

Question 1. Consider the following two relations:

R:	<table border="1" style="border-collapse: collapse; text-align: center;"><tr><th style="padding: 2px 5px;">A</th><th style="padding: 2px 5px;">B</th></tr><tr><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">2</td></tr><tr><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">0</td></tr><tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">4</td></tr></table>	A	B	1	2	1	0	3	4
A	B								
1	2								
1	0								
3	4								

S:	<table border="1" style="border-collapse: collapse; text-align: center;"><tr><th style="padding: 2px 5px;">B</th><th style="padding: 2px 5px;">C</th></tr><tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">7</td></tr><tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">5</td></tr><tr><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">4</td></tr><tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">4</td></tr></table>	B	C	2	7	2	5	0	4	3	4
B	C										
2	7										
2	5										
0	4										
3	4										

For each query below, compute its result on the above database.

a) Query 1.

```
SELECT T.A, COUNT (T.D)
FROM (SELECT R.A, SUM(S.C) AS D
      FROM R, S
      WHERE R.B=S.B
      GROUP BY R.A) AS T
HAVING COUNT(T.D) <= 2
GROUP BY T.A
```

Solution: a tuple (1,1)

b) Query 2.

```
SELECT DISTINCT R.A
FROM R
WHERE NOT EXISTS (SELECT *
                  FROM R R1, S
                  WHERE R1.B=S.B AND R.A > S.C)
```

Solution: values 1 and 3

c) Query 3.

$$\{x \mid \exists y R(x, y) \wedge (\forall y (R(x, y) \rightarrow \exists u \exists v (S(u, y) \wedge S(v, y) \wedge u \neq v)))\}$$

Solution: a single value 3

Question 2. In this question, we use the following relational schema:

- **Country**(name, capital, area), name is the key
- **People**(country, population, children, adult) where country refers to the name in **Country**, population is the total population, and children and adult is the percentage of the children and adult population.
- **Language**(country, language, percentage) – for each language spoken in the country, it lists the percentage of the population that speaks the language.

a) Write the following query in SQL: *Find names and capitals of countries where children outnumber adults, and at least three different languages are spoken.*

Solution:

```

SELECT C.name, C.capital
FROM Country C, People P, Language L
WHERE C.name=P.country AND C.name=L.country
      AND P.children > P.adult
GROUP BY C.name
HAVING COUNT(L.language) > 2

```

b) Write the following query in SQL: *Find languages that are only spoken in countries whose total population exceeds 10^7 .*

Solution:

```

SELECT L.language
FROM Language L
WHERE NOT EXISTS (SELECT *
                  FROM Country C, People P, Language L1
                  WHERE C.name=P.country AND
                        C.name=L1.country AND
                        P.population < 10000000 AND
                        L.language = L1.language)

```

Question 4 Write the SQL query `SELECT MAX(A) FROM R` in relational algebra. You may assume that R has a single attribute A.

Solution: $R - \pi_A(\sigma_{A < B}(R \times \rho_{B \leftarrow A}(R)))$