substituting \(\beta\) and \(\gamma\) in the schema Narration produces the conflicting conclusion \textit{Narration}(\(\beta, \gamma\)). The antecedents of rules 2 and 3 are not logically related to that of Narration, resulting in irresolvable conflict (cf. the Nixon Diamond). Thus no discourse relation between (7d) and
(7e) is inferred, indicating that (7d,e) forms an incoherent text segment. Therefore, (7e) must attach to one of the remaining clauses in the preceding text. A full analysis of this example will be given upon formalisation. For now, suffice to say that Closure on the Right was required to block the attachment of (7e) to (7d).

3.5 Dudley Doorite

Dudley Doorite is also a monotonic inference:

- **Dudley Doorite**
  \[ \phi > \chi, \psi > \chi \models (\phi \lor \psi) > \chi \]
  E.g., A Quaker is normally a pacifist, A Republican is normally a pacifist \models A Quaker or Republican is normally a pacifist

We use it to explain the ambiguity of text (9).

(9) The bimetallic strip changed shape. The temperature fell.

The appropriate KB contains the following laws:

- **Change=Bending or Straightening**
  A bimetallic strip changes shape if and only if it bends or straightens.

- **Bend Causal Law**
  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes the event \( e_1 \) of a bimetallic strip bending, and \( \beta \) describes an event \( e_2 \) of the temperature falling, then normally, \( e_1 \) causes \( e_2 \).

- **Straighten Causal Law**
  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes the event \( e_1 \) of a bimetallic strip straightening, and \( \beta \) describes an event \( e_2 \) of the temperature falling, then normally, \( e_2 \) causes \( e_1 \).

Neither the above causal laws’ antecedents are satisfied by the KB in the analysis of (9). However, Closure on the Right and Dudley Doorite can be used to infer the event structure for (9): Closure on the Right yields Law 1 and Law 2 respectively from the Bend Causal Law and the Straighten Causal Law:

- **Law 1**
  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes the event \( e_1 \) of a bimetallic strip bending, and \( \beta \) describes an event \( e_2 \) of the temperature falling, then normally, \( e_1 \) causes \( e_2 \) or \( e_2 \) causes \( e_1 \).

- **Law 2**
  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes the event \( e_1 \) of a bimetallic strip straightening, and \( \beta \) describes an event \( e_2 \) of the temperature falling, then normally, \( e_2 \) causes \( e_1 \) or \( e_1 \) causes \( e_2 \).
These then form the premises for Dudley Doorite which, together with Change=Bending or Straightening, produce the Change Causal Law:

- **Change Causal Law**
  If \( \beta \) is to be attached to \( \alpha \), and \( \alpha \) describes the event \( e_1 \) of a bimetallic strip changing shape, and \( \beta \) describes an event \( e_2 \) of the temperature falling, then normally, \( e_1 \) causes \( e_2 \) or \( e_2 \) causes \( e_1 \).

The reader's KB verifies the antecedent to Change Causal Law when interpreting text (9). By Defeasible Modus Ponens, the reader infers that the two events are causally connected, but he fails to infer the direction of the causal connection, resulting in temporal ambiguity.

## 4 Choosing a Nonmonotonic Logic

We will use all the above patterns of inference in text interpretation. So a logic is suitable for our purposes only if the logical consequence relation validates these inferences.

There are several different nonmonotonic logics which handle nonmonotonicity in various ways. For now, we simply survey which logics verify which of the above inferences. Reiter's (1980) default logic, autoepistemic logic (Moore 1984) and the logic of All I Know (Levesque 1991) verify Defeasible Modus Ponens and the Nixon Diamond, but none of the others. Konolige's (1988) Hierarchical Autoepistemic logic (HAEL) verifies Defeasible Modus Ponens and the Penguin Principle, but the premises of a Nixon Diamond yield a contradiction rather than no conclusion. Furthermore, it fails to verify the monotonic patterns of inference. Veltman's (1990) Update Semantics verify all the nonmonotonic patterns of inference, but none of the monotonic ones. It would be difficult to extend these logics to support Closure on the Right (cf. Morreau 1993). Since we require Closure on the Right, these logics are not suitable for our purposes here.

Pearl (1988) shows how conditional probability theory can be used to model nonmonotonic reasoning. However, the system cannot represent or reason with embedded defaults; that is, default rules where one default condition is embedded in another. In Lascarides, Asher and Oberlander (1992), we show that embedded defaults are needed to model how preceding discourse structure affects current discourse attachment. So Pearl's (1988) \( \epsilon \) semantics is not suitable for our purposes either.

Circumscription (McCarthy 1980) represents defaults using abnormality predicates. For example, \( birds \text{ fly} \) is represented as (10), which should be read as: for any \( x \) if \( x \) is a bird and is not abnormal in sense 1, then \( x \) flies.\(^4\)

\[
(\forall x)(bird(x) \land \neg ab_1(x) \rightarrow fly(x))
\]

The language includes many abnormality predicates, to capture the many senses in which individuals can be abnormal. The default \( Penguins \text{ don't fly} \), for example, is represented in

\(^4\)We consider here the first order language rather than the propositional version in order to clarify the discussion about abnormality predicates.
(11); it features a different abnormality predicate to (10) to reflect the intuition that being an abnormal penguin is different from being an abnormal bird.

\[(\forall x)(\text{penguin}(x) \land \neg ab_2(x) \rightarrow \neg fly(x))\]

Defeasible entailment in circumscription is defined in terms of those admissible models where the abnormality predicates have as small an extension as is consistent with the premises; the so-called minimal models. \(\psi\) defeasibly follows from \(\phi\) if for every minimal model in which \(\phi\) holds, \(\psi\) holds. This definition of validity captures Defeasible Modus Ponens and the Nixon Diamond.

Prioritised Circumscription (Lifschitz 1984) captures the Penguin Principle by fixing a particular order to the abnormality predicates, preferring models which minimise over \(ab_2\) to those that minimise over \(ab_1\). Although this captures the intuitively compelling pattern of inference, it only does so in virtue of machinery that’s extraneous to the semantics of defaults; namely the ordering of predicates in a hierarchy to guide inference. An alternative way of capturing the Penguin Principle, which does not require this extraneous machinery, is to assume the following law, which states that Penguins are abnormal birds (note we must use the abnormality predicate featured in (10) to express this).

\[(\forall x)(\text{penguin}(x) \rightarrow ab_1(x))\]

The definition of validity in circumscription then captures the intuition that more specific defaults override less specific ones. But this is done at the sacrifice of a uniform translation of NL statements about defaults; for sometimes laws like (12) will have to be encoded in the translation of defaults into the object language.

The fact that NL statement about defaults do not translate uniformly into the formal representation is a general problem with Circumscription; it also raises difficulties when attempting to capture Closure on the Right. Consider the premises of this inference: that is \((\forall x)(A(x) \land \neg ab_1(x) \rightarrow B(x))\) and \((\forall x)(B(x) \rightarrow C(x))\). From this it follows that \((\forall x)(A(x) \land \neg ab_1(x) \rightarrow C(x))\). But given the multitude of abnormality predicates in Circumscription, we have no way of knowing whether \(ab_1\) is the appropriate abnormality predicate for representing the default connection between \(A\) and \(C\). The customary translation of default statements into Circumscription is to introduce a new abnormality predicate for each default statement. So suppose the abnormality predicate to be used when expressing the default connection between \(A\) and \(C\) is \(ab_n\). Then we fail to support Closure on the Right: the above premises do not imply \((\forall x)(A(x) \land \neg ab_n(x) \rightarrow C(x))\). A similar tension arises between capturing Dudley Doorite and translations of NL default statements into Circumscription.

More recently, Delgrande (1988) has used conditional logic to model nonmonotonic reasoning. He defines a nonmonotonic consequence relation which is parasitic on his conditional connective \(>\). The idea is that \(can\text{-fly}(t)\) follows from \(\forall x(bird(x) > can\text{-fly}(x))\) and \(bird(t)\) just because \([\forall x(bird(x) > can\text{-fly}(x)) \land bird(t)] > can\text{-fly}(t)\) is a theorem.

Delgrande notices a problem with the conditional logic approach to nonmonotonic reasoning: the conditionals seem to be too nonmonotonic for defeasible reasoning. Intuitively, if one adds \(budgerigar(t)\) to the above premises, then \(can\text{-fly}(t)\) should still follow. To ensure that
the system supports this, Delgrande adds an external, syntactic mechanism for determining whether or not additional premises are irrelevant to the conclusions of arguments. Boutilier (1992) explains this problem, and our shared dissatisfaction with the solution: it invokes extra-logical machinery.

Commonsense Entailment (henceforward ce) (Asher and Morreau 1991, Morreau 1992) is a conditional logic for nonmonotonic reasoning that attempts to overcome the above problems in Circumscription and the above problems in Delgrande’s logic. It is a different application of conditional logic to defeasible reasoning than Delgrande and Boutilier, in that it doesn’t equate defeasible consequence with the conditional connective >. Morreau (1992) shows that consequently, one doesn’t need the extra-logical machinery set up by Delgrande to solve the Irrelevance Problem.

It solves the above problems with Circumscription by restricting all representation of normality to the metalanguage. NL defaults are translated into the formalism in a uniform way. All defaults are represented using a nonmonotonic conditional operator >. Intuitively, \( \phi > \psi \) is read as "If \( \phi \) then normally \( \psi \), and \( \text{birds fly} \) is represented as \((\forall x)(\text{bird}(x) > \text{fly}(x))\). All default statements are translated in this way, regardless of their specificity. The need for a uniform translation of default statements is paramount when dealing with the complex commonsense knowledge required to reason about discourse.

ce captures all the patterns of inference we have mentioned. Its approach to Closure on the Right is more satisfactory than Circumscription’s because multiple abnormality predicates are avoided. Furthermore, ce supports the Penguin Principle without resorting to machinery extraneous to the semantics of defaults, such as prioritising predicates as in Prioritised Circumscription, or forming hierarchies of defaults as in hael. We assume that whatever the semantics of default rules, that more specific defaults should override less specific ones when they conflict should be an inherent part of that semantics. We therefore favour the approach to the Penguin Principle taken in ce.

A further reason for using ce concerns the ability to carry out local inferences in a nonmonotonic framework. In general, it’s not possible to divide nonmonotonic inference into a chain of deductions based on parts of the context. This is because adding premises to nonmonotonic deductions doesn’t always preserve conclusions, making it necessary look at the premises as a whole. In ce, however, it is possible to divide inferences into a chain of subtheories under special circumstances, as shown in the appendix. We will exploit this property upon formalisation, in order to interleave reasoning about temporal structure and discourse structure. We leave open the question of whether chains of local inferences would be possible in Prioritised Circumscription.

We now examine in detail how the ideas presented here can be formally pinned down. To do this, we augment the drt framework with rhetorical relations, as proposed in Asher (1993); we show how to represent the appropriate \( \text{lik} \) and \( \text{wk} \) in ce; and we show how the appropriate temporal structures and discourse structures for NL texts are achieved.
5 Discourse Structure in DRT

The fragment of NL text considered here will be relatively simple, with no quantification, connectives, adverbials or future tense. We concentrate on characterising the pluperfect and simple past tenses alone. We employ an extension of DRT, so that we can compare directly our theory with previous, influential DRT theories of tense.

DRT represents discourse in terms of a discourse representation structure (DRS), which is a pair of sets identifying respectively the discourse entities and conditions on those entities. The individual sentences in this theory will be represented using DRS. But the representation of text as a whole extends the framework of DRT. Text is represented in terms of a discourse representation pair (DRP). This consists of a set of DRSs which define the semantic content of the sentences of the text, and a set of conditions on those DRSs, which characterise the discourse relations between them. So in essence, DRPs are the logical forms of the individual sentences plus discourse relations between them.

This kind of representation is a natural extension of the DRT framework: A DRP is a simpler version of an SDRS (or segmented discourse representation structure) as introduced in (Asher 1993). It is simpler in the sense that the discourse relations will relate only DRSs (corresponding to sentences) rather than SDRSs (corresponding to segments of text). Discourse relations between sentences rather than segments of text are adequate for the simple fragment considered here, but not adequate in general. For the sake of simplicity, we have chosen not to extend the DRT framework to SDRT here, although such an extension would be straightforward.

