

Modular features of motor control and learning

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The study of complex motor behaviours has highlighted the role of modular representations both in the planning and in the execution of actions. Recent findings suggest the presence of functional modules within a variety of neural structures. Computational investigations are now addressing the issue of how these modules may act concurrently to generate a wide repertoire of behaviours.

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Introduction

The most exciting advances in the study of motor systems have been brought about by a shift in attention from simple to complex behaviours. Indeed, the class of behaviours that one elects to consider drastically affects the perspective on neural computation. When the investigations focus on the rich repertoire of actions in which living organisms engage, the number of states and of motor commands to be represented appears to be tremendously large. Then, computational analyses may provide valuable insights on constraints that must be satisfied by the neural circuits of the brain. The focus on complex dynamical behaviours has also been a feature of recent progress in the control of artificial systems. There too, the attention has moved from highly constrained manipulations to more complex tasks, such as controlling a bouncing ball with a paddle [1•], guiding objects by pushing and rolling [2,3] and, more generally, handling objects without grasping them [4•]. Understanding how this complex yet ordinary motor competence may be represented and implemented in robots is of great value for the study of biological motor systems. This review describes some of the advances that have been recently brought about in neurobiology by dealing with the complexity of ‘real’ motor behaviours. Among these advances is the formulation of new hypotheses about the building blocks, or ‘modules’, that the central nervous system (CNS) uses to form useful representations for planning and control of actions [5].

The acquisition of complex skills is facilitated by internal models of limb dynamics

The ability to generate a variety of complex behaviours cannot be attained by simply storing randomly the control signals for each action and then recalling these signals when needed [6,7]. Simple considerations about the geometrical space of motor behaviours are sufficient to establish that this approach would be inadequate because the number of possible configurations of the human body

grows exponentially with the number of its degrees of freedom [8]. The number of possible movements, like the number of rice grains on a Chinese checkerboard, is larger than the number of synapses in the brain. Therefore, one’s past experience of movement is necessarily confined to a negligible portion of this space. To achieve its typical competence, the motor system must be capable of generalising beyond the set of movements that it has experienced in the past. This operation is possible only through the construction of some internal representation of the dynamics of the body and of its environment. These representations allow us to generate new behaviours and to handle situations that have not yet been encountered.

A vivid illustration of how internal dynamical models may facilitate motor learning is offered by Schaal and Atkeson (see [9,10,11•]), who studied the task of balancing an inverted pendulum on the hand of a robotic arm. Humans have no difficulty executing this balancing task. Therefore, it seemed that the simplest way to teach a robot arm the same task was to have it copy every movement made by a human. When Atkeson and Schaal [10] tried this direct imitation approach, it failed: even if the human hand movements were carefully copied by the robot, the smallest amount of uncertainty associated with sensing and acting did not allow the pendulum to remain balanced.

This does not mean that imitation of successful behaviour is not a valid strategy [12–14]. On the contrary, robots can learn to copy behaviour successfully when the data from the observed demonstrations are used not to mimic the expert’s movements but to build an internal representation of the motor dynamics associated with the task [9,10,11•]. Such a representation can be constructed using a computational method called a search procedure. This method involves starting with an arbitrary initial model that specifies which action should be taken at every possible state. Then, the data from trial and error experiences are used to iteratively update the model parameters until some optimal or at least satisfactory performance is attained. It turns out that, in most cases, search procedures are effective only if the starting point — the initial assumptions about the dynamic model — is not too far from the correct representation. Therefore, the work of Atkeson and Schaal [10] shows that imitation is a useful strategy when it provides the learner with a good starting point for the subsequent development of an internal model using a search procedure.

In the study of biological motor behaviour, the term ‘internal model’ refers to two distinct mathematical transformations: first, the transformation from a motor command to the consequent behaviour, and second, the transformation from a desired behaviour to the corresponding motor command [15–20]. The first type of

transformation is described by ‘forward models’. These models provide the control centers in the brain with the means not only to predict the expected outcome of a command, but also to estimate the current position and velocity of the moving limbs in the presence of feedback delays (delays associated with the neural processing of sensory information) [21]. A representation of the mapping (or transformation) from planned actions to motor commands is called an ‘inverse model’. Wolpert, Kawato and Miall (see [22••,23]) propose that the neural structures within the cerebellum perform sensory–motor operations equivalent to a combination of multiple forward and inverse models.

