

Quantitative Analysis of Collective Adaptive Systems

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Outline

1 Introduction

- Collective Adaptive Systems
- Quantitative Analysis

2 Modelling CAS

- Challenges for modelling CAS

3 CARMA

- The CARMA Modelling Language
- Smart Taxi System Example

4 Conclusions

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- The CARMA Modelling Language
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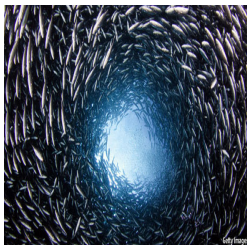
4 Conclusions

Collective Systems

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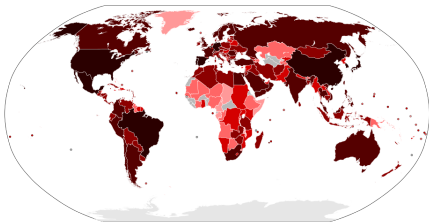
Collective Systems

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in the natural world



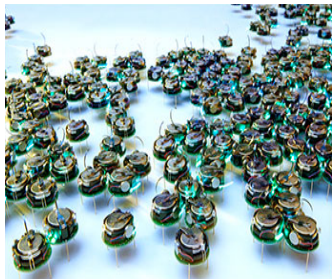
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We are surrounded by examples of **collective systems**:
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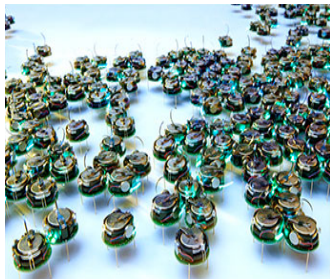
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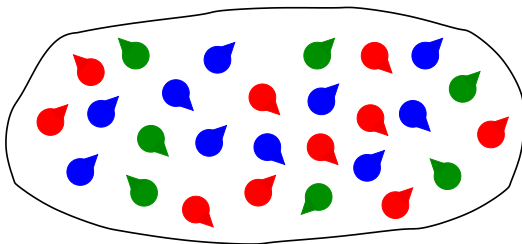
We are surrounded by examples of **collective systems**:
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Most of these systems are also **adaptive** to their environment

Collective Adaptive Systems

From a computer science perspective these systems can be viewed as being made up of a large number of interacting entities.

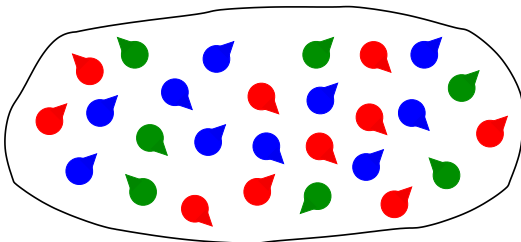


Each entity may have its own properties, objectives and actions.

At the system level these combine to create the **collective** behaviour.

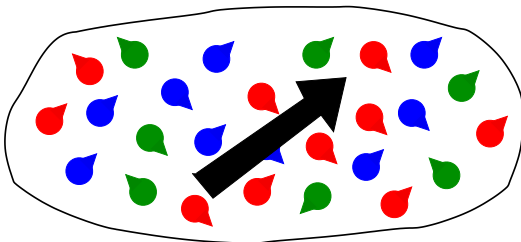
Collective Adaptive Systems

The behaviour of the system is thus dependent on the behaviour of the individual entities.



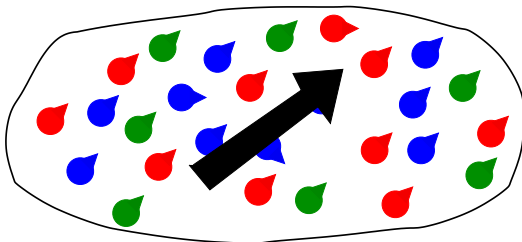
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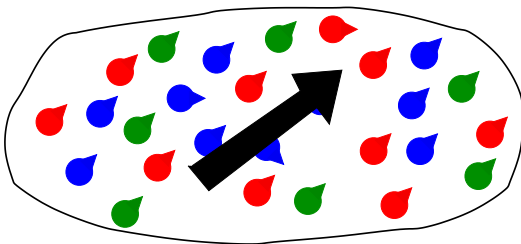
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And the behaviour of the individuals will be influenced by the state of the overall system.

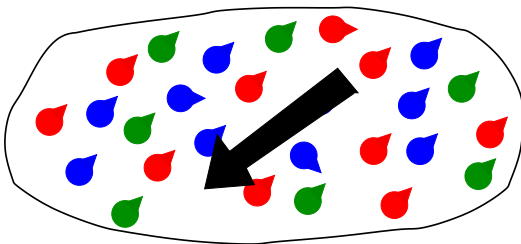
Collective Adaptive Systems

Such systems are often embedded in our environment and need to operate **without centralised control** or direction.