The formal definition of DRPs is as follows:

Definition of DRP and DRP Conditions

- If $\alpha_1, \ldots, \alpha_n$ are DRSs, $Con$ a set of DRP conditions on those DRSs, then $\{\alpha_1, \ldots, \alpha_n, Con\}$ is a DRP;
- If $\alpha_1$ and $\alpha_2$ are DRSs and $R$ is a discourse Relation, then $R(\alpha_1, \alpha_2)$ is a DRP condition on $\alpha_1$ and $\alpha_2$.
- If $\alpha$ is a DRS, then the DRP $\{\alpha, \emptyset\}$ is equivalent to $\alpha$ and shall be referred to as such.

For our purposes, discourse relations are two-place predicates whose semantics are defined by the interpretation function in the model. Thus the semantics of DRPs are obtained from the semantics of DRT given in the appendix simply by extending the interpretation function in the appropriate way.

5.1 The Logical Form of Sentences

We now turn to the question of representing sentences as DRSs. The logical form of sentences will introduce discourse entities denoting events and times to capture deictic reference (cf. Partee 1973). But since we are not concerned with NP reference, for simplicity we will assume NPs are represented by constants. We propose that the logical form of the sentences (13) is (13').
(13) Max stood up.

(13') \([e,t][t \prec \text{now}, \text{hold}(e,t), \text{standup}(\text{max},e)]\)

In words, (13') introduces discourse entities \(e\) and \(t\), and asserts that the event \(e\) is Max standing up and \(e\) holds at a point of time \(t\) earlier than now.

Contrary to traditional DRT, the semantics of (13') is given in a modal framework (as CE is modal), with truth defined relative to possible worlds. Moreover, the movement of time through discourse will be determined by defeasible rules for discourse attachment rather than by syntactic-based rules for constructing DRSS.

The logical form of (14) is (14'):

(14) Max had stood up.

(14') \([s,t][s : [e][\text{standup}(m,e), s = cs(e)], \text{hold}(s,t), t \prec \text{now}]\)

In (14'), \(s\) is the consequent state of the event of Max standing up, and it holds at the time \(t\) which precedes now. So our semantics of the perfect is like that in Moens and Steedman (1988): a perfect transforms an event into a consequent state, and asserts that the consequent state holds. The pluperfect of a state, such as (15), therefore, is assumed to first undergo a transformation into an event.

(15) John had loved Mary.

The event is usually the inceptive reading of the state—in this case, \textit{John started to love Mary}—although this can vary with the context. Then, the pluperfect asserts that the consequent state of this event holds—in this case, the consequent state is the state of John loving Mary itself.

We forego defining the function \(cs\) which takes events to consequent states here for reasons of space, but see Lascarides (1988) and Blackburn and Lascarides (1992) for a proposed semantics. We do, however, assume that the following relationship holds between an event and its consequent state:

- **Consequent States:**
  \[
  \Box(\forall t)(\text{hold}(cs(e), t) \rightarrow (\exists t')(\text{hold}(e, t') \land t' < t)) \\
  \Box(\forall t')(\text{hold}(e, t') \rightarrow (\exists t)(\text{hold}(cs(e), t) \land t \prec t'))
  \]

So a consequent state holds if and only if the event holds at an earlier time. This relationship means that simple past and pluperfect tensed sentences are truth conditionally equivalent, under the usual assumption that time is dense. They only differ in terms of which eventualities are available for future anaphoric reference.

This is unlike previous representations of the pluperfect, which invoke a tripartite relation between event time, reference time and speech time (Kamp and Rohrer (1983), Partee (1984), Hinrichs (1986), Dowty (1986)). In these theories, the simple past and pluperfect tenses differ
at the sentential level because the reference time is identified with the event time in the simple past and is after the event time in the pluperfect; thus the temporal structures are different.

But even though there is sentential equivalence, the pluperfect will play a distinct discourse role, as explained in section 8. Because discourse structure doesn’t arise solely from the logical form of sentences, the theory is rich enough to distinguish between the truth conditions of sentences and their discourse roles, thus allowing us to contrast the simple past and pluperfect in this way. Exploring this discourse level strategy for analysing the pluperfect is motivated by the fact that pluperfect sentences are understandable only in the context of preceding simple past tensed discourse.

This deals with sentences. Texts are represented as DRPs. The problem is to update the DRP: if $\tau$ is the DRP representing the first $n$ sentences of the text, and $\beta$ is the DRS representing the semantic content of the $n + 1$st sentence, then $\tau$ must be updated with $\beta$ by adding $\beta$ to $\tau$’s first set and adding discourse relations between $\beta$ and DRSs in $\tau$ to $\tau$’s second set. Updating will consist of:

1. Defining the constraints on the possible sites for attachment of the DRS $\beta$ (these will be some subset of DRSs in the DRP $\tau$); and
2. Defining rules for attachment of $\beta$ at an attachment site.

We now turn to the first task.

5.2 Constraints on Possible Sites for Attachment

We mentioned in section 2 the generally accepted view that only some components of a discourse structure are open in the sense that one may add new material to them as the discourse is processed. To update a DRP $\tau$ with the new information given by the sentence currently being processed, one has to relate the sentence’s DRS means of a discourse relation to an open DRS in $\tau$, where openness is as defined below. From an intuitive point of view, the definition of openness captures the following: an open clause is either the previous clause (i.e. the last one added to the DRP), or a clause that it elaborates or explains. This is in line with the openness constraints described in Scha and Polanyi (1988) and Asher (1993).

Definitions of Discourse Dominance

Suppose a DRP $\tau$ contains the DRSs $\alpha$ and $\beta$. Then:

- **Subordination**
  $\alpha$ is *subordinate* to $\beta$ if:
  
  (i) $Explanation(\beta, \alpha)$ or $Elaboration(\beta, \alpha)$ holds; or
  
  (ii) $\gamma$ is a DRS in $\tau$ such that $Explanation(\gamma, \alpha)$ or $Elaboration(\gamma, \alpha)$ holds, and
  $\gamma$ is subordinate to $\beta$.

- **Openness**
  A DRS $\alpha$ is *open* in the DRP $\tau$ if and only if $\alpha$ is the the DRS representing the previous clause in the text, or this DRS is subordinate to $\alpha$. 

18
One can represent DRPs as graphs, which are built in a depth-first left-to-right manner. The above definition of openness can then be represented pictorially as follows:

There are structural similarities between our notion of openness and Polanyi’s (1985) and Webber’s (1991); the open constituents are those on the right frontier of the discourse structure.

These constraints on the possible sites for attachment capture two intuitions noted in Scha and Polanyi (1988): first, the only clause to which the current clause can attach in narrative is the previous one; and second, an elaboration or explanation that occurs earlier than the previous clause cannot be resumed.\(^5\)

The awkwardness of text (16) illustrates the first intuition: (16c) should intuitively be related to (16a); but (16a) isn’t open since (16a,b) is narrative.

(16) a. Max stood up.
    b. John greeted him.
    c. Max got up slowly.

Text (17) illustrates the second intuition.

(17) a. John arrived late for work.
    b. He had taken the bus.
    c. He had totalled his car.
    d. His boss summoned him to his office.

Intuitively, (17b,c) explains (17a), but (17d) does not. Our definition of openness predicts that (17a-d,e) is awkward (because (17e) attempts to continue the ‘closed’ explanation (17b,c)), whereas (17a-d,f) is acceptable.

\(^5\)Definite noun phrases that refer to events previously described can occasionally allow one to refer back to segments of text which we claim are ‘closed off’. It is debatable, however, whether we re-open closed attachment sites or whether we start a new structure in the discourse. For the sake of simplicity, we ignore these sorts of discourses here, but see (Asher 1993).
(17) e. John had taken his car to the garage.
   f. John realised that his chances of promotion looked bleak.

The definition of openness permits several possible attachment sites for the incoming material. Our theory of discourse attachment doesn’t always choose which site among these possibilities is the preferred one. This is what one would want, because in some discourses there is no preference, leading to ambiguity (Asher 1993). However, our theory does predict that in some cases, the knowledge in the KB blocks attaching the incoming material to a particular open site. For example, we will formally pin down why even though (17c) is an open attachment site for (17d), (17d) doesn’t attach there.

Having chosen a particular attachment site according to the above constraints, we have yet to formally pin down the reasoning that underlies choosing which discourse relation to use. For example, we must specify why (17f) is related to (17d) by Narration, and not by any of the other discourse relations. We must define the rules for attaching new information to a particular attachment site. We have argued that these rules must be defeasible, characterising causal laws and pragmatic maxims. We now turn to the problem of representing these defeasible rules within CE.

6 A Brief Introduction to CE

CE supplies a modal semantics for defaults. On top of the truth conditional semantics there is a dynamic partial theory, which accounts for nonmonotonic inferences like those described above. Defeasible Modus Ponens intuitively goes as follows: first one assumes the premises birds fly and Tweety is a bird and no more than this. Second, one assumes that Tweety is as normal a bird as is consistent with these premises. Finally, from these two assumptions, one concludes that Tweety flies.

Let us first consider the semantics of defeasible statements. As already mentioned, “if φ then normally ψ” is represented as φ > ψ. We augment the language to include DRPs, and strict conditionals of the form □(A → B) in order to represent indefeasible laws like the Axiom on Narration. But we also simplify the language in that we use a propositional version.

The semantics of defeasible statements are defined in terms of a function * from worlds and propositions to propositions. Intuitively, *(w, p) is the set of worlds where the proposition p holds together with everything else which, in world w, is normally the case when p holds. So * encodes assumptions about normality. The truth conditions of defeasible statements are defined as follows:

- \( M, w \models \phi > \psi \) if and only if \( *(w, [\phi]) \subseteq [\psi] \)

In words, the above says that If \( \phi \) then normally \( \psi \) is true with respect to the model \( M \) at the possible world \( w \) if the set of worlds that defines what is normally the case when \( \phi \) is true in \( w \) all contain the information that \( \psi \) is also true. Thus CE is a conditional logic in the Acquisti (1972) tradition; it differs from previous conditional logics in the constraints it imposes on the function *.

Three constraints are particularly relevant here: Facticity,
Specificity and Dudley Doorite, as defined in the appendix. Facticity captures the intuition that however few properties a normal bird has, one of them is that he is a bird. Specificity encodes the constraint that normal birds aren’t penguins (because penguins don’t have the flying property associated with normal birds). Dudley Doorite encodes the constraint that if Quakers are pacifists and Republicans are pacifists, then Quakers and Republicans are pacifists.

The truth definitions for the full language are given in the appendix, together with the monotonic axioms which make the monotonic part of CE sound and complete. We use a modified version of the logic of CE given in (Asher and Morreau 1991): our axioms reflect ‘modal closure’ instead of just logical closure, where the background modal theory is S5. We show in the appendix that modal closure is necessary in order to build discourse structures.

Besides the monotonic axioms, CE develops a dynamic semantics of information states, which are sets of possible worlds, that verify defeasible inferences. This makes precise the notion of assuming no more than the premises of an argument (defined in terms of an update function + on information states), and assuming everything is as normal as is consistent with those premises (defined in terms of a normalisation function N). The functions *, + and N, which are defined in the appendix, characterise a further notion of (common sense) validity, written \( \models \) (also described in the appendix). This supports (at least) Defeasible Modus Ponens, the Nixon Diamond and the Penguin Principle. The monotonic validity \( \models \) supports Closure on the Right, and Dudley Doorite (and since \( \models \) is supra-classical, these are also valid under \( \models \)). Contrary to HAEI and Prioritised Circumscription, the Penguin Principle is verified without forming hierarchies of defaults. CE therefore captures in a satisfactory way all the patterns of inference we need. It may not do so in a minimal fashion, but it is the only candidate logic among those that we’ve discussed which does so at all. On the question of minimality, it should be noted that CE doesn’t support case-based reasoning, which is what default logic and circumscription are designed to do. So CE is not a strictly more powerful logic than these ones. One of our claims here is that case-based reasoning isn’t required to do discourse attachment, and so one doesn’t need the full power of default logic.

