

# 3D Pose Estimation from Planes

Robert B. Fisher  
School of Informatics  
University of Edinburgh

## Pose Estimation

Like 2D case, estimate rotation first, then translation

Assume:

- $N$  paired planes  $\{(M_i, D_i)\}_{i=1}^N$
- model and data normals  $\{\vec{m}_i\}$  and  $\{\vec{d}_i\}$
- a point on each model patch  $\{\vec{a}_i\}$
- a point on each data patch  $\{\vec{b}_i\}$  (need not correspond to  $\vec{a}_i$ )

## Rotation Estimation

Want  $R$  such that  $R\vec{m}_i \doteq \vec{d}_i$

A least square problem, minimizing

$$\sum_i || R\vec{m}_i - \vec{d}_i ||^2$$

Form matrix  $M = [\vec{m}_1 \vec{m}_2 \dots \vec{m}_N]$

Form matrix  $D = [\vec{d}_1 \vec{d}_2 \dots \vec{d}_N]$

Compute singular value decomposition (SVD):

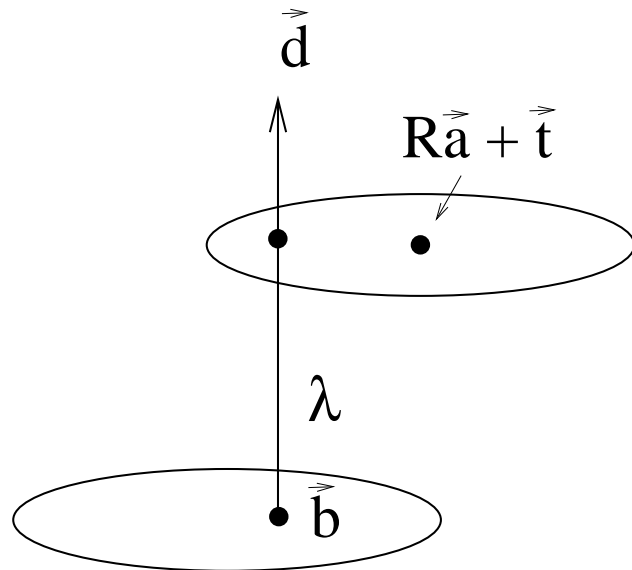
$$\text{svd}(DM') = U * S * V'$$

Compute rotation matrix:  $R = V' * U'$

Assumes at least 3 non-coplanar vectors  
(caution 1 special case)

## Translation Estimation

Minimize the perpendicular separation  $\lambda_i$  between rotated model patch and data patch:



Goal: find  $\vec{t}$  that minimizes  $\sum_i \lambda_i^2$

Form matrix:  $L = \sum_i \vec{d}_i \vec{d}_i'$

Form vector:  $\vec{n} = \sum_i \vec{d}_i \vec{d}_i' (R\vec{a}_i - \vec{b}_i)$

Compute translation  $\vec{t} = -(L)^{-1} \vec{n}$

## Verification

Multiple possible matching solutions:

globally invalid pairings, alternative pose hypotheses

Use verification to find correct one

1. Rotated model normals  $\vec{m}_i$  close to data normals  $\vec{d}_i$ :

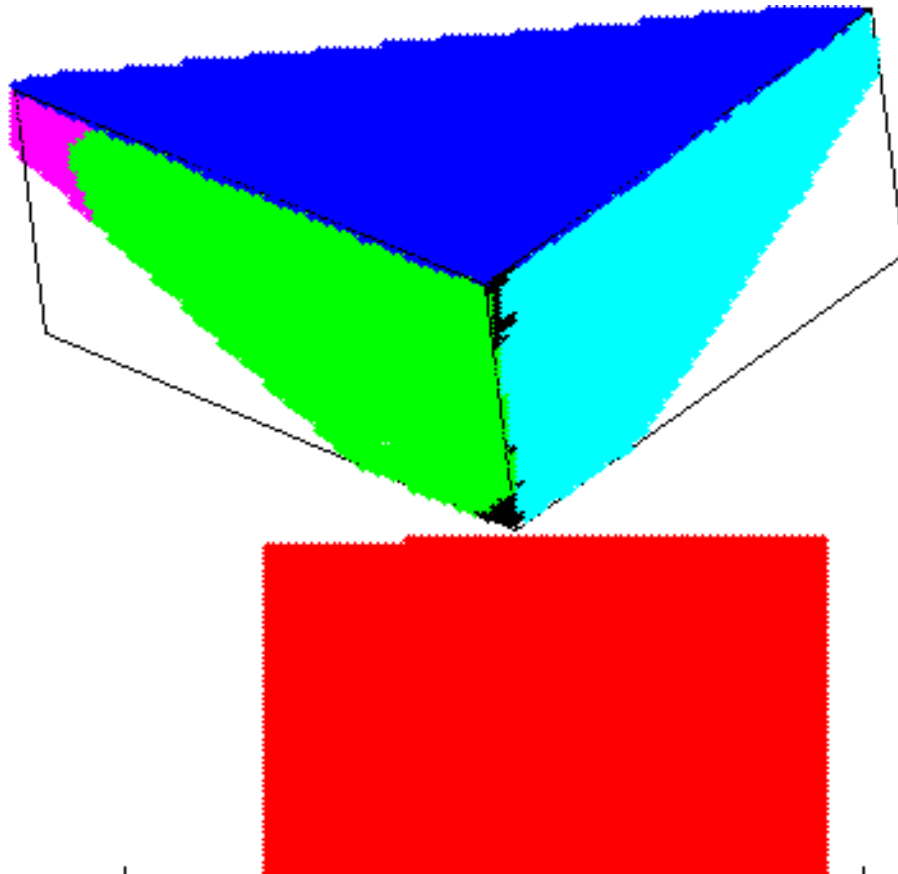
$$\text{acos}(\vec{d}_i' \mathbf{R} \vec{m}_i) < \tau_1$$

2. Transformed model vertices  $\vec{e}_i$  lie on the data plane

$$\vec{n}' \vec{x} + d = 0: \quad | \vec{n}' \vec{e}_i + d | < \tau_2$$

## Matching Results

Object recognized but three pose solutions as verification didn't check overlap areas



Accurate model-data alignment!

## What We Have Learned

- A least squares pose estimation algorithm using planes
- Constraints to verify 3D model matches