## Left:Right Line Pairing

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Left/right line pairs

## Computing 3D Overlap I

Given: Paired lines $(l, r)$ with midpoints $\left(\vec{m}_{l}, \vec{m}_{r}\right)$ and directions $\left(\vec{a}_{l}, \vec{a}_{r}\right)$
Given: Fundamental matrix $\mathbf{F}$ that maps left to right image

Find corresponding edge points on 2 images that lie on the 2 lines:


RIGHT LINE

## Finding Left:Right Line Pairs

For all (left line, right line) pairs
Reject if orientations not similar (vector dot $<0.9$ )
Compute 3D overlap between 2 images (*)
Reject short overlaps
Recompute segment midpoints given overlap
Compute contrast at midpoint (*)
Reject pairs that do not have similar contrasts and suitable disparity range (*)
Remove pairs that are not unique
$\left(^{*}\right)$ - algorithm details below
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## Computing 3D Overlap II

1) Compute all points on left line that cross image: $L=\left\{\vec{p}_{\lambda}:\right.$ for $\lambda=-\infty: \infty$ inimage $\left.\left(\vec{p}_{\lambda}=\vec{m}_{l}+\lambda \vec{a}_{l}\right)\right\}$
2) Compute projective space representation of right image line:
If $\vec{a}_{r}=\left(a_{r x}, a_{r y}\right)$, compute
$\vec{v}=\left(a_{r y},-a_{r x},-\left(a_{r y},-a_{r x}\right) \cdot \vec{m}_{r}\right)$

$$
\mathrm{M}=\left[\begin{array}{ccc}
0 & -v_{z} & v_{y} \\
v_{z} & 0 & -v_{x} \\
-v_{y} & v_{x} & 0
\end{array}\right]
$$

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## Computing 3D Overlap III

3) Predict corresponding point on right line that satisfies epipolar constraint for each point on left line:
for $\vec{p}_{l} \in L$ compute $\vec{q}=\mathrm{M} * \mathrm{~F} *\left(\vec{p}_{l x}, \vec{p}_{l y}, 1\right)^{\prime}$.
Then predicted pixel is: $\vec{p}_{r_{l}}=\left(q_{x} / q_{z}, q_{y} / q_{z}\right)^{\prime}$
4) Corresponding points are valid if the $\vec{p}_{l}$ and $\vec{p}_{r_{l}}$ are both near (eg. $\leq \pm 4$ pixels) to a detected image edge.
5) Keep longest subset of consecutive valid edge points Reject pairs if length is too small (eg. 55 points)
Recompute found segment midpoints
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contrast $=$ average(red pixels) - average(blue pixels)

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Allowable Disparity Range


Left midpoint predicts allowable disparity shift of right midpoint
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## What We Have Learned

- Using the Fundamental matrix to link points in 2 images
- Several new 3D geometry methods