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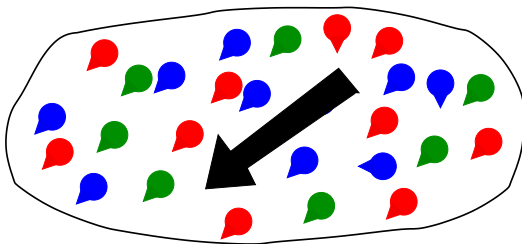
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Collective Adaptive Systems

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Moreover when conditions within the system change it may not be feasible to have human intervention to adjust behaviour appropriately.

Thus systems must be able to **autonomously adapt**.

The Informatic Environment

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Such systems are now becoming the reality, and many form collective adaptive systems, in which large numbers of computing elements collaborate to meet the human need.

For instance, many examples of such systems can be found in components of **Smart Cities**, such as **smart urban transport** and **smart grid electricity generation and storage**.

Quantitative Modelling

Performance modelling aims to construct models of the dynamic behaviour of systems in order to support the **fair** and **efficient** sharing of resources.

Quantitative Modelling

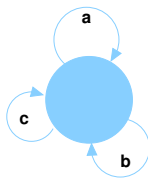
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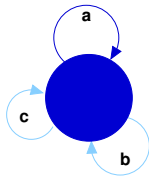
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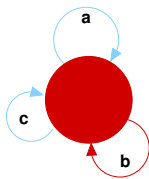
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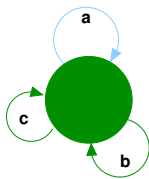
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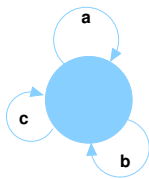
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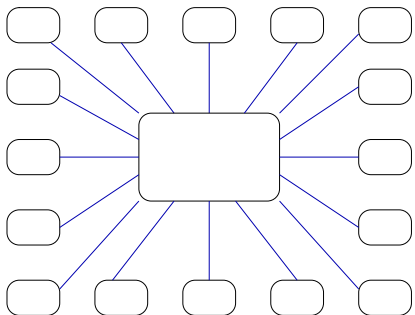
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Performance Modelling: Motivation



Capacity planning

- How many clients can the existing server support and maintain reasonable response times?

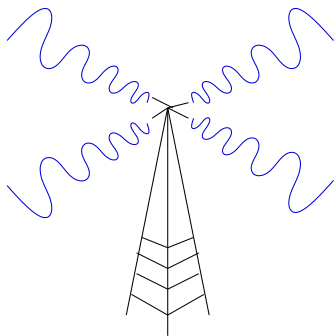
Performance Modelling: Motivation



Capacity planning

- How many buses do I need to maintain service at peak time in a **smart** urban transport system?

Performance Modelling: Motivation



Mobile Telephone Antenna



System Configuration

- How many frequencies do you need to keep blocking probabilities low?

Performance Modelling: Motivation

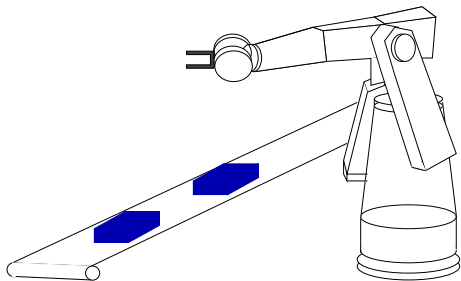


System Configuration

- What capacity do I need at bike stations to minimise the movement of bikes by truck?



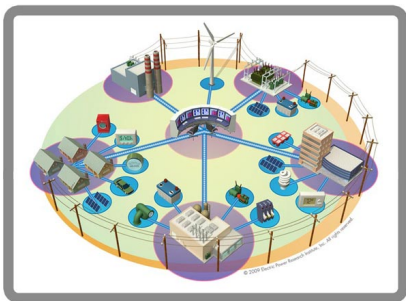
Performance Modelling: Motivation



System Tuning

- What speed of conveyor belt will minimize robot idle time and maximize throughput whilst avoiding lost widgets?

Performance Modelling: Motivation



System Tuning

- What strategy can I use to maintain supply-demand balance within a smart electricity grid?

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Primary examples include:

- **Stochastic Petri Nets** and
- **Stochastic Process Algebras**.

Stochastic Process Algebra

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SPA
MODEL

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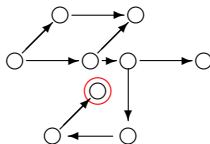
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Reachability analysis

How long will it take
for the system to arrive
in a particular state?

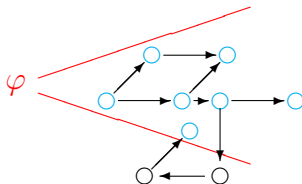


Integrated analysis

Qualitative verification can now be complemented by **quantitative** verification.

Model checking

Does a given property φ
hold within the system
with a given probability?

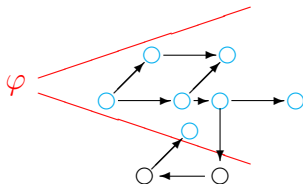


Integrated analysis

Qualitative verification can now be complemented by quantitative verification.