Extensive experimental evidence for the biological and behavioral relevance of internal models has been provided by numerous recent studies [16,24–27,28•,29]. Some studies examined the adaptation of arm movements to a perturbing force field generated by an instrumented manipulandum. The major findings of these studies are briefly summarized here. First, when exposed to a complex but deterministic field of velocity-dependent forces, arm movements are first distorted but, after repeated practice, the initial kinematics are recovered [16]. Second, if the force field is suddenly removed following adaptation, after-effects are clearly visible as mirror images of the initial perturbations [16,24]. Third, the CNS achieves adaptation by forming a local map that associates the states (i.e. positions and velocities) visited during the training period with the corresponding forces [30,31••]. Finally, after adaptation, this map (i.e. the internal model of the field) undergoes a process of consolidation [25].

In order to generate the appropriate command for a desired movement of the arm, an inverse model must take into account that multi-joint inertia depends on limb position and velocity. Therefore, an inverse model must be informed about the current state of motion of the limb. This information may come in one of two ways: first, from the input to the inverse model that specifies where the limb should be or, second, from a prediction of the current state based on delayed sensory feedback and on the past history of motor commands. Bhushan and Shadmehr [32••] have found compelling evidence for the second way. Their experimental results are consistent with the hypothesis that we learn to compensate for changes in limb dynamics through a process that involves the combined adaptation of a forward and of an inverse model of the limb.

What are internal models made of? The concept of motor receptive fields

Once established that the motor system creates internal representations of complex multi-joint dynamics, it remains to determine how these representations may come about. As pointed out by Marr [33], any mathematical transformation may be carried out in different ways depending on which elementary building blocks or ‘primitives’ are employed. To identify a set of possible primitives, one can use one of two approaches: a top-down

approach, which is based on the nature of the problem to be solved, or a bottom-up approach, which is based on the properties of the motor output. As detailed below, these approaches can lead to opposite conclusions about an important feature of motor primitives.

The goal of a control system is to define a policy [34] — that is, a function that assigns to every possible state of the system, and its relevant environment, a specific action, such as the force to be produced by the limb muscles. Schaal and Atkeson [35••] demonstrated that complex policies can be learned by tuning the parameters of local controllers. Their approach to motor learning falls within the broad mathematical framework of function approximation [36]. The construction of an optimal (or, simply, of a ‘good’) policy from experience is equivalent to the reconstruction of an unknown function from a set of sampled data — in this case, the combination of states and actions experienced during training. These data are used for tuning the parameters of predetermined basis functions — such as local linear controllers in [35••], radial basis function in [37] or Gaussian fields in [38]. A local controller operates only over a limited region of state space, which is called a receptive field in analogy with visual and somatosensory receptive fields. The computational analysis of Schaal and Atkeson [35••] shows that on-line learning of complex behaviours is successful only when the receptive fields are sufficiently small. If each local controller had a large region of influence, the tuning of its parameters might interfere disruptively with neighbouring regions.

In contrast to top–down analysis, bottom–up analysis has revealed that the likely building blocks used by the central nervous system for the generation of motor behaviours have large domains of influence. I call such building blocks ‘motor primitives’. Like primitives in natural and computer languages, motor primitives may be combined by the central nervous system to generate a grammar of more complex constructs that is, in this case, of more complex motor behaviours. Some important properties of biological motor primitives have emerged from the results of two electrophysiological studies. These studies, which involved the stimulation of muscles and of the spinal cord in spinalized frogs [39,40] presented three main findings: first, that the focal stimulation of a site in the lumbar spinal cord results in the activation of multiple muscles acting on the ipsilateral leg; second, that synergistic muscle recruitment generates a field of viscoelastic forces over a broad region of the leg workspace; and third, that the simultaneous activation of multiple spinal sites leads to the vectorial summation of the corresponding force fields. A computational analysis of electromyographic (EMG) activities induced in frogs by cutaneous stimulation of the leg has provided additional support to the hypothesis that the spinal cord organises a small set of motor primitives that are expressed by fixed synergies of leg muscles. [41••].