7 The Dynamic Construction of Discourse Structure

7.1 Narration and Defeasible Modus Ponens

The logical forms of the sentences in (1) are respectively \( \alpha \) and \( \beta \).

(1) Max stood up. John greeted him.

(\( \alpha \)) \[ [e_1, t_1][t_1 \prec \text{now, hold}(e_1, t_1), \text{standup}(\text{max}, e_1)] \]

(\( \beta \)) \[ [e_2, t_2][t_2 \prec \text{now, hold}(e_2, t_2), \text{greet}(\text{max}, \text{john}, e_2)] \]

The DRP representing (1) is constructed by updating the DRP \( \{\{\alpha\}, \emptyset\} \) with \( \beta \). We now formalise this. Let \( \langle \tau, \alpha, \beta \rangle \) be a function that updates the DRP \( \tau \) with the DRS \( \beta \) via a discourse relation with \( \alpha \), where \( \alpha \) is an open constituent of \( \tau \). Thus the output of this function is a new DRP \( \tau' \), which is just like \( \tau \) save that \( \beta \) is added to the first set and a
discourse relation between $\alpha$ and $\beta$ added to the second set. Let $me(a')$ stand for the main eventuality described in $a'$. The formal definition of $me$ is given in the appendix in a way that agrees with intuitions: For example, $me(a)$ is the event $e_1$ of Max standing up. Then Narration and its Axiom, which were introduced in section 3.1, are represented in \( CE \) as schemas:

- **Narration**
  \[
  \langle \tau, \alpha, \beta \rangle > \text{Narration}(\alpha, \beta)
  \]

- **Axiom for Narration**
  \[
  \Box(\text{Narration}(\alpha, \beta) \rightarrow me(\alpha) < me(\beta))
  \]

By the above assumptions (a) to (f) on the reader’s KB, \( \text{Narration}(\alpha, \beta) \) follows in \( CE \) from the KB by Defeasible Modus Ponens; and by modal closure in \( CE \), the standing up precededings the greeting. So the DRP representing (1) is (1′).

(1) Max stood up. John greeted him.

(1′) \{\{\alpha, \beta\}, \{\text{Narration}(\alpha, \beta)\}\}

Discourse structure is related to topic structure, as defined in Asher (1993). Intuitively, the topic of a segment is the overarching description of what the segment is about. For example, the topic of (1) could be John’s introduction to Max. In the case of \( \text{Narration} \), the law below states that \( \text{Narration}(\alpha, \beta) \) holds only if $\alpha$ and $\beta$ have a distinct, common (and perhaps implicit) topic $\gamma$:

- **Topic of Narration**
  \[
  \Box(\text{Narration}(\alpha, \beta) \rightarrow (\exists \gamma)(\text{topic}(\alpha) = \gamma \land \text{topic}(\beta) = \gamma \land \gamma \neq \alpha \land \gamma \neq \beta))
  \]

This rule is used to explain the incoherence of (18): as long as \( WK \) about cars breaking down and the sun setting is represented as intuitions would dictate, one cannot find a common distinct topic, and so \( \text{Narration} \) between the clauses can’t be inferred.

(18) ?My car broke down. The sun set.

But no other relation can be inferred given the defeasible \( \text{LK} \) and \( \text{WK} \) available. And hence no discourse structure for (18) is constructed. Note that we can improve the coherence of (18) by supplying a topic in a third clause, e.g. (19):

(19) Then I knew I was in trouble.

### 7.2 Knowledge Conflict and The Penguin Principle

The logical forms of the sentences in (2) are respectively $\alpha$ and $\beta$; they are constructed in the same way as those for the sentences in (1) because of the similar syntax:
(2) Max fell. John pushed him.

(α) \([e_1, t_1] [t_1 < \text{now}, \text{hold}(e_1, t_1), \text{fall}(\text{max}, e_1)]\)

(β) \([e_2, t_2] [t_2 < \text{now}, \text{hold}(e_2, t_2), \text{push}(\text{john, max}, e_2)]\)

We represent the Push Causal Law and the law that Causes Precede Effects in CE as:

- **Push Causal Law**
  \(\langle \tau, \alpha, \beta \rangle \land \text{fall}(\text{max}, \text{me}(\alpha)) \land \text{push}(\text{john, max}, \text{me}(\beta)) > \text{cause}(\text{me}(\beta), \text{me}(\alpha))\)

- **Causes Precede Effects**
  \(\square(\text{cause}(e_1, e_2) \rightarrow \neg e_2 < e_1)\)

We also capture the i.k that if \(\beta\) is to be attached to \(\alpha\), and moreover \(\beta\)’s event caused \(\alpha\)’s then normally, \(\beta\) explains \(\alpha\):

- **Explanation**
  \(\langle \tau, \alpha, \beta \rangle \land \text{cause}(\text{me}(\beta), \text{me}(\alpha)) > \text{Explanation}(\alpha, \beta)\)

And finally, in accordance with Scha and Polanyi (1988), we assume that the same two clauses cannot be related by both Explanation and Narration:

- **Axiom on Explanation**
  \(\square(\text{Explanation}(\alpha, \beta) \rightarrow \neg \text{Narration}(\alpha, \beta))\)

The KB contains \(\alpha, \beta\) and \(\langle \alpha, \alpha, \beta \rangle\). So Narration and the Push Causal Law apply. This forms a complex Penguin Principle; it is complex because the consequent of the two defeasible laws are not \(\chi\) and \(\neg \chi\), but instead the laws conflict in virtue of the Axiom on Narration and Causes Precede Effects. CE supports the more complex Penguin Principle:

- **The Complex Penguin Principle**
  \(\square(\phi \rightarrow \psi), \psi > \chi, \phi > \zeta, \square(\chi \rightarrow \theta), \square(\zeta \rightarrow \neg \theta), \phi \models \zeta\)

Therefore, there is a defeasible inference that the pushing caused the falling, as required.

Given the results of the Complex Penguin Principle, the antecedent of Explanation is verified. Moreover, the antecedent to Explanation entails that of the conflicting law Narration. So there is another Complex Penguin Principle, from which Explanation(\(\alpha, \beta\)) is inferred. So (2’) is the representation of (2).

(2’) \(\{\{\alpha, \beta\}, \{\text{Explanation}(\alpha, \beta)\}\}\)

The second application of the Penguin Principle in the above used the results of the first, but in nonmonotonic reasoning one must be wary of dividing theories into ‘subtheories’ in this way. We show in the appendix that the predicates involved in the above deduction are sufficiently independent that in CE one can indeed divide the above into two applications of
the Penguin Principle to yield inferences from the theory as a whole. We call this double application of the Penguin Principle where the second application uses the results of the first the *Cascaded Penguin Principle*.

By the openness constraints on DRPs defined earlier, the only available sentence for attachment if one were to add a sentence to (1) is *John greeted him*, whereas in (2), both sentences are available. So although the sentences in (1) and (2) have similar syntax and logical forms, the texts have very different discourse structures. The events they describe also have different causal structures. The difference in the natural interpretations of (1) and (2) arose essentially from causal knowledge. But the difference is not that (1) is always a narrative and (2) is always an explanation. Rather, *in the absence of information to the contrary*, (1) is a narrative and (2) is an explanation. In (Lascarides, Asher and Oberlander 1992), we demonstrate that this framework is sufficiently powerful to explain why the natural interpretation of (2) *in vacuo* is different from the interpretation of the same sentence pair in (20).

(20) **John and Max were at the edge of a cliff. Max felt a sharp blow to the back of his neck. He fell. John pushed him. Max rolled over the edge of the cliff.**

In (20), the falling and pushing are related by *Narration* rather than *Explanation*.

The discourse structure for (5) is built in an exactly analogous way to (2), using the rules Elaboration and Axiom on Elaboration below, where \( \text{prep}(me(\alpha), me(\beta)) \) means \( \beta \)'s eventualty is in the preparatory phase of \( \alpha \)'s.

(5) **The council built the bridge. The architect drew up the plans.**

- **Elaboration**
  \[ \langle \tau, \alpha, \beta \rangle \land \text{prep}(me(\beta), me(\alpha)) > \text{Elaboration}(\alpha, \beta) \]

- **Axiom on Elaboration**
  \[ \Box (\text{Elaboration}(\alpha, \beta) \rightarrow \neg \text{Narration}(\alpha, \beta)) \]

Now we fold states into the picture. States Overlap, which was introduced earlier, is formally represented as follows:

- **States Overlap**
  \[ \langle \tau, \alpha, \beta \rangle \land \text{state}(me(\beta)) > \text{overlap}(me(\alpha), me(\beta)) \]

There is also a version of States Overlap where \( \text{state}(me(\beta)) \) is replaced with \( \text{state}(me(\alpha)) \): this handles the cases where \( \alpha \) is stative rather than an event sentence.

Background captures the intuition that if \( \beta \) is to be attached to \( \alpha \) and the eventualities they describe overlap, then the discourse relation is *Background*, if things are normal, and the Axiom on Background prevents the text segment from being iconic:

- **Background**
  \[ \langle \tau, \alpha, \beta \rangle \land \text{overlap}(me(\alpha), me(\beta)) > \text{Background}(\alpha, \beta) \]
• Axiom on Background
\[ (\text{Background}(\alpha, \beta) \rightarrow \neg \text{me}(\alpha) < \text{me}(\beta)) \]

The appropriate \( \text{KB} \) when interpreting (3) forms the premises of a Cascaded Penguin Principle: the pairs of conflicting laws are States Overlap and Narration and Background and Narration

(3) Max opened the door. The room was pitch dark.

Thus the event and state overlap and the clauses are related by \( \text{Background} \). Now we turn to text (4).

(4) Max switched off the light. The room was pitch dark.

We have the following causal law, which reflects the knowledge that the room being dark and switching off the light, if connected, are normally such that the event causes the state.\(^6\)

• Dark Causal Law
\[ \langle \tau, \alpha, \beta \rangle \land \text{switchoff}(\max, \text{light}, \text{me}(\alpha)) \land \text{dark}(\text{room}, \text{me}(\beta)) > \text{cause}(\text{me}(\alpha), \text{me}(\beta)) \]

Suppose the reader’s \( \text{KB} \) is as usual. Then this \( \text{KB} \) verifies the antecedents of Narration, Dark Causal Law and States Overlap. Narration conflicts with States Overlap, which in turn conflicts with the causal law. Moreover, the causal law is more specific than States Overlap (for we assume \( \text{dark}(\text{room}, s_2) \) entails \( \text{state}(s_2) \) by the stative classification of the predicate \( \text{dark} \), and States Overlap is more specific than Narration. In CE the most specific rule wins, and so a causal relation between the event and state is inferred. Full details of the proof are given in the appendix.

A constraint on the use of the discourse relation \( \text{Result} \) is defined as follows:

• Result
\[ \langle \tau, \alpha, \beta \rangle \land \text{cause}(\text{me}(\alpha), \text{me}(\beta)) > \text{Result}(\alpha, \beta) \]

Given the above inference, the antecedents to \( \text{Result} \) and Narration are verified. \( \text{Result} \) and Narration don’t conflict, so the consequents of both Narration and \( \text{Result} \) are inferred from the \( \text{KB} \). Thus text (4) is a narrative, and moreover, the darkness is the \( \text{result} \) of switching off the light.

The Penguin Principle captures the following intuition concerning text processing: the reader never ignores information that is derivable from the text and relevant to calculating temporal structure and discourse structure. For example, in the case of (3) the Penguin Principle ensures the following information is not ignored: a stative expression was used instead of an event one.

There is an air of artificiality about the examples we’ve discussed in relation to the Penguin Principle, and there may be worries about the soundness of proceeding from our decontextualised cases to more realistic data. Texts containing more linguistic structure and information

\(^6\)For the sake of simplicity we ignore the problem of inferring that the light is in the room.
will in general mean that more information should be taken into account when attempting discourse attachment. Will this change the underlying inference patterns, and deem CE inappropriate? Any theory that makes precise the inferences that underly language interpretation suffers from this problem of complexity, and our theory is no exception. Our conjecture, however, is that however complex the rules for discourse attachment, specificity will always govern the way in which knowledge conflict is resolved. Since CE supports resolution of conflict by specificity, it is hoped that it will be a suitable logic for handling more complex data. Some research on this is currently underway. In Asher and Lascarides (1993), we show how, through spreading the semantic processing load between the lexicon and rules for discourse attachment, generalisations on the rules for discourse attachment can be achieved, which enable a much wider coverage of data. But exploring the role of specificity when analysing real data from a corpus is an area of future research.