Model checking

For a given starting state
how long is it until
a given property φ holds?



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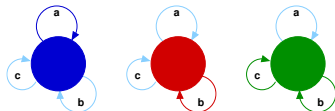
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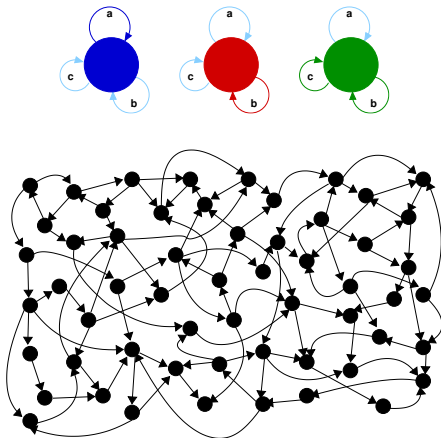
Solving discrete state models

Under the SOS semantics a SPA model is mapped to a **CTMC** with global states determined by the local states of all the participating components.

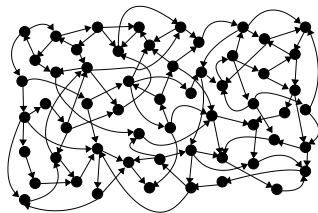


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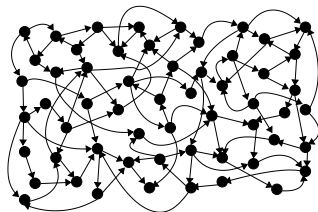


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When the size of the state space is not too large they are amenable to **numerical solution** (linear algebra) to determine a **steady state** or **transient probability distribution**.

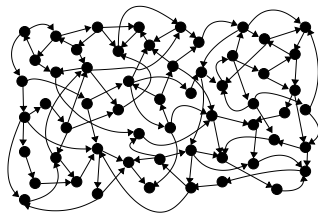
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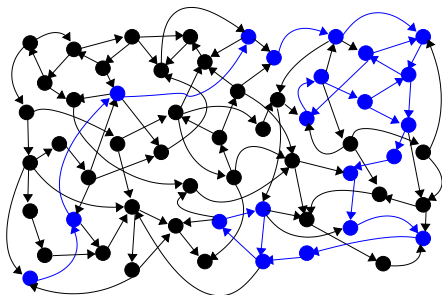
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$$\pi(t) = (\pi_1(t), \pi_2(t), \dots, \pi_N(t))$$

$$\pi(\infty)Q = 0$$

Solving discrete state models

Alternatively they may be studied using **stochastic simulation**. Each run generates a single trajectory through the state space. Many runs are needed in order to obtain average behaviours.

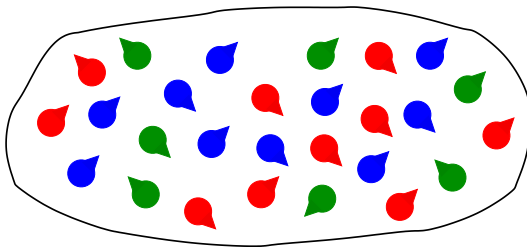


State space explosion

As the size of the state space becomes large it becomes infeasible to carry out numerical solution and extremely time-consuming to conduct stochastic simulation.

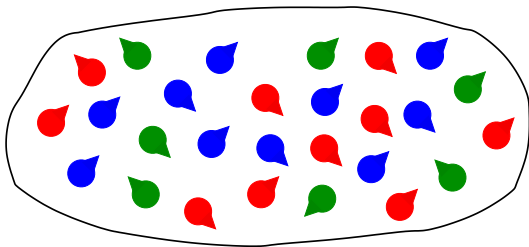
Modelling collective behaviour

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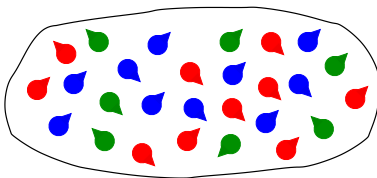
High-level modelling formalisms allow this repetition to be captured at the high-level rather than explicitly.

The Fluid Approximation Alternative

We can shift attention to the **populations** rather than the **individual** entities, and then consider the average behaviour within a population.

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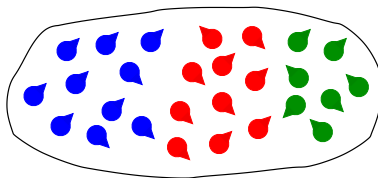
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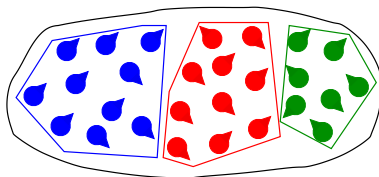
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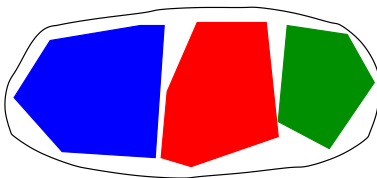
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Even better reductions can be achieved when we no longer regard the components as **individuals**.