Taken together, these studies indicate that motor commands are not directed at controlling the forces of

individual muscles or single joint torques. Instead, it appears that the descending commands that are directed at spinal interneurons modulate the viscoelastic force fields produced by specific sets of muscles [42]. These force fields influence broad regions of the limb state space as each active muscle within a synergy contributes a significant force over a large range of positions and velocities. Simulation studies have shown that broadly tuned nonlinear force fields similar to those elicited by stimulation of the spinal cord can generate — by linear combination — the kinematic and dynamic repertoire of reaching movements [38]. However, as shown by Schaal and Atkeson [35**], broadly tuned force fields would lead to negative interference if their parameters were modified so as to optimize locally one movement at a time. In this respect, it is worth pointing out that human subjects display a significant degree of negative interference when adapting to a novel force field [16]: after adaptation is completed in a region of workspace, after-effects are clearly observable in different regions.

The trade-off between learning and stability

As pointed out by Hogan [43], another critical issue in defining the properties of motor primitives is the issue of stability (see also [44]). A controlled behaviour is stable when errors induced either by inaccuracies in planning or by unexpected perturbations are automatically corrected so that the behaviour is rapidly restored. A number of experimental and theoretical studies provide support for the equilibrium point hypothesis, according to which reaching movements, as well as other behaviours, are generated by the CNS shifting the static equilibrium of a limb along a continuous trajectory [45]. From a mechanical standpoint, this theory emphasizes stability: movements are constructed and represented as smooth transitions among stable postures. In this respect, the hypothesis that the CNS combines spinal force fields to generate stable behaviours is an extension of the equilibrium point hypothesis.

Lohmiller and Slotine [46**] have used an elegant paradigm from nonlinear fluid dynamics to show that in the control of a nonlinear system, such as a multijoint arm, the linear combination of stable dynamical primitives leads to stable behaviours. They found that the force fields generated by muscle synergies are indeed stable primitives within regions that correspond to the receptive fields defined above: these are regions within which external perturbations are compensated for by elastic forces. From this analysis it follows that stable behaviours are enforced over broad domains of a limb's state space by combining stable synergies with large receptive fields.

Higher-order primitives

While the internal representation of limb dynamics is vital for the execution of complex tasks, movements are planned in ways that may be independent from the details of movement execution. Indeed, the computational modules that are needed for movement planning may have

features that are distinct from the modules for movement control. In early groundbreaking work, Georgopoulos *et al.* [47] investigated the activities of motor cortical neurons in relation to the direction of hand movements. They found that the firing rates of individual neurons are broadly tuned to preferred hand directions and that the linear combinations of preferred directions weighted by the cells' activities provide a good estimate of movement direction. The importance of Georgopoulos' approach lies in the attempt to establish a direct relation between neural activities and kinematic variables related to movement planning (see [48,49]). These findings, however, were controversial as they may be consistent both with coding of variables related to movement execution, such as muscle activities, and with coding of variables related to movement planning, such as hand kinematics [50,51]. Whereas some recent studies suggest a strict relation of motor cortical activity with the action of muscles [52–54], others have shown dissociation between cortical activity and movement execution [55,56**,57**].

The presence of separate neural representations for movement planning and movement execution raises interesting questions regarding the relationship between these representations. Rizzolatti and Fadiga [58] suggest that the representation of action supported by 'mirror neurons' in area F5 is a representation of action goals rather than of motor outputs. If these neurons form the basis for a 'vocabulary' of actions [59**] — that is, if they support planning modules — then it is of great importance to understand how the words of this vocabulary may be combined with each other by the brain to span a repertoire of purposeful behaviours. At present, we know that force fields implementing the execution of motor commands are combined by vectorial superposition. However, the rules that govern the combination of goals appear to be more complex. If there is a system of higher order primitives that codes for goals, then it remains to be established how these goals may be translated into movements so that their concurrent activation leads to meaningful actions.