7.3 Discourse Popping and The Nixon Diamond

Consider text (7).

(7) 
   a. Guy experienced a lovely evening last night.
   b. He had a fantastic meal.
   c. He ate salmon.
   d. He devoured lots of cheese.
   e. He won a dancing competition.

Let the logical forms of the respective clauses (7a-e) be $\alpha$, $\beta$, $\gamma$, $\delta$ and $\epsilon$. The discourse structure for (7a-d) involves Cascaded Penguin Principles and Defeasible Modus Ponens as before. Use is made of the defeasible knowledge connecting eating cheese and salmon with having a meal and experiencing a lovely evening.

Guy experienced a lovely evening last night

```
<table>
<thead>
<tr>
<th>Elaboration</th>
</tr>
</thead>
<tbody>
<tr>
<td>He had a fantastic meal</td>
</tr>
</tbody>
</table>
```

```
<table>
<thead>
<tr>
<th>Elaboration</th>
</tr>
</thead>
<tbody>
<tr>
<td>He ate salmon</td>
</tr>
</tbody>
</table>
```

```
<table>
<thead>
<tr>
<th>Elaboration</th>
</tr>
</thead>
<tbody>
<tr>
<td>He devoured lots of cheese</td>
</tr>
</tbody>
</table>
```

Narration

We study the attachment of $\epsilon$ to the preceding text in detail. The open clauses are $\delta$, $\beta$ and $\alpha$. But intuitively $\epsilon$ is not related to $\delta$ at all, and so we must block the inference to Narration’s
consequent. $\text{Elaboration}(\beta, \delta)$ is in the KB because the interpretation of the text so far is taken to be fixed; $\langle \tau, \alpha, \epsilon \rangle$, $\langle \tau, \beta, \epsilon \rangle$ and $\langle \tau, \delta, \epsilon \rangle$ are also in the KB. Rules 2 and 3 below are specifications of the rules introduced in section 3.4; Rule 2 being obtained from Narration via Closure on the Right:

- **Rule 2**
  \[
  \langle \tau, \beta, \epsilon \rangle > \neg \text{Elaboration}(\beta, \epsilon)
  \]

- **Rule 3**
  \[
  \text{Elaboration}(\beta, \delta) \land \neg \text{Elaboration}(\beta, \epsilon) > \neg \text{Narration}(\delta, \epsilon)
  \]

The result is a ‘Nixon Polygon’. There is irresolvable conflict between Narration on the one hand, and Rules 2 and 3 on the other because their antecedents are not logically related:

![Diagram](attachment:diagram.png)

In CE, conflict is never resolved if the conflicting rules have unrelated antecedents (this is shown in the appendix). So neither $\text{Narration}(\delta, \epsilon)$ nor $\neg \text{Narration}(\delta, \epsilon)$ are inferred from the above.

We assume that any KB that verifies $\langle \tau, \delta, \epsilon \rangle$ but fails to verify any discourse relation between $\delta$ and $\epsilon$ is inconsistent. And because the linguistic processing is incremental, the interpretation of the preceding discourse is taken to be fixed. Consequently, the only assumption that can be dropped from the KB in order to ameliorate the inconsistency is $\langle \tau, \delta, \epsilon \rangle$. So $\epsilon$ must be attached to $\alpha$ or $\beta$, but not $\delta$. Using Cascaded Penguin Principles and Defeasible Modus Ponens, one infers $\text{Elaboration}(\alpha, \epsilon)$ and $\text{Narration}(\beta, \epsilon)$, in agreement with intuitions.

The above shows that the Nixon Diamond provides the key to discourse popping; $\epsilon$ is attached to a constituent that dominates $\delta$ because a Nixon Diamond meant that $\epsilon$ couldn’t be attached to $\delta$ itself.

### 7.4 Dudley Doorite and Text Ambiguity

We earlier indicated that interpreting text (9) requires Closure on the Right and Dudley Doorite.
(9) The bimetallic strip changed shape. The temperature fell.

We used these inferences to motivate the following causal law:

- **Change Causal Law**
  
  \[
  \langle \tau, \alpha, \beta \rangle \land change(\text{strip}, me(\alpha)) \land fall(\text{temperature}, me(\beta)) > cause(me(\alpha), me(\beta)) \lor cause(me(\beta), me(\alpha))
  \]

Now suppose we assume that the sentences in (9) are not dominated by a common topic. This conjecture is supported by standard heuristics for defining constraints on possible topics, which entail that sentences under a common topic should share actors and/or patients (cf. Groz and Sidner 1986, Asher 1993). Then, by the contrapositive version of Common Topic for Narration, the relevant KB in analysing (9) verifies \(\neg \text{Narration}(\alpha, \beta)\). So although the antecedent to Narration is satisfied in analysing (9), \(\text{Narration}(\alpha, \beta)\) cannot be inferred.

Closure on the Right and Dudley Doorite yield the following from Result and Explanation:

**Closure on the Right on Result and Explanation**

(i) \(\langle \tau, \alpha, \beta \rangle \land cause(me(\alpha), me(\beta)) > \text{Result}(\alpha, \beta) \lor \text{Explanation}(\alpha, \beta)\)

(ii) \(\langle \tau, \alpha, \beta \rangle \land cause(me(\beta), me(\alpha)) > \text{Result}(\alpha, \beta) \lor \text{Explanation}(\alpha, \beta)\)

**Dudley Doorite on (i) and (ii)**

(iii) \(\langle \tau, \alpha, \beta \rangle \land (cause(me(\alpha), me(\beta)) \lor cause(me(\beta), me(\alpha))) > (\text{Result}(\alpha, \beta) \lor \text{Explanation}(\alpha, \beta))\)

The antecedent of Change Causal Law is satisfied by the KB. So by Defeasible Modus Ponens \(cause(me(\alpha), me(\beta)) \lor cause(me(\beta), me(\alpha))\) is inferred. By Defeasible Modus Ponens again on rule (iii), (21) is inferred.

(21) \(\text{Explanation}(\alpha, \beta) \lor \text{Result}(\alpha, \beta)\)

Thus the discourse relation between the sentences in (9) is ambiguous.\(^7\)

## 8 The Pluperfect

We have so far examined how to infer discourse relations in simple past tensed texts. To explore what role the pluperfect plays in discourse, we first consider the following texts.

(22) ?Max poured a cup of coffee. He had entered the room.

(23) Max entered the room. He poured a cup of coffee.

Intuitively, the temporal order between entering the room and pouring a cup of coffee are the same in (22) and (23). So why is (22) awkward but (23) acceptable? Intuitively, we can find a connection between the events in (23) that is compatible with the tenses used; the

\(^7\) Note that this is an informative ambiguity in that \(\text{Explanation}(\alpha, \beta) \lor \text{Result}(\alpha, \beta)\) is not a tautology.
connection is that Max entered the room so that he could pour himself a cup of coffee. On the other hand, this connection cannot be compatible with the tenses used in (22), since (22) is awkward. Theories that analyse the distinction between the simple past and pluperfect purely in terms of different relations between reference times and event times, rather than in terms of event-connections, fail to explain why (29) is acceptable but (22) is awkward.

Intuitively, a pluperfect clause $\beta$ can be connected to a simple past tense clause $\alpha$ if $\beta$ elaborates $\alpha$ (e.g. text (24)) or explains $\alpha$ (e.g. (25)).

(24) Max arrived late for work. He had taken the bus.

(25) The council built the bridge. The architect had drawn up the plans.

Indeed, it suffices for $\beta$ to be part of an elaboration or explanation of $\alpha$, for we can improve text (22) by adding to it a further clause that, together with the pluperfect clause, explains Max pouring the coffee (e.g. text (26), first cited in Caepeel 1991):

(26) Max poured himself a cup of coffee. He had entered the room feeling depressed, but now felt much better.

Furthermore, pluperfect and simple past clauses can form a ‘parallel’ under a common topic, as in text (27) (cf. Asher 1993), and contrast each other, as in (28).

(27) Max was wrong. He had been wrong. He will always be wrong.

(28) Max got the answer wrong. But John had got the the answer right.

Both the contrast and parallels must be such that the event in the pluperfect happens before that in the simple past.

This seems to exhaust the possible connections between the simple past event and the pluperfect one. This is why (22) is awkward, for it is difficult to think of the circumstances under which the entering the room explains or elaborates pouring the coffee, and they clearly cannot form parallel or contrast. Of course, many more connections are allowed between two events described in the simple past. The task now is to formalise this intuition that the discourse role of the pluperfect is to restrict the kinds of discourse connections that can hold.

Let $C_{pp}(\alpha, \beta)$ mean that $\alpha$ and $\beta$ are connected by the kind of discourse relation allowed between simple pasts and pluperfects: that is, $\beta$ is (part of) an elaboration or explanation of $\alpha$, or $\beta$ and $\alpha$ form parallel or contrast, with the event described in $\beta$ preceding that described in $\alpha$. Then the discourse role of the pluperfect is captured as follows:

- **Connections When Changing Tense (cct)**

\[ \Box (\langle r, \alpha, \beta \rangle \land sp(\alpha) \land pp(\beta) \rightarrow C_{pp}(\alpha, \beta)) \]

It’s important to stress that $C_{pp}(\alpha, \beta)$ doesn’t necessarily follow if $\beta$ is simple past rather than pluperfect. For simple past tensed texts, more connections are permissible, e.g., $Narration(\alpha, \beta)$.
Given the above rule one can explain the awkwardness of (22). If the \( \textit{wk} \) is stated as intuitions would dictate, then the \( \textit{kb} \) in analysing (22) would be one where the clauses described in (22) are not related by \( C_{pp} \). So by the contrapositive version of \( \textit{cct} \) and the fact that information states incorporate modal closure, the sentences are not related by a discourse relation; for \( \langle \tau, \alpha, \beta \rangle \) must be false. This makes (22) incoherent. Analysing (26) would involve relating whole discourse segments to a clause by a discourse relation; that is the second and third clauses togetherness must stand in the relation \( \textit{Explanation} \) to the first. Providing such analysis is beyond our scope here since we have concentrated on relations between single sentences (but see Lascarides and Asher (1993) for a detailed discussion of such cases).

\( \textit{cct} \) captures the relevant distinction between the use of the simple past tense and the pluperfect as illustrated in (29) and (30).

(29) Max slipped. He had spilt a bucket of water.

(30) Max slipped. He spilt a bucket of water.

Intuitively, the discourse relation in (29) is \( \textit{Explanation} \) and in (30) it is \( \textit{Narration} \). This difference must arise solely in virtue of the pluperfect. The analysis of (30) is exactly like that of (1); by Defeasible Modus Ponens on \( \textit{Narration} \), it’s narrative. Now consider (29). The relevant \( \textit{kb} \) satisfies the antecedents of \( \textit{Narration} \), States Overlap and the indefeasible law \( \textit{cct} \). \( \textit{cct} \) entails \( C_{pp}(\alpha, \beta) \), where \( \alpha \) and \( \beta \) are respectively the logical forms of the clauses. Now if spilling the water and spilling are connected so that either the spilling explains, elaborates, parallels or contrasts the slipping, then normally the spilling explains the slipping. This intuition is reflected in the following law, where \( \textit{Info}(\alpha, \beta) \) is the gloss for “\( \alpha \) describes Max slipping and \( \beta \) describes Max spilling a bucket of water”.