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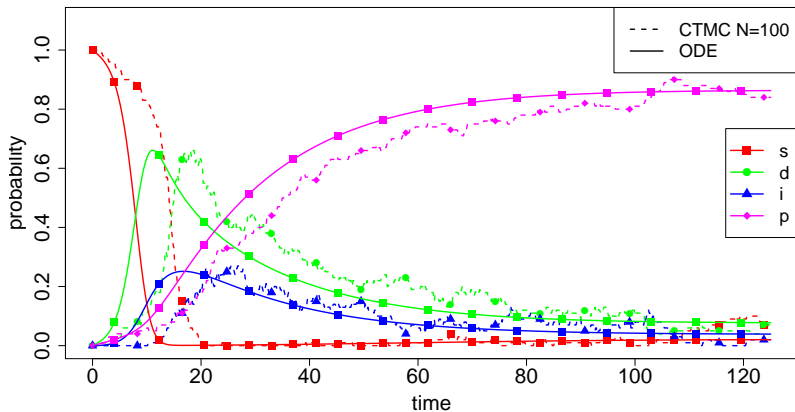
To characterise the behaviour of a population we calculate the **proportion** of individuals within the population that are exhibiting certain behaviours rather than tracking individuals directly.

Furthermore we make a **continuous** or **fluid approximation** of how the proportions vary over time.

M.Tribastone, S.Gilmore and J.Hillston. Scalable Differential Analysis of Process Algebra Models. IEEE TSE 2012.

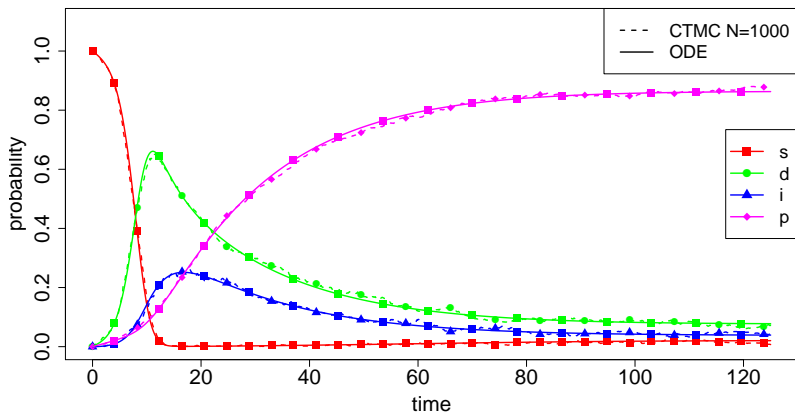
Illustrative trajectories

Limit fluid ODE and single stochastic trajectory of a network epidemics example for $N = 100$



Illustrative trajectories

Limit fluid ODE and single stochastic trajectory of a network epidemics example for $N = 1000$



Example Applications

Large scale software systems

Issues of scalability are important for user satisfaction and resource efficiency but such issues are difficult to investigate using discrete state models.

Spread of viruses and malware

Improved modelling of networks under attack could lead to improved detection and better security in computer systems.

Biochemical signalling pathways

Understanding these pathways has the potential to improve the quality of life through enhanced drug treatment and better drug design.

Example Applications

Crowd dynamics

Technology enhancement is creating new possibilities for directing crowd movements in buildings and urban spaces, for example for emergency egress, which are not yet well-understood.

Smart city infrastructure

The dynamics of large scale urban infrastructures, such as bike sharing systems, are difficult to model and analyse, but such analysis is essential to ensure that the infrastructure can meet demand.

Challenges for modelling CAS

The work over the last decade demonstrates a solid basic framework for modelling systems with collective behaviour but there remain a number of challenges:

- Richer forms of interaction
- The influence of space on behaviour
- Capturing adaptivity

Richer forms of interaction

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Languages like **SCEL** offer these richer communication patterns, with components which include a knowledge store which can be manipulated by other components and **attribute-based communication**.

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Developing scalable analysis techniques, such a fluid approximation, for such languages remains an open problem.

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It would be preferable to model space **explicitly** but this poses significant challenges both for **model expression** and **model solution**.

Again this is difficult for **scalable analysis** which is often based on an implicit assumption that all components are **co-located**.

Capturing adaptivity

- Existing process algebras, tend to work with a fixed set of actions for each entity type.
- Some stochastic process algebras allow the **rate** of activity to be dependent on the state of the system.
- But for truly adaptive systems there should also be some way to identify the **goal** or **objective** of entity in addition to its behaviour.