Conclusions

The latest progress in the study of the motor system has been characterized by an increased focus on the complex dynamics of natural tasks in conjunction with the development of new experimental paradigms for the investigation of motor learning. There is a convergence of theoretical and experimental studies on the concept that complex control problems may be solved by a combination of independent modules. From a functional perspective, these modules implement control policies by associating an action to each state (position and velocity) visited during past limb movements. From a neurophysiological perspective, these modules organize specific synergies of muscles. Finally, from a mechanical perspective, these modules generate force fields upon the controlled limbs. The range of action of a module has been defined as a receptive field. There is a significant trade-off between the demands for

stability and the mechanics of muscles, both of which lead to broad receptive fields, and the demands of learning, which suggests narrow receptive fields in the interest of reducing unwanted interference across the state space. This trade-off defines an important area for future investigations into the interactions between higher and lower centers of the motor system.

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References and recommended reading

Papers of particular interest, published within the annual period of review, have been highlighted as:

- of special interest
- of outstanding interest

1. Burridge R, Rizzi A, Koditschek D: **Sequential composition of dynamically dexterous robot behaviours.** *Int J Robotics Res* 1999, **18**:534-555.

The paper describes both in formal and in intuitive terms an elegant approach to implementing complex manipulation skills in robot manipulators. In particular, this study focuses on problems such as controlling the bouncing of a ball on a paddle, where it is difficult for an engineer to define a single control procedure that may work across the entire state space. To deal with these problems, the authors divide the state space of the controlled system (for example, the space of all possible positions and velocities of the paddle and of the ball) into smaller non-overlapping regions. If a region is sufficiently small, then a simple control procedure – called a ‘local controller’ – is sufficient to ensure that the controlled system, once it has entered the region, can be brought to a pre-defined state. After this fragmentation is completed, the local controllers are combined into a single composite procedure that is capable of bringing the system from any state to the desired final state. The work makes use of the formalism of differential geometry to develop this idea.

2. Mason M: **Mechanics and planning of manipulator pushing operations.** *Int J Robotics Res* 1986, **5**:53-71.
3. Bicchi A, Sorrentino R: **Dexterous manipulation through rolling.** In *Proceedings of the IEEE International Conference on Robotics and Automation*. Piscataway, New Jersey: IEEE; 1995:425-457.
4. Lynch K, Mason M: **Dynamic nonprehensile manipulation: controllability, planning and experiments.** *Int J Robotics Res* 1999, **18**:64-92.

Conventional robot manipulators establish a rigid contact with the manipulated object. This simplifies the geometrical relation between the object and manipulator coordinates; however, it also constrains the range of possible operations. Humans and other animals handle objects by establishing ‘non-prehensile’ contacts: that is, contacts that allow slipping or rolling of the object. This type of contact is more difficult to describe mathematically, but it offers a broader repertoire of control policies. Lynch and Mason provide a mathematically insightful approach for solving this problem and some impressive demonstrations.

5. Ghahramani Z, Wolpert D: **Modular decomposition in visuomotor learning.** *Nature* 1997, **386**:392-395.
6. Marr D: **A theory of cerebellar cortex.** *J Physiol* 1969, **202**:437-470.
7. Albus J: **The theory of cerebellar function.** *Math Biosci* 1971, **10**:25-61.
8. Bizzi E, Mussa-Ivaldi FA: **The acquisition of motor behaviour.** *Daedalus* 1998, **127**:217-232.
9. Schaal S: **Learning from demonstration.** In *Advances in Neural Information Processing Systems*. Edited by Mozer M, Jordan M, Petsche T. Cambridge, Massachusetts: MIT Press; 1997:1040-1046.
10. Atkeson C, Schaal S: **Robot learning from demonstration.** In *Machine Learning: Proceedings of the Fourteenth International Conference (ICML '97)*. Edited by Fisher DH Jr; San Francisco: Morgan Kaufmann; 1997:12-20.
11. Schaal S: **Is imitation learning the route to humanoid robots?** *Trends Cog Sci* 1999, **3**:233-242.