- **Slipping Law**
  \[
  \langle \tau, \alpha, \beta \rangle \land C_{pp}(\alpha, \beta) \land \textit{Info}(\alpha, \beta) \geq \textit{Explanation}(\beta, \alpha)
  \]

Thus the \( \textit{kb} \) satisfies the antecedents to the above law as well. Note that the Slipping Law is different from the causal laws considered so far, because \( C_{pp}(\alpha, \beta) \) is in the antecedent. This added conjunct is crucial to the plausibility of the above law concerning spilling and slipping. For intuitively, there is no \( \textit{wk} \) that normally the spilling caused the slipping if the choice of connection between these events encompasses the full range of possibilities, including that the slipping caused the spilling. It must be also stressed that this law plays no part in the analysis of (30); the relevant \( \textit{kb} \) doesn’t verify its antecedent, because \( C_{pp}(\alpha, \beta) \) is not in the \( \textit{kb} \).

We must investigate what follows from \( \textit{Narration} \), States Overlap and the Slipping Law in the interpretation of (29). The Slipping Law and States Overlap don’t conflict, but they each conflict with \( \textit{Narration} \) and are more specific than it. By the Penguin Principle, \( \textit{Explanation}(\alpha, \beta) \) and \( \text{overlap}(\text{\textit{me}(\alpha)}, \text{\textit{me}(\beta)}) \) are inferred; thus the antecedent to \( \textit{Background} \) is verified and \( \textit{Background}(\alpha, \beta) \) is inferred. So, spilling the water explains why Max slipped, and the consequences of spilling the water are are still in force when Max slips.

These texts show that although simple past tenses sentences are equivalent to the corresponding pluperfects they play distinct roles in discourse. Our formalism reflects the intuition that
the pluperfect acts as a syntactic discourse marker to indicate that only a restricted set of discourse relations is possible, thus yielding different inferences about discourse structure. We have used indefeasible and defeasible inference on IK to explain this and not formal devices like reference times.

We have investigated how the pluperfect sentences are related to simple past tensed ones. We now evaluate how pluperfect sentences are related to each other. Consider (31).

(31)  
  a. Max arrived late for work.  
  b. He had taken the bus.  
  c. He had totalled his car.  
  d. His boss summoned him to his office.

The theory presented here is rich enough to reflect the intuition that each pluperfect sentence in (31) explains the previous pluperfect sentence. Let the logical forms of (31a) to (31d) be respectively α, β, γ and δ. The discourse relation between α and β is worked out in an analogous way to that in (29): Background(α, β) and Explanation(α, β) are inferred. α and β are both open clauses to γ. Again, by a similar inference to that for text (29) Background(α, γ) and Explanation(α, γ) are inferred.

In connecting β to γ, the KB satisfies the antecedent of States Overlap and Narration. There is also a causal law relating totalling the car and taking the bus. By the Penguin Principle, the consequents of States Overlap and the Causal Law are inferred, and subsequently, we infer Background(β, γ) and Explanation(β, γ).

The open clauses to δ are α, β and γ. A Nixon Polygon occurs when attempting to attach δ to γ and δ to β in a similar way to that which occurred in (7) described earlier. This time, we use a constraint on Narration defined in terms of Explanation rather than Elaboration:

- Explanation(β, γ) ∧ ¬Explanation(β, δ) > ¬Narration(γ, δ)

Thus δ must attach to α. By Defeasible Modus Ponens on Narration, Narration(α, δ) is inferred. Thus the DRP representing (31) is (31').

(31') \{\{α, β, γ, δ\}, \{Explanation(α, β), Background(α, β)\} \\
Explanation(α, γ), Background(α, γ) \\
Explanation(β, γ), Background(β, γ) \\
Narration(α, δ)\}\}
Max arrived late for work  

Narration  

His boss summoned him to his office

Explanation

He had taken the bus

Explanation

He had totalled the car

The pluperfect sentences in (31) each create further subordinations in the discourse structure. But pluperfects don’t necessarily do this. Consider (32).

(32)  

a. Alexis was a really good girl by the time she went to bed yesterday.  

b. She had done her homework.  

c. She had helped her Mum with housework.  

d. She had played piano.  

e. We all felt good about it.

Suppose the logical forms of (32a) to (32e) are respectively α to ε. By a similar argument to the one above, common sense inference yields Explanation(α, β), Explanation(α, γ) and Explanation(α, δ). World knowledge does not yield any preference as to the connections between the event in γ and the event in the open clause β. So β and γ satisfy the antecedents of States Overlap and Narration, and so a Cascaded Penguin Principle yields Background(β, γ). Similarly, we infer Background(γ, δ). And as in (31), a Nixon Diamond gives rise to discourse ‘popping’ for ε, and in fact we obtain Background(α, ε).

Alexis was a good girl . . .  

Background  

We all felt good about it

Explanation

She had done her homework

Explanation

She had helped her Mum

Background

She had played piano

Background

The fact that (32b-d) form background to each other entails nothing about how the events they describe are temporally ordered, for we cannot infer from Background where the the
consequent states start relative to each other, and the corresponding events are placed at the start of these consequent states. This is in agreement with the intuitive interpretation of (32), in contrast to the order of events inferred from Narration when analysing the corresponding simple past tensed text (33).

(33) Alexis did her homework. She helped her Mum with housework. She played piano.

The events described by a sequence of pluperfect clauses will occur in their textual order only if that order is inferrable from wk or other temporal information present in the text (cf. (34)).

(34) Max arrived at the summit at midday. He had got up at 5:30am, had prepared his lunch, had chosen his route, and had passed based camp before 7am.

This is in agreement with the claim made in Kamp (1991), that the temporal order of events described by a sequence of pluperfect clauses depends on the discourse type.

9 Conclusion

We have proposed a framework for calculating the structure of text, where the contributions made by syntax, semantic content, causal knowledge and linguistic knowledge are all explored within a single logic. The distinct discourse relations that are prevalent in texts with similar syntax arose from defeasible laws, by using intuitively compelling patterns of defeasible entailment.

We argued that a full account of the simple past and pluperfect tenses exemplify the inference patterns of Defeasible Modus Ponens, The Penguin Principle, the Nixon Diamond, Closure on the Right, and Dudley Doorite. Closure on the Right and Dudley Doorite provided the key to discourse structure ambiguity. The Nixon Diamond provided the key to ‘popping’ from subordinate discourse structure. And the Penguin Principle captured the intuition that the reader never ignores information relevant to calculating discourse structure.

We examined the effects of wk and lk on interpretation in a logical context. Consequently, the traditional DRT syntactic-based account for calculating relations between reference times in order to determine temporal structure was not needed. The distinct discourse roles of the simple past and the pluperfect were brought out through a mixture of defeasible and indefeasible reasoning, rather than by different relations between reference times determined in syntax.

33
Appendix

The Language

The basic building blocks of DRPs are DRSS and discourse relations between them. In order to simplify the proofs in this appendix, we make some simplifying assumptions about the language for reasoning about discourse structure. In particular, the language in this appendix will not make full use of the truth definitions of DRSS. We are able to simplify things in this way because the only semantic information that’s part of a DRS and relevant to constructing discourse structure—such as the information that the event described is Max falling—can be represented as a predicate which takes the DRs as an argument. In other words, for simplicity, we re-write \( \text{fall}(\text{Max}, \text{me}(\alpha)) \) as \( \text{Max fall}(\alpha) \). The second simplification concerns the function \( \text{me} \) (standing for “main eventuality”). In the text, \( \text{me} \) is a partial function \( \text{me} : \text{DRS} \rightarrow U_{\text{DRS}} \), where \( U_{\alpha} \) is the universe of the DRs \( \alpha \) and \( \text{me}(\alpha) \) is the main eventuality discourse referent as defined in (Asher 1993). But we can for the sake of reasoning about DRP construction rephrase the function \( \text{me} \) and relations involving main events of DRSS as relations on the DRSS themselves. These two moves make the proof theory simpler. In particular our language will remain that of propositional logic. We call this propositional language for reasoning about DRP construction \( L_{\text{DRP}} \).

We can essentially treat DRSS as atomic propositions in \( L_{\text{DRP}} \). But this simplification comes with a cost. \( L_{\text{DRP}} \) is capable of expressing the fact that a DRs is true, but this assignment is independent of the assignment of truth values to DRSS given in the standard truth definition for DRSS below. If we wish, we may restrict our attention to those \( L_{\text{DRP}} \) models in which the assignment of truth values to DRSS and to predicates involving DRSS reflects the values assigned in the standard interpretation of DRSS. But we leave open the question of how the proofs in this appendix must be extended so as to apply to this class of models.

The Standard Truth Definition for DRSS

We give here the semantics of atomic DRSS, which are the only kind used in this paper. A full truth definition for DRP can be found in Kamp and Reyle (in press).

- If \( \psi \) is an n-ary DRs predicate and \( x_1, \ldots, x_n \) are discourse references, then \( \psi(x_1, \ldots, x_n) \) is an atomic condition.

- If \( x_1 \) and \( x_2 \) are discourse references (of any kind), then \( x_1 = x_2 \) is an atomic condition.

- A DRs is a pair \( \langle U, \text{Con} \rangle \), where \( U \) is a set of discourse referents, and \( \text{Con} \) is a set of conditions.

The semantics of DRSS are defined with respect to a model \( \langle W, T, D, E, [] \rangle \), where \( W \) is a non-empty set of possible worlds; \( T \) is a non-empty set of time points; \( D \) is a function from \( W \) into a family of non-empty sets \( D(w) \) is the domain of individuals in \( w \); \( E \) is a function from \( W \) into a family of non-empty sets \( E(w) \) is the domain of eventualities in
$w$; and $[]$ is an interpretation function that assigns to DRS predicates functions from $W$ to $\wp(\cup_{w \in W} (D \cup E)^n \cup T)$.

A proper embedding of a DRS $K$ in a model $M$ is defined in terms of a function from discourse referents into objects $O_M$ in $M$ ($O_M = D_M \cup E_M \cup T_M$). Any such function from discourses references into $O_M$ is an embedding function.

Define $g$ to extend an embedding function $f$ to an embedding of $K$ in $M$ at $w$ (written $g \supseteq_K f$) just in case $\text{Dom}(g) = \text{Dom}(f) \cup U_K$.

Define an external anchor $A$ for $K$ in $M$ to be a partial function from $U_K$ into $\cup_{w \in W} D_w \cup T$, such that if now occurs in $U_K$ then $A(\text{now})$ is the utterance time of the discourse, and if $i$ occurs in $U_K$, then $A(i)$ is the speaker of the discourse.

Now we define a proper embedding $f$ of $K$ in $M$ at $w$ (written $[f, K]_M^w w$) with respect to a possibly empty external anchor $A$ for $K$ in $M$ and we define satisfaction of a condition in $M$ relative to an embedding function $f$ for the DRS in which the conditions occur at $w$ (written $M \models_{w, f} \theta$).

(i) If $\psi$ is an atomic condition of the form $\phi(x_1, \ldots, x_n)$, then $M \models_{w, f} \psi$ iff $(f(x_1), \ldots, f(x_n)) \in \llbracket \phi \rrbracket (w)$.

(ii) If $\psi$ is an atomic condition of the form $x_1 = x_2$, then $M \models_{w, f} \psi$ iff $f(x_1) = f(x_2)$.

(iii) If $A$ is an external anchor for $K$ in $M$, then $[f, K]_M^w : (i) \quad f \supseteq_K g$; (ii) $A \subseteq f$; (iii) $\forall \theta \in \text{Con}_K, M \models_{w, f} \theta$.

Definition of Main Eventuality

To define $me(\alpha)$, we assume the theory is expressed in DRT with the syntax analysed in GPSG. Under these circumstances, the definition is as follows: For a non-conjunctive clause $\alpha$, $me(\alpha)$ is the eventuality discourse entity introduced by the verb phrase that heads the clause.

The Language $L_{DRP}$

The language of $L_{DRP}$ is built recursively in the usual way:

- DRS names $\alpha, \beta, \gamma$ are well formed expressions of $L_{DRP}$, and DRP names $\tau$ and $\tau'$ are well-formed expressions of $L_{DRP}$.
- If $\alpha$ is a DRS name or DRP name, then $\downarrow \alpha$ is a well-formed formula (WFF) of $L_{DRP}$.
- If $\alpha_1, \ldots, \alpha_n$ are DRS names, and $p_n$ is an $n$-place predicate on DRS names, then $p_n(\alpha_1, \ldots, \alpha_n)$ is an atomic WFF.
- If $\alpha$ and $\beta$ are WFF, then $\alpha \land \beta, \alpha \lor \beta, \neg \alpha, \alpha \to \beta, \alpha > \beta$ and $\Box \alpha$ are WFF.
- If $\tau$ is a DRP name and $\alpha$ and $\beta$ are DRS names, then $\langle \tau, \alpha, \beta \rangle$ is a WFF.
- If $\phi, \psi$ and $\chi$ are WFF, then $(\phi, \psi) > \chi$ is a WFF.