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This includes the language, **CARMA** (Collective Adaptive Resource-sharing Markovian Agents), which handles:

- 1 The **behaviours** of agents and their interactions;

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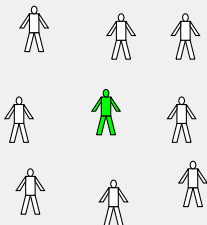
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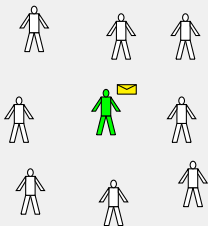


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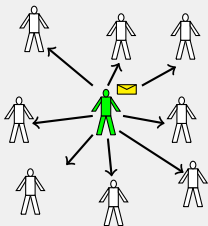


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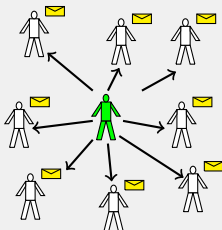


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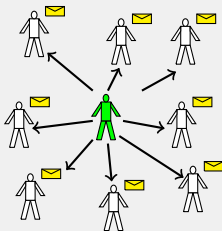


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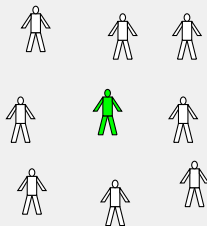
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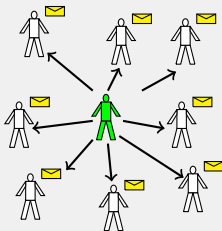


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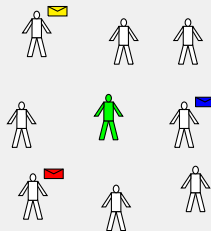
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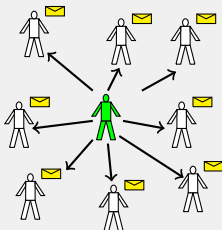


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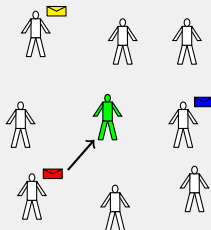
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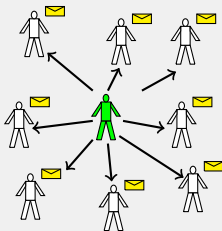


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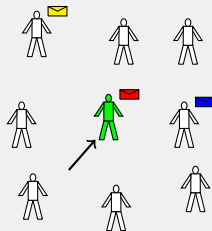
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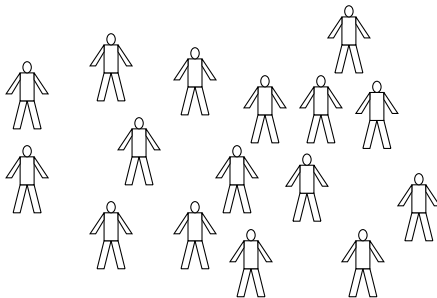


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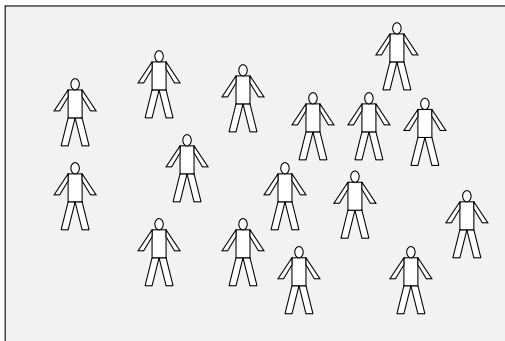
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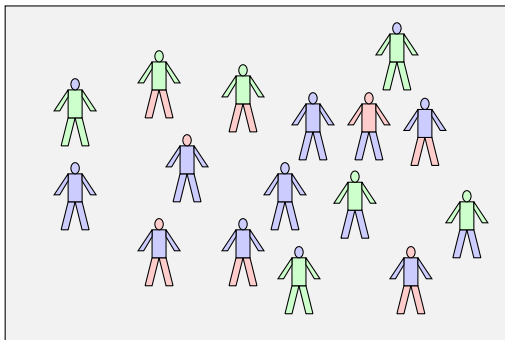


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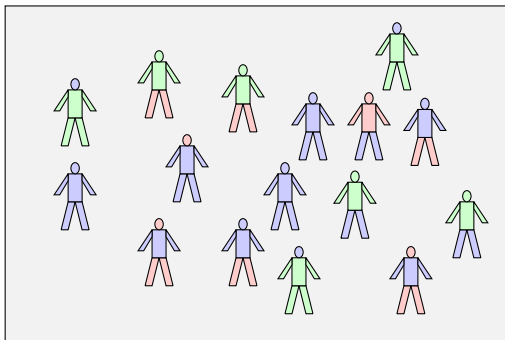


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Processes are referenced via their attributes!

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Environment...

- models the rules intrinsic to the context where agents operate;
- mediates and regulates agent interactions.

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Agents in CARMA are defined as components C of the form (P, γ) where. . .

- P is a process, representing agent behaviour;
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The participants of an interaction are identified via **predicates**. . .

- the **counterpart** of a communication is selected according its **properties**

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The execution of an action takes an **exponentially distributed time**;
the rate of each action is determined by the **environment**.