In previous work, Schaal and Atkeson demonstrated that learning by imitation is most effective when the demonstration data are used to prime an internal model. In this paper, Schaal compares a variety of different

approaches to learning by imitation, including model-based learning, symbolic approaches and direct learning of control policies.

12. Whiten A: **Imitation of the sequential structure of actions by chimpanzees (Pan troglodytes).** *J Comp Psychol* 1998, **112**:270-281.
13. Byrne R, Russon A: **Learning by imitation: a hierarchical approach.** *Behav Brain Sci* 1998, **21**:667-684.
14. Mataric M, Pomplun M: **Fixation behaviour in observation and imitation of human movement.** *Brain Res* 1998, **7**:191-202.
15. Jordan M, Rumelhart D: **Forward models: supervised learning with a distal teacher.** *Cog Sci* 1992, **16**:307-354.
16. Shadmehr R, Mussa-Ivaldi FA: **Adaptive representation of dynamics during learning of a motor task.** *J Neurosci* 1994, **14**:3208-3224.
17. Johansson R: **Sensory input and control of grip.** *Novartis Foundation Symposium* 1998, **218**:45-59.
18. Kawato M, Wolpert D: **Internal models for motor control.** *Novartis Foundation Symposium* 1998, **218**:291-304.
19. McIntyre J, Berthoz A, Lacquaniti F: **Reference frames and internal models.** *Brain Res Rev* 1998, **28**:143-154.
20. Blakemore S, Goodbody S, Wolpert D: **Predicting the consequences of our own actions: the role of sensorimotor.** *J Neurosci* 1998, **18**:7511-7518.
21. Miall R, Wolpert D: **Forward models for physiological motor control.** *Neural Networks* 1996, **9**:1265-1279.
22. Wolpert D, Kawato M: **Multiple paired forward and inverse models for motor control.** *Neural Networks* 1998, **11**:1317-1329.

This paper describes a computational architecture in which motor commands are generated by a collection of paired forward and inverse models. The approach is similar to the ‘mixture of experts’ proposed earlier by Jacobs *et al.* [60]. Here, different forward models generate independent state estimations. Comparison of these predictions with the actual state is used to establish the degree to which each corresponding inverse model should contribute to the motor output.

23. Wolpert D, Miall R, Kawato M: **Internal models in the cerebellum.** *Trends Cog Sci* 1998, **2**:338-347.
24. Flash T, Gurevich I: **Arm stiffness and movement adaptation to external loads.** *Proc Annu Con Eng Med* 1992, **13**:885-886.
25. Brashers-Krug T, Shadmehr R, Bizzi E: **Consolidation in human motor memory.** *Nature* 1996, **382**:252-255.
26. Gottlieb G: **On the voluntary movement of compliant (inertial-viscoelastic) loads by parcelated control mechanisms.** *J Neurophysiol* 1996, **76**:3207-3229.
27. Flanagan J, Wing A: **The role of internal models in motion planning and control: evidence from grip force adjustments during movements of hand-held loads.** *J Neurosci* 1997, **17**:1519-1528.
28. Sabes P, Jordan M, Wolpert D: **The role of inertial sensitivity in motor planning.** *J Neurosci* 1998, **18**:5948-5957.

The authors demonstrate that when an obstacle must be circumvented during a reaching movement, the hand trajectory is planned so that the point of minimum distance to the object is reached with the largest inertia in the direction between the hand and obstacle. This course of action ensures that when the hand is closest to the object, there is a minimal sensitivity to perturbations that could cause a collision. This paper provides evidence that internal models of limb dynamics are used in motor planning.

29. Hore J, Ritchie R, Watts S: **Finger opening in an overarm throw is not triggered by proprioceptive feedback from elbow extension or wrist flexion.** *Exp Brain Res* 1999, **125**:301-312.
30. Condit MA, Gandolfo F, Mussa-Ivaldi FA: **The motor system does not learn the dynamics of the arm by rote memorization of past experience.** *J Neurophysiol* 1997, **78**:554-560.
31. Condit MA, Mussa-Ivaldi FA: **Central representation of time during motor learning.** *Proc Natl Acad Sci USA* 1999, **96**:11625-11630.

