

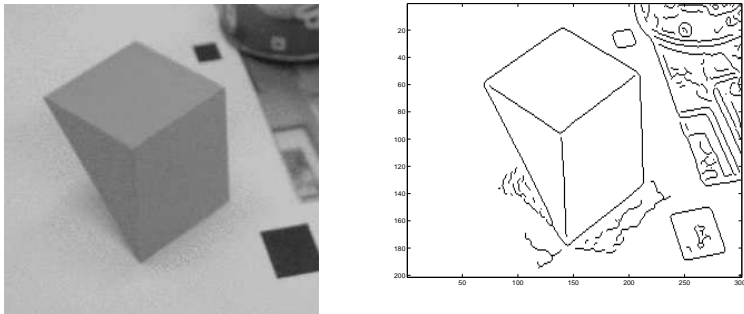
## Canny Edge Detection

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## Edge Detector Introduction

- Edge detection: find pixels at large changes in intensity
- Much historical work on this topic in computer vision (Roberts, Sobel)
- Canny edge detector (1986) first modern edge detector and still commonly used today
- Edge detection never very accurate process: image noise, areas of low contrast, a question of scale. Humans see edges where none exist.

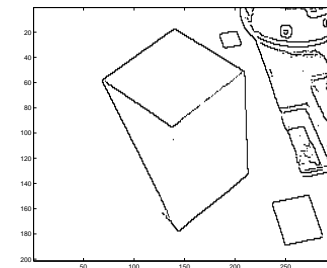
## Canny Edge Detections



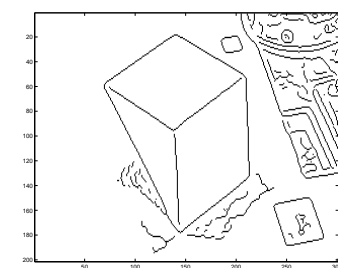
Finds most edges, even in low contrast  
Finds lots of noisy detail too

## Comparison Edge Detections

Roberts' Cross



Canny



Differences in sensitivity and details, esp. in busy areas

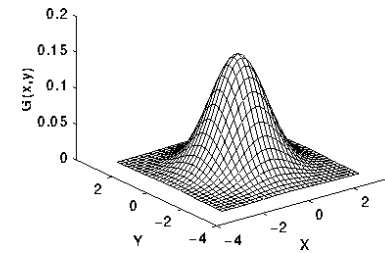
## Canny Edge Detector

Four stages:

1. Gaussian smoothing: to reduce noise and smooth away small edges
2. Gradient calculation: to locate potential edge areas
3. Non-maximal suppression: to locate “best” edge positions
4. Hysteresis edge tracking: to locate reliable, but weak edges

## Canny: Gaussian Smoothing

Convolve with a 2D Gaussian



$$\frac{1}{273}$$

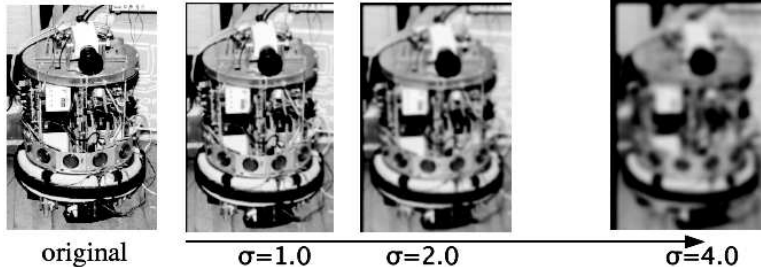
1	4	7	4	1
4	16	26	16	4
7	26	41	26	7
4	16	26	16	4
1	4	7	4	1

Averages pixels with preference near center:  
smooths noise without too much blurring of  
edges

$\sigma$  of Gaussian controls smoothing explicitly

$$\text{convolution mask}(r, c) = \frac{1}{2\pi\sigma} e^{-\frac{r^2+c^2}{2\sigma^2}}$$

Larger  $\sigma$  gives more smoothing - low pass filter



## Gaussian Smoothing Examples

$\sigma = 5$



$\sigma = 20$



## Conservative Smoothing

Gaussian smoothing inappropriate for salt&pepper/spot noise



Noisy image    Gauss smooth    Conservative

So do this before Canny or Gaussian Smoothing

## Canny: Gradient Magnitude Calculation

$G(r, c)$  is smoothed image

Compute local derivatives in the  $r$  and  $c$  directions as  $G_r(r, c)$ ,  $G_c(r, c)$ :

Edge gradient:  $\nabla G(r, c) = (G_r(r, c), G_c(r, c))$

Gradient magnitude:

$$H(r, c) = \sqrt{G_r(r, c)^2 + G_c(r, c)^2}$$

$$\doteq |G_r(r, c)| + |G_c(r, c)|$$

Gradient direction

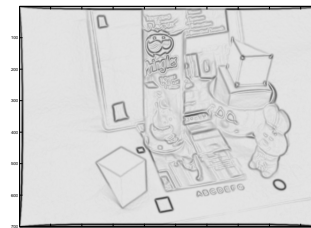
$$\theta(r, c) = \arctan(G_r(r, c), G_c(r, c))$$

$$G_r(r, c) = \frac{\partial G}{\partial r} = \lim_{h \rightarrow 0} \frac{G(r+h, c) - G(r, c)}{h}$$