Interaction primitives

Syntax

$act ::=$	$\alpha^*[\pi]\langle \vec{e} \rangle \sigma$	Broadcast output
	$\alpha^*[\pi](\vec{x}) \sigma$	Broadcast input
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- α is an **action type**;
- π is a predicate;
- σ is the **effect** of the action on the store.

Updating the store

After the execution of an action, a process can update the component store:

- σ denotes a function mapping each γ to a probability distribution over possible **stores**.

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Remark:

- Processes running in the same component can implicitly interact via the local store;
- Updates are instantaneous.

More on synchronisation

Predicates regulating broadcast/unicast inputs can refer also to the received values.

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Example:

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Pattern matching can be encoded in CARMA.

Examples of interactions. . .

Broadcast synchronisation:

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- consists of a pair (γ, ρ) :
 - a **global store** γ , that models the overall state of the system;
 - an **evolution rule** ρ that regulates component interactions (receiving probabilities, action rates,...).

Example: Smart Taxi System

System description:

- We consider a set of **taxis** operating in a city, providing service to **users**;
- Both taxis and users are modelled as components.
- The city is subdivided into a number of **patches** arranged in a grid over the geography of the city.
- The users arrive randomly in different patches, at a rate that depends on the specific time of day.
- After arrival, a user makes a **call** for a taxi and then waits in that patch until they successfully engage a taxi and **move** to another randomly chosen patch.
- Unengaged taxis **move** about the city, influenced by the calls made by users.

Taxis and Users: stores

Both kinds of component use the local store to publish the relevant data that will be used to represent the state of the agent.

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Taxis

- *loc*: identifies current taxi location;
- *occupancy*: ranging in $\{0, 1\}$ describes if a taxi is free (*occupancy* = 0) or engaged (*occupancy* = 1);
- *dest*: if occupied, this attribute indicates the destination of the taxi journey.

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Users

- *loc*: identifies user location;
- *dest*: indicates user destination.

User processes

Users

```
process User =  
    Wait : call*[ $\top$ ]( $\langle$ my.loc.x, my.loc.y $\rangle$ ).Wait  
    +  
    take[loc.x == my.loc.x  $\wedge$  loc.y == my.loc.y]  
        ( $\langle$ my.dest.x, my.dest.y $\rangle$ ).kill  
endprocess
```

Taxi processes

Taxis

```
process Taxi =  
  F : call*[(my.loc.x  $\neq$  posx)  $\wedge$  my.loc.y  $\neq$  posy](posx, posy)  
    {dest := [x := posx, y := posy]}.G  
  +  
  take[T](posx, posy)  
    {dest := [x := posx, y := posy], occupancy := 1}.G  
  G : move*[\bot](o)  
    {loc := dest, dest := [x := 3, y := 3], occupancy := 0}.F  
endprocess
```

Modelling arrivals

The Arrivals process has a single attribute **loc**.

Arrivals process for users

```
process Arrivals =  
    A : arrival* $[\perp]$  $\langle \circ \rangle$ .A  
endprocess
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```
process Arrivals =  
    A : arrival*[ $\perp$ ]( $\circ$ ).A  
endprocess
```

This process is executed in a separated component where attribute **loc** indicates the location where the user arrives.

Modelling arrivals

The Arrivals process has a single attribute **loc**.

Arrivals process for users

```
process Arrivals =  
    A : arrival* $[\perp]$  $\langle \circ \rangle$ .A  
endprocess
```

This process is executed in a separated component where attribute **loc** indicates the location where the user arrives.

The precise role of this process will be clear when the environment is described.

The environment

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The environment manages these aspects of system behaviour, and others in the **evolution rule**.

The evolution rule ρ

ρ is a function, dependent on **current time**, the global store and the current state of the collective, returns a tuple of functions $\varepsilon = \langle \mu_p, \mu_w, \mu_r, \mu_u \rangle$ known as the **evaluation context**

- $\mu_p(\gamma_s, \gamma_r, \alpha)$: the probability that a component with store γ_r can receive a broadcast message α from a component with store γ_s ;
- $\mu_w(\gamma_s, \gamma_r, \alpha)$: the weight to be used to compute the probability that a component with store γ_r can receive a unicast message α from a component with store γ_s ;
- $\mu_r(\gamma_s, \alpha)$ computes the execution rate of action α executed at a component with store γ_s ;
- $\mu_u(\gamma_s, \alpha)$ determines the updates on the environment (global store and collective) induced by the execution of action α at a component with store γ_s .

Evolution rule: μ_p

Defining the probabilities of broadcast actions

```
prob{  
    T, call* : global.plost  
    default 1  
}
```

- call* can be missed with a probability p_{lost} defined in the global store.
- All the other interactions occur with probability 1.

Evolution rule: μ_w

Defining the weights of unicast actions

```
prob{  
   $\top$ , take : Takeprob(real( $\#\{ \textit{Taxi}[F] \mid$   
    (my.loc.x == sender.loc.x)  $\wedge$   
    (my.loc.y == sender.loc.y)  $\}$ )));  
}
```

- Each taxi receives a user request (take) with a weight that depends on the number of taxis in the patch.