Earlier studies showed that the motor system compensates for a perturbing force field by representing the dependence of the experience force upon the position and velocity of the limb. This paper demonstrates that when the experimental force depends explicitly on time instead of position or velocity, the internal representation is not accurate because the motor system still compensates for these forces as though they depended upon limb state. As a consequence, adaptation does not generalize correctly to different movements.

32. Bhushan N, Shadmehr R: **Computational nature of human adaptive control during learning of reaching movements in force fields.** *Biol Cyber* 1999, **81**:39-60.

This paper provides the first compelling evidence suggesting that a forward and an inverse model of arm dynamics operate jointly during adaptation to a novel force field. The authors suggest that a forward model is needed to provide the motor system with the opportunity to mentally rehearse new dynamics following a limited period of practice. This rehearsal would allow the consolidation of an inverse model, a process that has been observed in subjects after an initial exposure to a novel force field.

33. Marr D: *Vision*. San Francisco, California: WH Freeman and Co; 1982.

34. Sutton R, Barto A: *Reinforcement Learning: an Introduction*. Cambridge, Massachusetts: MIT Press; 1998.

35. Schaal S, Atkeson C: **Constructive incremental learning from only local information.** *Neural Computation* 1998, **10**:2047-2084.

The authors describe a learning model, called receptive field weighted regression, in which simple locally linear elements are combined to approximate unknown functions in parallel with the collection of input-output data. This type of learning is called on-line learning to distinguish it from batch-learning methods, in which all the data are first acquired and then used subsequently. The authors show that the receptive fields of the linear elements can be adapted rapidly to minimize the amount of negative interference between different regions of the input space. It is worthwhile to observe that the local linear elements of this model correspond mathematically to the Gaussian fields described and used in [38].

36. Bishop C: *Neural Networks for Pattern Recognition*. Oxford: Oxford University Press; 1996.

37. Platt J: **A resource-allocating network for function interpolation.** *Neural Computation* 1991, **3**:213-225.

38. Mussa-Ivaldi FA: **Nonlinear force fields: a distributed system of control primitives for representing and learning movements.** In *Proceedings of the 1997 IEEE International Symposium on Computational Intelligence in Robotics and Automation*: 1997, July 10-11; Monterey, Los Alamitos, CA: The Computer Society Press; 1997:84-90.

39. Giszter S, Mussa-Ivaldi FA, Bizzi E: **Convergent force fields organized in the frog's spinal cord.** *J Neurosci* 1993, **13**:467-491.

40. Mussa-Ivaldi FA, Giszter S, Bizzi E: **Linear combinations of primitives in vertebrate motor control.** *Proc Natl Acad Sci USA* 1994, **91**:7534-7538.

41. Tresch M, Saltiel P, Bizzi E: **The construction of movement by the spinal cord.** *Nat Neurosci* 1999, **2**:162-167.

These authors used non-linear regression techniques to fit electromyographic (EMG) data obtained after cutaneous stimulation of several sites of the frog hindlimb. They found that the linear combination of only four muscle synergies was sufficient to reproduce 126 EMG activities induced in nine muscles by electrically stimulating the leg in 14 different locations. These results are consistent with the hypothesis that the neural circuits of the spinal cord implement a small number of independent muscle synergies.

42. D'Avella A, Bizzi E: **Low dimensionality of supraspinally induced force fields.** *Proc Natl Acad Sci USA* 1998, **95**:7711-7714.

43. Hogan N: **The mechanics of multi-joint posture and movement control.** *Biol Cybernetics* 1985, **52**:315-331.

44. Won J, Hogan N: **Stability properties of human reaching movements.** *Exp Brain Res* 1995, **107**:125-136.

45. Bizzi E, Hogan N, Mussa-Ivaldi FA, Giszter S: **Does the nervous system use equilibrium-point control to guide single and multiple joint movements?** *Behav Brain Sci* 1992, **15**:603-613.