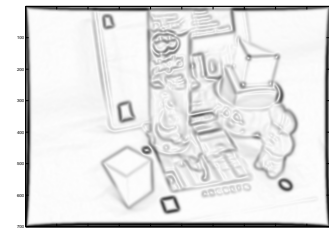
$$\doteq G(r+1, c) - G(r, c)$$

## Gradient Magnitude Examples

$\sigma = 5$



$\sigma = 20$



$\sigma$  controls amount of smoothing  
Smaller  $\sigma$  gives more detail & noise  
Larger  $\sigma$  gives less detail & noise

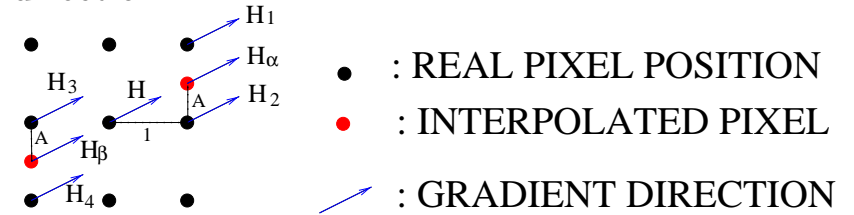
## Canny: Non-maximal Suppression

Where exactly is the edge? peak of gradient

Suppress lower gradient magnitude values: need to check **ACROSS** gradient

0	0	3	12	4	0
0	0	6	10	2	0
0	2	8	7	1	0
0	3	11	4	0	0

Estimate gradient magnitudes using gradient direction:



$$A = \frac{|G_r|}{|G_c|}$$

$$H_\alpha = AH_1 + (1 - A)H_2$$

$$H_\beta = AH_4 + (1 - A)H_3$$

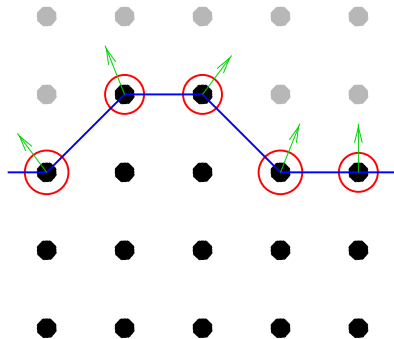
Suppress (set to 0) if  $H < H_\alpha$  OR  $H < H_\beta$

## Canny: Hysteresis Tracking

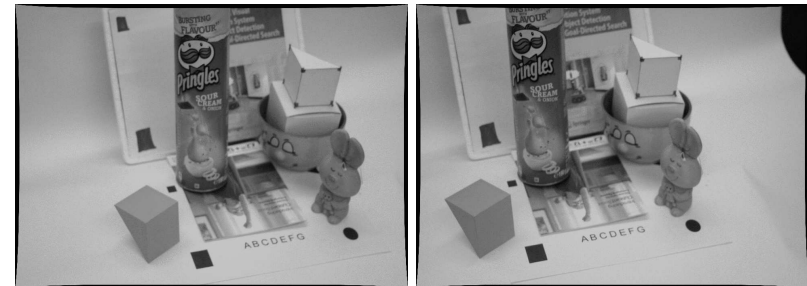
Start edges at certainty:  $H > \tau_{start}$