Evolution rule: μ_r

Defining the rates of actions

```
rate{  
  T, take : global.rt  
  T, call* : global.rc  
  T, move* : Mtime(now, sender.loc, sender.dest, 6)  
  T, arrival* : Atime(now, sender.loc, 1)  
  default 0  
}
```

While **take** and **call** have constant rates, the rates of the actions **move** and **arrival** are functions that depend on time, reflecting shifting traffic patterns within the city over the course of a day.

Evolution rule: μ_u

In the taxi example, the arrival of a new user is achieved via the update rule:

Update rule

```
update{  
    T, arrival* : new User(sender.loc, DestLoc(now, sender.loc), Wait)  
}
```

Measures

To extract data from a system, a CARMA specifications also contains a set of **measures**.

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The number of waiting users at a location

```
measure WaitingUser00[i := 0] = #{User[Wait] |  
                                my.loc.x == 0 ∧ my.loc.y == 0};
```

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The number of waiting users at a location

```
measure WaitingUser00[ $i := 0$ ] =  $\#\{\text{User}[\text{Wait}] \mid$   
                                 $\text{my.loc.x} == 0 \wedge \text{my.loc.y} == 0\};$ 
```

The number of taxis relocating

```
measure Taxi_Relocating[ $i := 1$ ] =  $\#\{\text{Taxi}[G] \mid \text{my.occupancy} == 0\};$ 
```

Two Scenarios

We consider a grid of 3×3 patches, i.e., a set of locations (i, j) where $0 \leq i, j \leq 2$, and two different scenarios:

Scenario 1: Users arrive in all the patches at the same rate;

Scenario 2: At the beginning users arrive with a higher probability to the patches at the border of the grid; subsequently, users arrive with higher probability in the centre of the grid.

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These are investigated by placing the **same collective** in **different environments**.

Smart Taxi System Collective

```
collective {  
    new : Arrival(0 : 2, 0 : 2);  
    new Taxi(0 : 2, 0 : 2, 3, 3, 0, F);  
}
```

Quantitative Analysis

The semantics of CARMA gives rise to a **Continuous Time Markov Chain (CTMC)**.

This can be analysed by

- by **numerical analysis** of the CTMC for small systems;
- by **stochastic simulation** of the CTMC;
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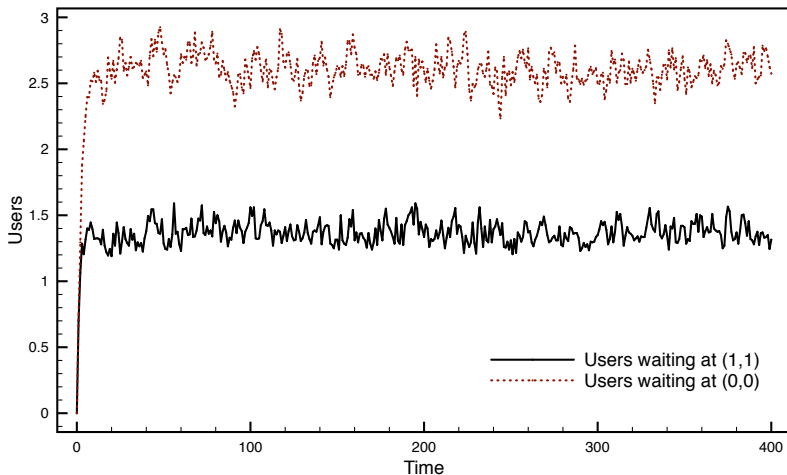
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Here we show the results of stochastic simulation.

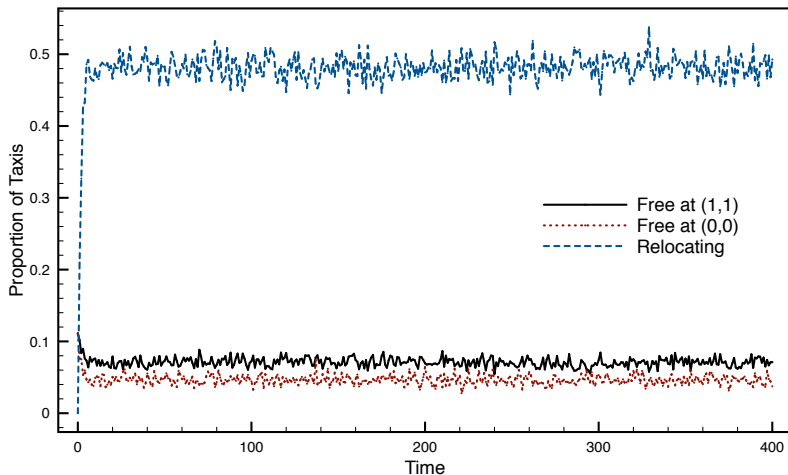
Scenario 1 results

Average number of users waiting at (1,1) and (0,0)



