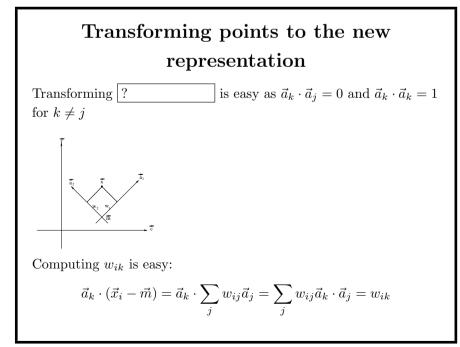


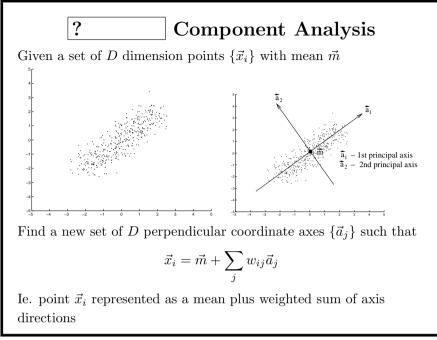
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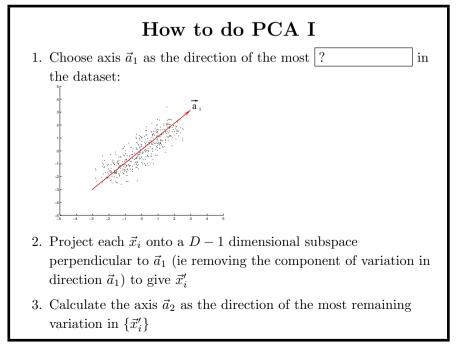


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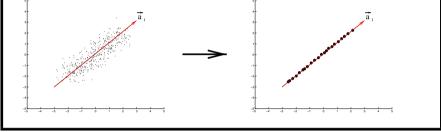


Many possible axis sets  $\{\vec{a}_i\}$ 

? chooses axis directions  $\vec{a}_i$  in order of largest remaining variation

Gives an ordering on dimensions from most to least significant

Allows us to omit low significance axes. Eg, projecting  $\vec{a}_2$  gives:



What We Have Learned

to find the 'natural' axes

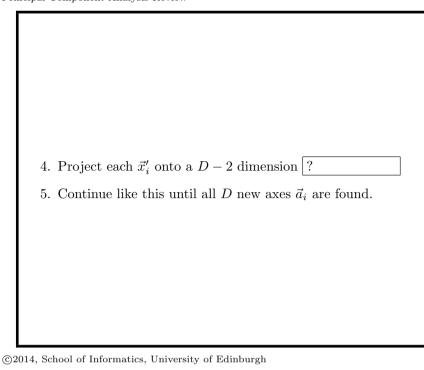
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Principal Component Analysis Review

1. Using ?

of a dataset

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## How to Do PCA II

Via Eigenanalysis

```
Given N D-dimensional points \{\vec{x}_i\}
```

- 1. Mean  $\vec{m} = \frac{1}{N} \sum_i \vec{x}_i$
- 2. Compute ? matrix  $S = \sum_{i} (\vec{x}_{i} - \vec{m}) (\vec{x}_{i} - \vec{m})'$
- 3. Compute Singular Value Decomposition (SVD): S = U D V', where D is a diagonal matrix and U' U = V' V = I
- 4. PCA:  $i^{\text{th}}$  column of V is axis  $\vec{a}_i$  ( $i^{th}$  eigenvector of S)  $d_{ii}$  of D is a measure of significance ( $i^{th}$  eigenvalue)

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2. Algorithm for computing PCA

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