46. Lohmiller W, Slotine J-J: **On contraction analysis for nonlinear systems.** *Automatica* 1998, **34**:683-696.

This paper describes an approach to investigating the stability of a control system based on a paradigm from nonlinear fluid dynamics. The approach is

centered on the definition of a contraction region as a region in which the Jacobian of the dynamics equations is uniformly negative definite. The analysis of the contraction regions of a dynamic system allows one to make strong inferences about the exponential convergence of the system toward a nominal trajectory.

47. Georgopoulos AP, Kalaska JF, Caminiti R, Massey JT: **On the relations between the direction of two dimensional arm movements and cell discharge in primate motor cortex.** *J Neurosci* 1982, **2**:1527-1537.

48. Georgopoulos A, Lurito J, Petrides M, Schwartz A, Massey J: **Mental rotation of the neuronal population vector.** *Science* 1989, **243**:234-236.

49. Georgopoulos A, Taira M, Lukashin A: **Cognitive neurophysiology of the motor cortex.** *Science* 1993, **260**:47-52.

50. Mussa-Ivaldi F: **Do neurons in the motor cortex encode movement direction? An alternative hypothesis.** *Neurosci Lett* 1988, **91**:106-111.

51. Sanger T: **Theoretical considerations for the analysis of population coding in motor cortex.** *Neural Computation* 1994, **6**:12-21.

52. Caminiti R, Johnson P, Urbano A: **Making arm movements within different parts of space: dynamic aspects in the primate motor cortex.** *J Neurosci* 1990, **10**:2039-2058.

53. Sergio L, Kalaska J: **Systematic changes in directional tuning of motor cortex cell activity.** *J Neurophysiol* 1997, **78**:1170-1174.

54. Scott S, Kalaska J: **Reaching movements with similar hand paths but different arm.** *J Neurophysiol* 1997, **77**:826-852.

55. Fetz E, Finocchio D: **Operant conditioning of isolated activity in specific muscles and precentral cells.** *Brain Res* 1972, **40**:19-23.

56. Carpenter A, Georgopoulos A, Pellizzer G: **Motor cortical encoding of serial order in a context-recall task.** *Science* 1999, **283**:1752-1757. This is a study of motor cortical activity during a context-recall task. In this task, a monkey was instructed to look at a sequence of targets; it was then cued to exert a force in a particular direction. A significant number of cells were found to modulate their activity exclusively in relation to the serial order of a target, regardless of its spatial location. This indicates a role for the motor cortex in higher-order planning of motor sequences.

57. Chapin J, Moxon K, Markowitz R, Nicolelis M: **Real-time control of a robot arm using simultaneously recorded neurons in the motor cortex.** *Nat Neurosci* 1999, **2**:664-670.

These investigators used the cortical and thalamic signals associated with a movement of the forelimb for controlling a motorized lever that performed the same task as the forelimb by releasing a water reward. As the action was transferred from the limb-operated lever to the motorized lever, the limb ceased to move while the neural activities remained correlated with the task performed by the artificial mechanisms. This study provides a convincing demonstration that cortical activity patterns may be dissociated from the action of muscles.

58. Rizzolatti G, Fadiga L: **Grasping objects and grasping action meanings: the dual role of monkey rostroventral premotor cortex (area F5).** *Novartis Foundation Symposium* 1998, **218**:81-95.

59. Rizzolatti G, Arbib M: **Language within our grasp.** *Trends Neurosci* 1998, **21**:188-194.

This is a thought-provoking interpretation of the role played by mirror neurons, which were described by Rizzolatti's group earlier (see [58]). Considering the correspondence of area F5 in monkey with Broca's area in human, the authors suggest that mirror neurons provide the foundation for the development of symbolic and linguistic processing in humans. This idea is based on the observation that language evolved not from animal calls but, more likely, from the mechanisms of communication associated with imitative behaviours.

60. Jacobs RA, Jordan MI, Nomlan SJ, Hinton GE: **Adoptive mixtures of local experts.** *Neural Computation* 1991, **3**:79-87.