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The Truth Definition for \(L_{\text{DRP}}\)

The well-formed expressions of the language are defined with respect to a model \(\langle W, *, f \rangle\) for the language, where \(f\) assigns DRS and DRP names functions from \(W\) to propositions (which in turn are functions from \(W\) to \(\{0, 1\}\)), and assigns predicate constants functions from \(W\) to suitable sets of propositions.

(a) Where \(\beta\) is either a name constant or a predicate constant, \([\beta]^M(w) = f(\beta)(w)\).

(b) Where \(\beta\) is a DRS or DRP name, \(\lceil \downarrow \beta \rceil^M(w) = (f(\beta))(w)\).

(c) Where \(\beta\) is an atomic wff \(p^n(d_1, \ldots, d_n)\),
\[ [\beta]^M(w) = 1 \text{ iff } \langle [d_1]^M(w), \ldots, [d_n]^M(w) \rangle \text{ belongs to } [p^n]^M(w). \]

(d) \([A \land B]^M(w) = 1 \text{ iff } [A]^M(w) = 1 \text{ and } [B]^M(w) = 1.\]

(e) \([\phi > \psi]^M(w) = 1 \text{ iff } *(w, [\phi]^M) \subseteq [\psi]^M\]

(f) \([\square \phi]^M(w) = 1 \text{ iff for all } w', [\phi]^M(w') = 1\]

(g) \([\langle \phi, \psi \rangle > \chi]^M(w) = 1 \text{ iff } *(w, [\phi]) \cap *(w, [\psi]) \subseteq [\chi]\]

Constraints on the Model

The function * must satisfy the following constraints for the model to be admissible:

- **Facticity**
  \(*\langle w, p \rangle \subseteq p\)

- **Specificity**
  If \(p \subseteq q\), \(*\langle w, p \rangle \cap *(w, q) = \emptyset\), then \(*\langle w, q \rangle \cap p = \emptyset\)

- **Dudley Doorite**
  \(*\langle w, p \cup q \rangle \subseteq *\langle w, p \rangle \cup *\langle w, q \rangle\)

Facticity captures the intuition that whatever the properties of a normal bird, one is that he’s a bird. Specificity captures the intuition that normal birds aren’t penguins. Dudley Doorite captures the intuition that if quakers are pacifists and republicans are pacifists, then quakers and republicans are pacifists.\(^8\) We will henceforth restrict ourselves to admissible models.

Monotonic Proof in CE

The monotonic theory of CE in (Asher and Morreau 1991) is to be strengthened by the following axiom schemata which reflect S5 ‘modal closure’ instead of just logical closure.

\[(A1)\quad \phi \text{ where } \phi \text{ is a tautology.}\]

\(^8\) In fact, Specificity follows from Dudley Doorite.
(A2) \( \phi > \phi \)

(A3) \( (\phi > \psi \land \zeta > \psi) \rightarrow ((\phi \lor \zeta) > \psi) \)

(A4) \( ((\phi, \psi) > \bot \land \Box(\phi \rightarrow \psi)) \rightarrow \psi > \neg \phi \)

(A5) \( (\phi > \psi) \rightarrow ((\phi, \psi) > \psi) \)

(A6) \( ((\phi, \psi) > \chi) \leftrightarrow ((\zeta, \phi) > \chi) \)

(A7) \( (\phi > \chi \land \psi > \chi) \rightarrow (\phi, \psi) > \chi \)

(A8) \( (\phi, \psi) > \psi \rightarrow \phi > \psi \)

(A9) \( \Box (\phi \leftrightarrow \psi) \rightarrow ((\phi > \zeta) \leftrightarrow (\psi > \zeta)) \)

(A10) \( \Box (\phi \rightarrow \psi) \rightarrow ((\zeta > \phi) \rightarrow (\zeta > \psi)) \)

(A11) \( \Box \phi \rightarrow \phi \)

(A12) \( \Box (\phi \rightarrow \psi) \rightarrow (\Box \phi \rightarrow \Box \psi) \)

(A13) \( \Diamond \phi \rightarrow \Box \Diamond \phi \).

(R) \( ((\phi \rightarrow \psi) \land \phi) \rightarrow \psi \)

(R1) If \( \vdash \phi \), then \( \vdash \Box \phi \)

Let the above axioms and rules be called \( T_0 \). We will write \( \vdash_{T_0} \) for the derivability notion, and we define the \( L_{\text{DRP}} \) consequence to be the following:

- **\( L_{\text{DRP}} \) Consequence**

  \( \Gamma \models_{L_{\text{DRP}}} \phi \) iff for every admissible \( L_{\text{DRP}} \) model \( M \) and for every world \( w \) in \( W_M \) if every element of \( \Gamma \) is true at \( w \) in \( M \) then \( \phi \) is true at \( w \) in \( M \).

**Fact:**

\( \Gamma \vdash_{T_0} \phi \Rightarrow \Gamma \models_{L_{\text{DRP}}} \phi \)

To prove completeness, we construct a canonical model in the usual fashion for propositional modal logic, except that we add a construction for \( * \). Each world in the set of worlds \( \Box \) in the canonical model is defined to be a maximal consistent set of sentences, and we may for each such set \( \Gamma \) and each formula \( \psi \) define:

\( \Gamma^+ = \{ \phi: (\psi > \phi) \in \Gamma \} \)

\( \Gamma^- = \{ \phi: (\neg (\psi > \phi)) \in \Gamma \} \)

\( *(\Gamma, [\phi]) = \{ \Gamma' \in W : \Gamma^+_\psi \subseteq \Gamma' \} \).

This construction suffices to yield a canonical model such that one can then prove:

**Fact:**

\( \Gamma \models_{L_{\text{DRP}}} \phi \Rightarrow \Gamma \vdash_{T_0} \phi \)
We mention one other result about propositional CE, which one can prove using the filtration method (cf. Chellas 1980):

**Fact:** $T_0$ has the finite model property, and so is decidable.

The Nonmonotonic Part of CE

Just as in (Asher and Morreau 1991), we define CE entailment, written $\models_*$, in terms of the function $*$ on information states, the update function $+$, and the normalisation function $N$. These three functions are defined as follows:

**Definition of $*$ on information states:** $*(s,p) = \bigcup_{w \in s} \ast (w,p)$

**Definition of $+$:** $s + \Gamma = \{ w \in s : w \models \Gamma \}$

**Definition of Normalisation:**

$$N \ast (s,p) = \{ w \in s : w \not\in p \setminus \ast (s,p) \} \text{ if } \ast (s,p) \cap s \neq \emptyset$$

$$s \text{ otherwise}$$

The definition of $\models_*$ uses the notion of normalisation chain derived from $N$ as follows:

**Definition of $\text{Ant}(\Gamma)$:** Where $\Gamma$ is a set of sentences of $L_{DRP}$ we define $\text{Ant}(\Gamma)$ to be

$$\{ \phi : \phi > \psi \text{ occurs positively as a subset of a formula of } \Gamma \}$$

$\text{Cons}(\Gamma)$—the set of consequents of conditionals in $\Gamma$—is defined analogously to $\text{Ant}(\Gamma)$.

**Definition of $\Gamma$-normalisation chain:** For $\Gamma \subseteq L_{DRP}$, the $\Gamma$-normalisation chain with respect to an enumeration $\mu$ of $\text{Ant}(\Gamma)$ is defined to be the following sequence:

$$N_0^\mu = s$$

$$N_{\alpha+1}^\mu = N(N_\alpha^\mu(\phi)), \text{ where } \alpha = \lambda + n + 1, \text{ and } \nu(\phi) = n + 1$$

$$N_\lambda^\mu = \bigcap_{\mu \in \lambda} N_\mu^\mu$$

**Definition of $\models_*$:** $\Gamma \models_* \phi$ iff for any $\Gamma$-normalisation chain $C$ beginning from $\bigcirc + \Gamma$, $C^\ast \models \phi$, where $C^\ast$ is the fixpoint of $C$, where $\bigcirc$ is the set of worlds constructed in the canonical model.

When $\Gamma$ is finite note that $\text{Ant}(\Gamma)$ is finite. And when $\text{Ant}(\Gamma)$ is finite and $\Gamma$ has no embedded $\rhd$-formulae within $\rhd$-formulae, it is easy to see that all normalisation chains defined with respect to $\text{Ant}(\Gamma)$ reach a fixed point after finitely many normalisations. Together with the fact that $T_0$ has the finite model property, we can show the following:

**Fact:** $\models_*$ is decidable.

We will be working in the canonical model $\bigcirc$. So in particular we will often define information states for various theories in terms of the operations of (Asher and Morreau 1991) — e.g. the information state $S$ corresponding to a theory $T$ will be defined as $S = \bigcirc + T$. The following definitions will also be useful.

**Definition:** Let $T$ be a theory. $\text{Formula}(T) = \{ \phi : \phi \in \text{Ant}(T) \vee \phi \in \text{Cons}(T) \vee T \models \phi \}$.

**Definition:** Let $T$ be a theory. Then $\phi$, $\psi$ are $T$-independent iff any boolean combination of $\phi$ and $\psi$ is consistent with $T$.

**Definition:** Two sets of formulae $X$, $Y$ are $T$-independent iff $\forall \phi \in X$, $\forall \psi \in Y$, $\phi$, $\psi$ are $T$-independent.
Fact: Let $T$ be any theory, and let $T_1, \ldots, T_n$ be subtheories such that every $\text{Formula}(T_i)$ and $\text{Formula}(T_j)$, $i \neq j$ are $T$-independent. Then $\text{Formula}(T_i) \cap \text{Formula}(T_j) = \emptyset$.

Definition: A $T$ survivor world $w$ is a world that survives on every normalisation chain defined with respect to $\text{Ant}(T)$ and which verifies $T$ in $\mathbb{C}$.

Definition: A default theory is a set of $> \rangle$ conditionals.

Definition: $* \uparrow (T, w)$ is the $*$ function restricted to $\text{Ant}(T)$ at $w$.

Definition: $\text{Th}(w \uparrow L_T) = \{ \phi \in L_{\text{DRP}} \cap L_T : w \models \phi \}$

We will use the term theory here in a colloquial sense; we will not assume as is standard in logic that a theory is closed under some notion of logical consequence. Rather, our theories are collections of sentences that constitute the reader’s knowledge, as described in the paper.

We now prove the lemmas that enable us to divide these theories into subtheories in CE under special circumstances. These will be used to model the Cascaded Penguin Principle.

Irrelevance Lemma

Suppose $T$ is a theory and $T_1, \ldots, T_n$, $T_i \subseteq T$ are default theories such that $\cup T_i = T$. If $\text{Formula}(T_i)$ and $\text{Formula}(T_j)$ for $i \neq j$ are $T$-independent, then for any $T_i$ and $T_j$ survivor world $w_1$, if each $T_j$ for $j = 1, \ldots, n$ has a survivor world then there is a $T$ survivor world $w_1$ such that $* \uparrow (T_i, w_1) = * \uparrow (T_i, w_i)$ and $\text{Th}(w_1 \uparrow \text{Formula}(T_i)) = \text{Th}(w_i \uparrow \text{Formula}(T_i))$.

Proof

Suppose $T_1, \ldots, T_n$ are as above and suppose all the individual $T_j$ have survivor worlds. Let $w_0$ be a $T_i$ survivor world. By assumption $T_1$ has a survivor world $w_1$. By independence, $\exists w'_1$ such that $w'_1$ is a survivor world for $T_1$ and $\text{Th}(w'_1 \uparrow \text{Formula}(T_i)) = \text{Th}(w_0 \uparrow \text{Formula}(T_i))$.