Reduce requirements at connected edges to get

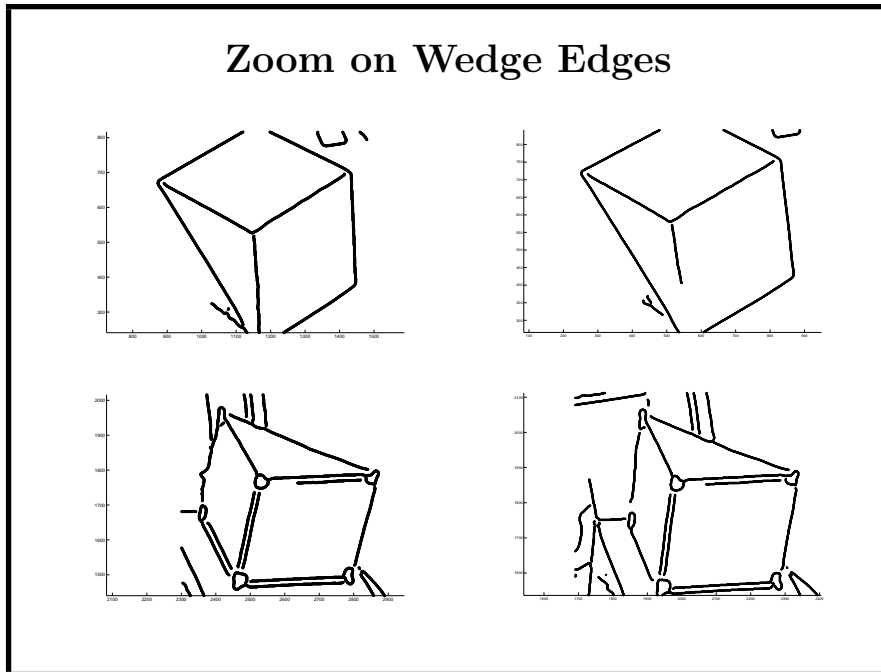
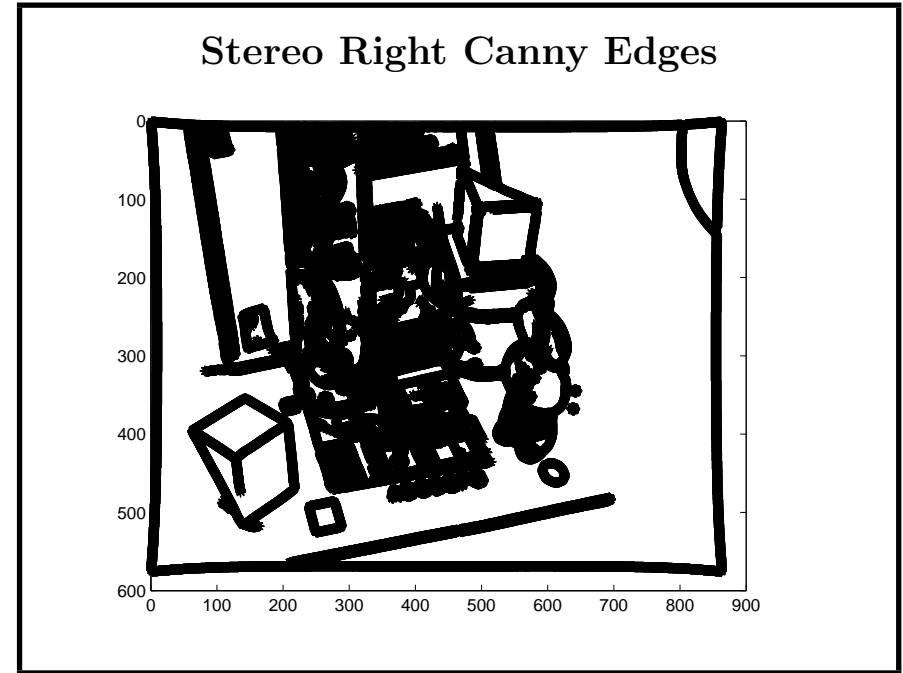
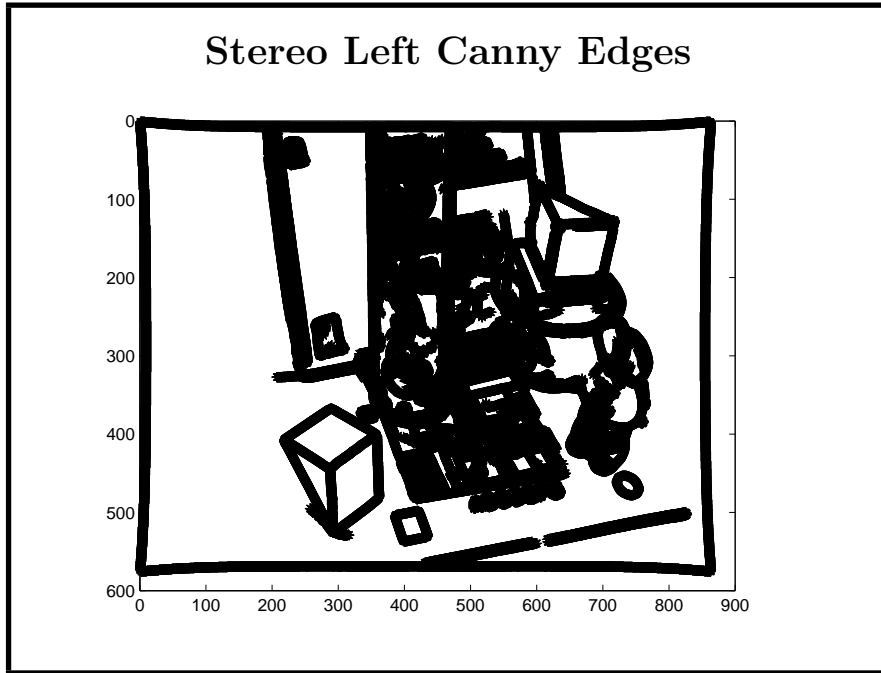
weaker edges:  $H > \tau_{continue}$



## Stereo Canny Edges



Matlab has Canny: `edge(left, 'canny', [], 4);`



## What We Have Learned

- Capabilities of edge detectors
- Noise and detail reduction by smoothing
- Canny algorithm details
- Can find too many edges