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3D Line Calculation

Aim: recovery of 3D line positions **Assume:** line successfully matched in L & R images

- 1. Compute 3D plane that goes through image line and camera origin
- 2. Compute ? of 3D planes from 2 cameras (which gives a line)

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3D Lines

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Computing 3D Line Positions II

Given: paired lines (l,r) with midpoints $\vec{m}_l = (m_{lx}, m_{ly})$ and \vec{m}_r and directions $\vec{a}_l = (a_{lx}, a_{ly})$ and $\vec{a}_r = (a_{rx}, a_{ry})$ Fundamental matrix **F** that maps left to right image

1) Define ?] left midpoint: $\vec{c}_l = (m_{lx}, m_{ly}, 1)'$ and line
direction $\vec{u} = (a_{lx}, a_{lx})$	(y,0)'
2) Define projective right	line: $\vec{v} = (a_{ry}, -a_{rx}, -(a_{ry}, -a_{rx}) \cdot \vec{m}_r)$
3) Define skew matrix ve	rsion of projective right line (for
algebraic line interse	ection):
M =	$\begin{bmatrix} 0 & -v_z & v_y \\ v_z & 0 & -v_x \\ -v_y & v_x & 0 \end{bmatrix}$

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3D Lines

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Triangulating 2 points $(\vec{a}, \vec{b}) \rightarrow \vec{x}$

Given: Left/right projection matrices: \mathbf{P}_{l} , \mathbf{P}_{r} Left/right ? parameter matrices: \mathbf{K}_{l} , \mathbf{K}_{r} Left/right matched points: $\vec{a} = (a_{x}, a_{y})'$ and $\vec{b} = (b_{x}, b_{y})'$ Compute: $\vec{r} = (\mathbf{K}_{l})^{-1}(a_{x}, a_{y}, 1)'$ and $\vec{s} = (\mathbf{K}_{r})^{-1}(b_{x}, b_{y}, 1)'$ $\vec{a}_{1} = r_{1} * \mathbf{P}_{l}(3, :) - \mathbf{P}_{l}(1, :)$ and $\vec{a}_{2} = r_{2} * \mathbf{P}_{l}(3, :) - \mathbf{P}_{l}(2, :)$ $\vec{a}_{3} = s_{1} * \mathbf{P}_{r}(3, :) - \mathbf{P}_{r}(1, :)$ and $\vec{a}_{4} = s_{2} * \mathbf{P}_{r}(3, :) - \mathbf{P}_{r}(2, :)$ $[USV] = svd(\frac{\vec{a}_{1}}{||\vec{a}_{1}||}; \frac{\vec{a}_{2}}{||\vec{a}_{2}||}; \frac{\vec{a}_{3}}{||\vec{a}_{3}||}; \frac{\vec{a}_{4}}{||\vec{a}_{4}||})$ $\vec{x} = V(1:3, 4)'/V(4, 4)$

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<image><image><image><image><image><image>

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3D Lines

84

60

Block 2 2D Line Labels

31

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3D Lines

3D Lines

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Block 1 3D Line Relative Orientations I

Left 1	Left 2	True	?
1	6	1.57	1.52
1	24	0.00	0.20
1	42	0.00	0.14
1	55	1.57	1.50
1	65	1.57	1.55
1	70	1.57	1.48
1	83	1.57	1.43
6	24	1.57	1.45
6	42	1.57	1.50
6	55	0.00	0.07

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Block 1 3D Line Relative Orientations II

Left 1	Left 2	True	Computed
6	65	0.78	0.84
6	70	1.57	1.44
6	83	1.57	1.52
24	42	0.00	0.06
24	55	1.57	1.49
24	65	1.57	.153
24	70	1.57	1.52
24	83	1.57	1.56
42	55	1.57	1.54
42	65	1.57	1.54

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3D Lines

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What We Have ?	
• Computing 3D line by intersecting backprojected 2D lines	
• Backprojection geometric calculations, including triangulatio	n
• Backprojection is reasonably accurate, but not perfect	

Block 1 3D Line Relative Orientations III

	Left 1	Left 2	True	Computed
	42	70	1.57	1.56
	42	83	1.57	1.52
	55	65	0.78	0.78
	55	70	1.57	1.51
	55	83	1.57	1.56
	65	70	0.78	0.86
	65	83	0.78	0.78
	70	83	0.00	0.09
Clearly rea	sonably	?		in 3D

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