Scenario 1 results

Proportion of free taxis at $(1,1)$ and $(0,0)$ and in transit

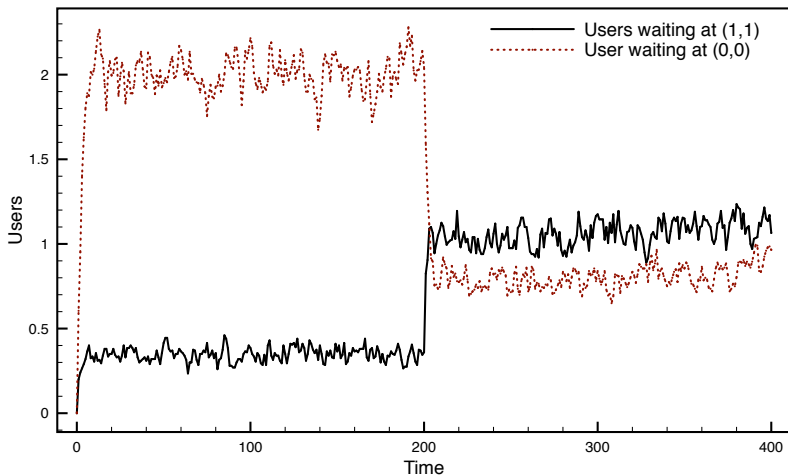


Comments: Scenario 1

- In Scenario 1 after an initial startup period, around 2.5 users are waiting for a taxi in the peripheral location while only 1.5 users are waiting for a taxi in location (1, 1).
- In this scenario a larger fraction of users are delivered to location (1, 1) so soon a larger fraction of taxis are available to collect users at the centre.
- A large fraction of taxis (around 50%) are continually moving between the different patches.

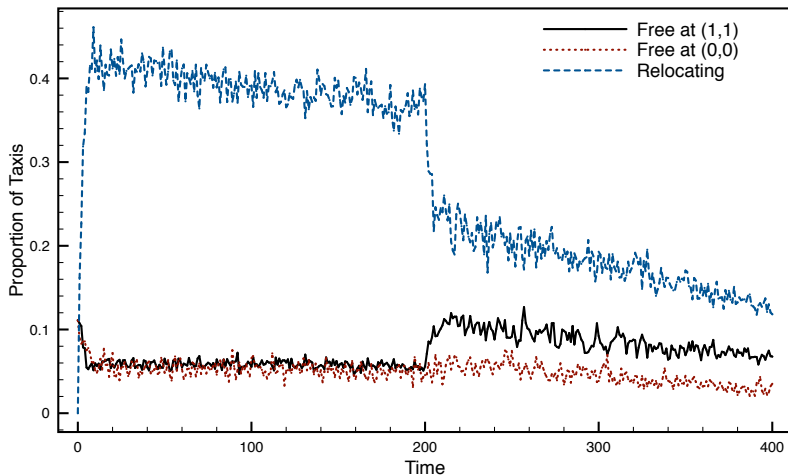
Scenario 2 results

Average number of users waiting at (1,1) and (0,0)



Scenario 2 results

Proportion of free taxis at $(1,1)$ and $(0,0)$ and in transit



Comments: Scenario 2

- In Scenario 2 the location of new arrivals depends on the current time:
 - $[0, 200)$: 3/4 of users arrive on the border and only 1/4 in the centre;
 - $[200, 400)$: 1/4 of users arrive on the border and 3/4 in the centre.
- Results in the first phase are similar to Scenario 1.
- After time 200, the number of users waiting for a taxi in the border decreases below 1 whilst the average waiting for a taxi in the centre increases to just over 1 and the fraction of taxis continually moving is reduced to 20%.

Outline

1 Introduction

- Collective Adaptive Systems
- Quantitative Analysis

2 Modelling CAS

- Challenges for modelling CAS

3 CARMA

- The CARMA Modelling Language
- Smart Taxi System Example

4 Conclusions

Concluding remarks

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- Collective Systems are an interesting and challenging class of systems to design and construct.
- Their role within infrastructure, such as within smart cities, make it essential that quantitative aspects of behaviour is taken into consideration, as well as functional correctness.
- The complexity of these systems poses challenges both for model construction and model analysis.
- CARMA aims to address many of these challenges, supporting rich forms of interaction, using attributes to capture explicit locations and the environment to allow adaptivity.

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- Collective Systems are an interesting and challenging class of systems to design and construct.
- Their role within infrastructure, such as within smart cities, make it essential that quantitative aspects of behaviour is taken into consideration, as well as functional correctness.
- The complexity of these systems poses challenges both for model construction and model analysis.
- CARMA aims to address many of these challenges, supporting rich forms of interaction, using attributes to capture explicit locations and the environment to allow adaptivity.
- Fluid approximation based analysis offers hope for scalable quantitative analysis techniques, but further work is needed to make this applicable to a wider class of CAS.

Thanks

Thanks

Thanks to my collaborators and colleagues on the QUANTICOL project, especially **Michele Loreti**.

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