Furthermore, by the assumption of independence, $\text{Ant}(T_1) \cap \text{Ant}(T_i) = \emptyset$. So we may choose $w'_1$ such that for each $p \in \text{Ant}(T_i)$, $*(w'_1, p) = *(w_0, p)$. Since by hypothesis each $T_j$ is independent from $T_i$, we can repeat this for $T_2, \ldots, T_n$ and so construct a $T$ survivor world.

Strengthened Irrelevance Lemma

Suppose $T$ is a theory and $T_1, \ldots, T_n$, $T_i \subseteq T$ are default theories such that $\cup T_i = T$. If $\text{Formula}(T_i) \supseteq \Delta$ and $\text{Formula}(T_j) \supseteq \Delta$ for $i \neq j$ are $T$-independent for some $\Delta \subseteq L_{T_k \cap \ldots \cap T_m}$ and there are survivor worlds $w_k, \ldots, w_m$ for $T_k, \ldots, T_m$ respectively such that for each $\delta \in \Delta$ and each $w$, $w' \in \{w_k, \ldots, w_m\}$ $*([\delta], w) = *([\delta], w')$, then for any $T_i$ survivor world $w_0$, there is a world $w_1$ such that $w_1$ is a $T$ survivor, provided $T$ has a survivor. And further $* \uparrow (T_i, w_1) = * \uparrow (T_i, w_0)$, $\text{Th}(w_1 \uparrow \text{Formula}(T_i)) = \text{Th}(w_0 \uparrow \text{Formula}(T_i))$.

Proof

Suppose again $w$ is a $T_i$ survivor world and suppose that $T_1$ has a survivor world $w_1$. If every $T_i$ formula is $T$-independent of every $T_1$ formula, then by the irrelevance lemma we have a survivor for $T_i$ and $T_1$. Now suppose that $T_i$ and $T_1$ share a common set of formulas $\Delta$. By hypothesis the propositions $p$ defined by the common formulas in $\text{Ant}(T_i)$ and $\text{Ant}(T_1)$ are such that any $T_i$ survivor world $w_i$, $*(w_i, p) = *(w_1, p)$. Again by using the irrelevance lemma on the independent formulae in $\text{Formula}(T_j) \supseteq \Delta$, we can show that there is a survivor $w_2$ such that $\text{Th}(w_2 \uparrow \text{Formula}(T_i)) = \text{Th}(w_1 \uparrow \text{Formula}(T_i))$. Again by extending the argument to all the subtheories, we get the desired result. □.
It seems that we may strengthen the irrelevance still further in the case where for each of the common formulae in $\Delta$ among the theories $T_k, \ldots, T_m$ there are survivor worlds $w_k, \ldots, w_m$ that can be ordered in such a way that $*([\delta], w_j) \subseteq *([\delta], w_i)$ for $i \leq j$ then a $T$ survivor world may be constructed from any $T_i$ survivor by following the procedure already outlined and then taking for the common predicates the strongest or smallest set of normal worlds. That a world $w$ is a $T_i$ survivor depends solely on the structural relationship between the survivor world and the set of normal worlds it assigns to $[\phi]$ for $\phi \in \text{Ant}(T_i)$. By the hypothesis and the construction procedure suggested, this relationship is preserved. We formalise this observation in the following lemma, but first some definitions:

**Definition:** Suppose $T_1, \ldots, T_n$ are sets of $\geq$-sentences, such that $T = T_1 \cup \ldots \cup T_n$ and either:

(a) $\text{Formula}(T_i), \ldots, \text{Formula}(T_n)$ are $T$-independent (if distinct), or

(b) $T_j \ldots T_m$ have a common set of formulae $\Delta$ such that

$\text{Formula}(T_1), \ldots, \text{Formula}(T_j-1)$,

$\text{Formula}(T_j) - \Delta, \ldots, \text{Formula}(T_m) - \Delta$,

$\text{Formula}(T_{m+1}), \ldots, \text{Formula}(T_n)$

are $T$-independent (if distinct), and there are survivor worlds $w_j, \ldots, w_m$ of $T_j, \ldots, T_m$ that can be ordered such that for each $\delta \in \Delta$ $*([w_i, \delta]) \subseteq *([w_j, \delta])$ for $i < j$.

Then we say $T_1, \ldots, T_n$ has the *chain survivor property*.

**Definition:** Suppose $T_1, \ldots, T_m$ are theories such that $T_1 \vDash \phi_1$ and $\phi_1 \in T_2, T_2 \vDash \phi_2$ and $\phi_2 \in T_3, \ldots, T_{m-1} \vDash \phi_{m-1}$ and $\phi_{m-1} \in T_m$ and that $\cup T_i \setminus \{\phi_1, \ldots, \phi_m\} = T$. Then we say that $T_1, \ldots, T_m$ are *default expanded subtheories of* $T$.

**Starkly Strengthened Irrelevance Lemma (ssI)**

Suppose $T$ is a theory and $T_1, \ldots, T_n$ are default expanded subtheories of $T$. If $\text{Formula}(T_i) - \Delta, \text{Formula}(T_j) - \Delta$, are $T$-independent for $i \neq j$ for some set $\Delta \subseteq L_{T_k} \cap \ldots \cap L_{T_m}$ and there are survivor worlds $w_k, \ldots, w_m$ for $T_k, \ldots, T_m$ respectively such that for each $\delta \in \Delta$ such that $T_k, \ldots, T_m$ have the chain survivor property with respect to $\delta$, then for any $T_i$ survivor world $w_0$ there is a world $w_1$ such that $w_0$ is a $T$ survivor and $*([w_1, \psi]) = *(w_0, \psi)$ for all independent formulae in $\text{Formula}(T_i)$, and for any common formula $\delta \in \Delta$, $*([w_1, \delta]) \subseteq *([w_0, \delta])$ and if $w_0 \in S_i \cap *([w_1, \delta])$ then $w_1 \in S_i \cap *([w_1, \delta])$.

**Corollary:**

Given a theory $T$ and subtheories $T_1, \ldots, T_n$ such that $\text{Formula}(T_i) - \Delta$ and $\text{Formula}(T_j) - \Delta$ are $T$-independent for $i \neq j$ for some set $\Delta \subseteq T_k \cap \ldots \cap T_m$ and these subtheories have the chain survivor property with respect to any $\delta \in \Delta$, then if $T_i \vDash \phi_i$ then $T \vDash \phi$.

The proof of this follows from the fact that for any $T_i$ subtheory the nonmonotonic consequences are verified by the construction of a survivor world (see propositions 1 - 6 in Asher and Moreau 1991). By the starkly strengthened irrelevance lemma (ssI) we can construct a survivor world that also survives through all of the normalisation chains defined by $\text{Ant}(T)$.

We now turn to the patterns that are commonly used in this paper to explain the examples. There are three: the Cascaded Penguin Principle, the Nixon Polygon, and the Double Penguin Principle. We give a short analysis of each one within this framework.
We will make use of the following fact: If \( \mathcal{A} \) is an admissible model of \( L_{DPR} \) in which there is a \( T \)-survivor world \( w \) then the theory of \( w \) is an element of \( \mathcal{W} \). We will plan to construct small models to verify the defeasible inference patterns that we use.

**The Cascaded Penguin Principle**

Consider text (2).

(2) Max fell. John pushed him.

The theory \( T \) relevant to this example consists of the following:

**The Basic Axioms**

\[
\langle \tau, \alpha, \beta \rangle > \text{Narration}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Cause}(\beta, \alpha) > \text{Explanation}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta) > \text{Cause}(\beta, \alpha)
\]

**The Axioms of Temporality**

\[ \Box(\text{Cause}(\beta, \alpha) \rightarrow \neg \text{Narration}(\alpha, \beta)) \]

\[ \Box(\text{Narration}(\alpha, \beta) \rightarrow \neg \text{Explanation}(\alpha, \beta)) \]

The information state \( S_0 \) that is to be normalised contains all this information. In addition it verifies: \( \langle \tau, \alpha, \beta \rangle \) and \( \text{Info}(\alpha, \beta) \). And by axiom (A4) we also have:

\[
\langle \tau, \alpha, \beta \rangle > \neg \text{Cause}(\beta, \alpha)
\]

\[
\langle \tau, \alpha, \beta \rangle > \neg \text{Info}(\beta, \alpha)
\]

We will isolate the following default expanded subtheories of \( T \) that allow us to use the ss1.

**\( T_1 \):**

\[
\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle > \text{Narration}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta) > \text{Cause}(\beta, \alpha)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta) > \langle \tau, \alpha, \beta \rangle
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta) > \neg \text{Narration}(\alpha, \beta)
\]

\[ \Box(\text{Cause}(\beta, \alpha) \rightarrow \neg \text{Narration}(\alpha, \beta)) \]

\[ \Box(\text{Narration}(\alpha, \beta) \rightarrow \neg \text{Explanation}(\alpha, \beta)) \]

**\( T_2 \):**

\[
\langle \tau, \alpha, \beta \rangle \land \text{Cause}(\beta, \alpha)
\]

\[
\langle \tau, \alpha, \beta \rangle > \text{Narration}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Cause}(\beta, \alpha) > \text{Explanation}(\alpha, \beta)
\]

\[
\langle \tau, \alpha, \beta \rangle \land \text{Cause}(\beta, \alpha) > \langle \tau, \alpha, \beta \rangle
\]

\[ \Box(\text{Narration}(\alpha, \beta) \rightarrow \neg \text{Explanation}(\alpha, \beta)) \]

\( T_1 \) and \( T_2 \) have common formulas except for \( \text{Info}(\alpha, \beta) \), which is independent of all the others. We want to check that \( T_1 \) and \( T_2 \) have the chain survivor property with respect to their common vocabulary. Of course, all this can only be checked given the construction of an appropriate \( T_1 \) and \( T_2 \) survivor world and checking the properties. First, we turn to a \( T_1 \) survivor world. \( w_0 \) below is an appropriate \( T_1 \) survivor world.
The normal worlds above (drawn as the quadrangles) verify the formulae to their sides. It can be checked that the model above is an admissible \( L_{DRP} \) model subject to the following proviso: for any proposition \( p \neq [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \) and \( p \neq \langle \langle \tau, \alpha, \beta \rangle \rangle \), \(*w_0, p = *w_0, p = p*\).

We now show that \( w_0 \) is a survivor world for \( T_1 \). Typically in CE we do so by induction on the length of normalisation chains. Given that \( \text{Ant}(T_0) \) is finite, however, the chains are finite; in fact there are just two sorts of normalisations one with \( [\langle \tau, \alpha, \beta \rangle] \) and one with \( \langle [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \rangle \). The information state, \( S_0 \) verifies the axioms and the information \( \langle \tau, \alpha, \beta \rangle \) and \( \text{Info}(\alpha, \beta) \). So clearly, \( w_0 \in S_0 \).

**Lemma 1**
If \( w_0 \in S \), then \( w_0 \in N* (S,p) \), where \( p \in \{ [\langle \tau, \alpha, \beta \rangle], [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \} \).

**Proof**
Suppose \( w_0 \in S_0 \) and \( \phi = [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \). \( w_0 \in *w_0, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \) and so \( w_0 \in *w_0, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \) and so

\[
N * (S, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)]) = \{ w \in S : w \not\in [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \ \land \ *w_0, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \}
\]

Since \( w_0 \in *w_0, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \) and \( w_0 \in S \) by hypothesis, \( w_0 \in N* (S, [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \). Now suppose \( \phi = [\langle \tau, \alpha, \beta \rangle] \). Then \( w_0 \not\in *w_0, [\langle \tau, \alpha, \beta \rangle] \). But \( *w_0, [\langle \tau, \alpha, \beta \rangle] \not\models \text{Info}(\alpha, \beta) \) and \( S \models \text{Info}(\alpha, \beta) \). So \( S \cap *w_0, [\langle \tau, \alpha, \beta \rangle] = \emptyset \). So \( N * (S, [\langle \tau, \alpha, \beta \rangle]) = S \) and so \( w_0 \in N * (S, [\langle \tau, \alpha, \beta \rangle]). \) □
Given that \( w_0 \) is a \( T_1 \) survivor world, we now show that the fixpoint of every normalisation chain leading from \( S_0 \) verifies \( \neg \text{Narration}(\alpha, \beta) \) and \( \text{Cause}(\beta, \alpha) \).

**Fact 2**

\[ T_1 \models \neg \text{Narration}(\alpha, \beta) \land \text{Cause}(\beta, \alpha) \]

**Proof**

Suppose that there is a chain \( C \) such that the fixpoint \( C_\lambda \) contains a world \( v \) such that \( v \models \neg (\neg \text{Narration}(\alpha, \beta) \land \text{Cause}(\beta, \alpha)) \). So \( v \models \text{Narration}(\alpha, \beta) \lor \neg \text{Cause}(\beta, \alpha) \). Then \( v \models C_\lambda [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \). But then \( v \in *\langle C_\lambda [\langle \tau, \alpha, \beta \rangle \land \text{Info}(\alpha, \beta)] \rangle \). So then \( v \models \neg \text{Narration}(\alpha, \beta) \land \text{Cause}(\beta, \alpha) \), which contradicts our hypothesis. \( \square \)

Now we turn to the appropriate \( T_2 \) survivor world \( w_2 \). Given \( T_1, T_2 \) is a default expanded subtheory of \( T \). Here now is the normal worlds set-up for \( T_2 \).

![Diagram](image)

The normal worlds for the other propositions can be filled in; only the above are relevant to making our point. This is also a DRP admissible model subject to the following proviso: for any proposition \( p \neq \langle \tau, \alpha, \beta \rangle \land \text{Cause}(\beta, \alpha) \), \( p \neq \langle \tau, \alpha, \beta \rangle \), \(*\langle w_2, p \rangle = *\langle w_3, p \rangle = p \).

Suppose \( S_1 \models T_2 \). The proof that \( w_2 \) is a \( T_2 \) survivor world and that the fixpoints of every normalisation chain defined on \( S_1 \) goes exactly as before. But note that by the construction the common predicates for \( T_1 \) and \( T_2 \) have the chain survivor property with respect to these formulas. By \text{ss1}, there is a common survivor world for \( T \) and the fixpoint of every normalisation chain defined with respect to \( T \) verifies the conjunction of all formulas verified by each local fixpoint: i.e. \( \neg \text{Narration}(\alpha, \beta), \text{Explanation}(\alpha, \beta) \) and \( \text{Cause}(\beta, \alpha) \).

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This verifies the desired conclusions of the Cascaded Penguin.

The Nixon Polygon

Consider text (7).

(7)  a. Guy experienced a lovely evening last night.
    b. He had a great meal.
    c. He ate salmon.
    d. He devoured lots of cheese.
    e. He won a dancing competition.

Let us assume a constituent $\alpha$ about a dinner, is elaborated by constituents $\beta_1$ and $\beta_2$ — about various courses. We now consider how to attach a constituent $\beta_3$ about winning a dance competition to this text structure. Both $\beta_2$ and $\alpha$ are open for $\beta_3$ and we have to look at both possibilities.

We suppose a basic information state verifying the following subtheories:

$T_1$:

$Elaboration(\alpha, \beta_2) \land \langle \tau, \alpha, \beta_3 \rangle \land \langle \tau, \beta_2, \beta_3 \rangle$

$\langle \tau, \alpha, \beta_3 \rangle > \neg Elaboration(\beta_3, \alpha)$

$\Box (Narration(\alpha, \beta_3) \rightarrow \neg Elaboration(\alpha, \beta_3))$

$T_2$:

$\langle \tau, \alpha, \beta_3 \rangle \land \neg Elaboration(\alpha, \beta_3) \land \langle \tau, \beta_2, \beta_3 \rangle \land Elaboration(\alpha, \beta_2)$

$\langle \tau, \beta_2, \beta_3 \rangle > Narration(\beta_2, \beta_3)$

$Elaboration(\alpha, \beta_2) \land \neg Elaboration(\alpha, \beta_3) > \neg Narration(\beta_2, \beta_3)$

$\Box (Narration(\alpha, \beta_3) \rightarrow \neg Elaboration(\alpha, \beta_3))$

A survivor world for $T_1$ is not difficult to construct. But a survivor world for $T_2$ is more involved. Let $w_0$ verify $Narration(\beta_2, \beta_3), \langle \tau, \beta_2, \beta_3 \rangle$ and $\langle \tau, \alpha, \beta_3 \rangle$. And let $w_1$ verify $\neg Narration(\beta_2, \beta_3), \neg Elaboration(\alpha, \beta_3), Elaboration(\alpha, \beta_2)$ and $\langle \tau, \alpha, \beta_3 \rangle$. Then we show:

Lemma 5

$w_0$ survives to the fixpoint of any $T_2$ normalisation chain in which no normalisation of the form $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle)$ occurs in $C$ prior to a normalisation of the form $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle)$. And $w_1$ survives to the fixpoint of any $T_2$ normalisation chain in which no normalisation of the form $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle)$ occurs before a normalisation of the form $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle)$.

The proof of the two cases is completely symmetric. So let us illustrate by taking the case of $w_0$ first. Suppose no normalisation of the form $N \ast (S_m, \neg Elaboration(\alpha, \beta_3))$ occurs in $C$ prior to a normalisation of the form $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle)$. There are only three sorts of links in a $T_2$ normalisation chain: $N \ast (S_m, \langle \tau, \beta_2, \beta_3 \rangle), N \ast (S_m, \neg Elaboration(\alpha, \beta_3))$ and $N \ast (S_m, Elaboration(\alpha, \beta_2) \land \neg Elaboration(\alpha, \beta_3))$. By the specification of $w_0$ above $w_0 \models T_2$. If $S = \bigcirc + T_2$, then $w_0 \in S$. $w_0 \in *\langle w_0, \langle \tau, \beta_2, \beta_3 \rangle \rangle$, so $(S, \langle \tau, \beta_2, \beta_3 \rangle) \cap S \neq \emptyset$ and so
\[ N \ast (S, [\langle \tau, \beta_2, \beta_3 \rangle]) = \{ w \in S : w \not\in [\langle \tau, \beta_2, \beta_3 \rangle] \setminus (N(S, [\langle \tau, \beta_2, \beta_3 \rangle]) \}
\]
and
\[ w_0 \in N \ast (S_m, [\langle \tau, \beta_2, \beta_3 \rangle]). \]

Let \( N \ast (S_m, [\langle \tau, \beta_2, \beta_3 \rangle]) = S' \). Suppose now that \( N \ast (S', \lnot \text{Elaboration}(\alpha, \beta_3)) \) is the next normalisation in the chain prior to the fixpoint of \( N(S'', \lnot \text{Elaboration}(\alpha, \beta_3)) \). Since \( S'' \models \text{Narration}(\beta_2, \beta_3) \) but \( S'' \models \text{Elaboration}(\alpha, \beta_2) \land \lnot \text{Elaboration}(\alpha, \beta_3) > \neg \text{Narration}(\beta_2, \beta_3) \), \( S'' \cap (N(S'', \lnot \text{Elaboration}(\alpha, \beta_3)) = \emptyset \).

So \( N \ast (S'', \lnot \text{Elaboration}(\alpha, \beta_3)) = S'' \)

But then \( w_0 \in N \ast (S'', \lnot \text{Elaboration}(\alpha, \beta_3)) \). A similar argument shows that \( w_0 \) survives if the normalisation chain with respect to:

\[ \text{Elaboration}(\alpha, \beta_2) \land \lnot \text{Elaboration}(\alpha, \beta_3) \]

comes prior to the normalisation chain with respect to \( \lnot \text{Elaboration}(\alpha, \beta_3) \). Since this exhausts all the types of \( T_2 \) normalisation chains in which no normalisation of the form \( N \ast (S_m, [\langle \tau, \beta_2, \beta_3 \rangle]) \) occurs in \( C \) prior to a normalisation of the form \( N \ast (S_m, [\langle \beta_2, \beta_3 \rangle]) \), we have the desired result: \( w_0 \) survives in every \( T_2 \) normalisation chain in which no normalisation of the form \( N \ast (S_m, [\langle \beta_2, \beta_3 \rangle]) \) occurs in \( C' \) prior to a normalisation of the form \( N \ast (S_m, [\langle \beta_2, \beta_3 \rangle]) \). \( \square \)

By Lemma 5, we see that in some fixpoints \( w_0 \) survives: in others \( w_1 \). By an argument parallel to that in Fact 2, we conclude then that at those fixpoints \( S_\lambda \) in which \( w_0 \) survives \( \models \text{Narration}(\beta_2, \beta_3) \) and at those fixpoints \( C' \) in which \( w_1 \) survives \( \models \lnot \text{Narration}(\beta_2, \beta_3) \). So we conclude:

**Fact 6**

\( T_2 \not\models \text{Narration}(\beta_2, \beta_3) \)

But further, since no other axiom of \( T_2 \) allows us to conclude any other discourse relation between \( \beta_2 \) and \( \beta_3 \), we have that \( S = \bigcirc + T_2 \) is such that \( S \models \langle \beta_2, \beta_3 \rangle \) and \( S \not\models R(\beta_2, \beta_3) \) for any discourse relation \( R \). We assume such a state \( S \) to be incoherent.

Because we must avoid whenever possible incoherent information states, we seek another attachment. We thus look at the information state \( S'' \) that is the update of \( \bigcirc \) with \( T_3 \):

\[ T_3: \]
\[ \langle \tau, \alpha, \beta_3 \rangle \]
\[ \langle \tau, \alpha, \beta_3 \rangle > \text{Narration}(\alpha, \beta_3) \]

An easy survivor argument shows that:

\[ T_3 \models \text{Narration}(\alpha, \beta_3) \]

**Double Penguin Principle**

The relevant example for the Double Penguin is text (4).
Max switched off the light. The room was dark.

The axioms for this example involve two resolvable conflicts — one between States Overlap and Narration and one between States Overlap and Result.

\[ T: \]
\[ \langle \tau, \alpha, \beta \rangle > Narration(\alpha, \beta) \]
\[ \langle \tau, \alpha, \beta \rangle \land Info(\alpha, \beta) \]
\[ \langle \tau, \alpha, \beta \rangle \land State(\beta) > Overlap(\alpha, \beta) \]
\[ \langle \tau, \alpha, \beta \rangle \land State(\beta) > \langle \tau, \alpha, \beta \rangle \]
\[ \langle \tau, \alpha, \beta \rangle \land Info(\alpha, \beta) > \langle \tau, \alpha, \beta \rangle \]
\[ \langle \tau, \alpha, \beta \rangle \land Info(\alpha, \beta) > Cause(\alpha, \beta) \]
\[ \langle \tau, \alpha, \beta \rangle \land Cause(\alpha, \beta) > Result(\alpha, \beta) \]
\[ \square (Overlap(\alpha, \beta) \rightarrow \neg Narration(\alpha, \beta)) \]
\[ \square (Overlap(\alpha, \beta) \rightarrow \neg Result(\alpha, \beta)) \]
\[ \square (Info(\alpha, \beta) \rightarrow state(\beta)) \]

Because of the connections between the various formulas in \( Ant(T) \) — e.g. between \( \langle \tau, \alpha, \beta \rangle \), \( \langle \tau, \alpha, \beta \rangle \land Info(\alpha, \beta) \) and \( \langle \tau, \alpha, \beta \rangle \land State(\beta) \), subtheories that each do one of the Penguin inferences will not have the required chain survivor property with respect to their common vocabulary. So we require one large survivor proof. This proof depends on the following \( T \) survivor:

\[ *\langle w_1, [\langle \tau, \alpha, \beta \rangle \land State(\beta)] \rangle \]

\[ *\langle w_1, [\langle \tau, \alpha, \beta \rangle \land Info(\alpha, \beta)] \rangle \]

\[ *\langle w_1, [\langle \tau, \alpha, \beta \rangle] \rangle \]

Again, analogous proofs to those in Lemmas 2–5, we may show:
**Lemma 8**

$w_1$ is a $T$ survivor

and from this follows:

**Fact**

$T \models Result(\alpha, \beta) \land Narration(\alpha, \beta) \land \neg Overlap(\alpha, \beta)$
References


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