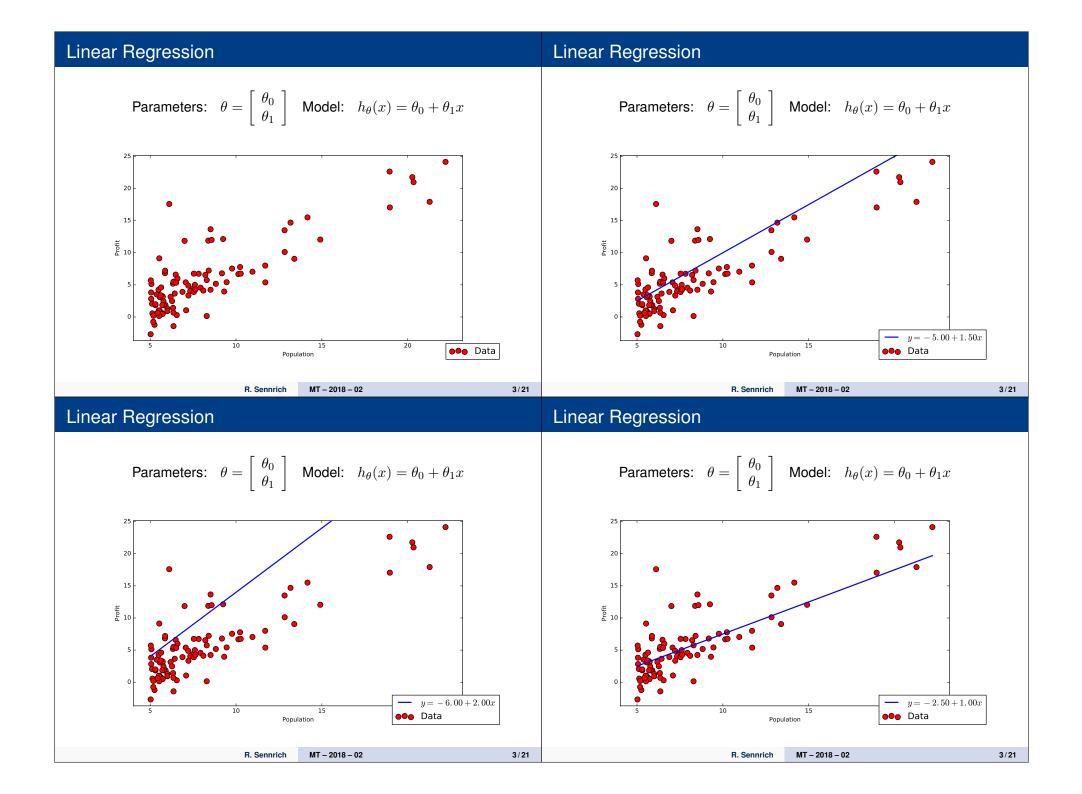
Machine T 02: Neural Ne Rico Se University of	etwork Basics	THE UNIVERSITY of EDINBURGH	<ul> <li>MSc by Research + PhD</li> <li>Research-focused: Work on your thesis topic from the start</li> <li>Collaboration between:</li> <li>University of Edinburgh's</li> </ul>	<ul> <li>Research topi hardware, the application o</li> <li>Parallelism</li> <li>Concurrency</li> <li>Distribution</li> <li>Full funding a</li> <li>Industrial eng programme in internships at companies</li> <li>Now accep Find out m</li> </ul>	eory and f: available gagement ncludes	EPSRC Brearing and Physics 25 Weight down	
R. Sennrich	MT – 2018 – 02	1/21		R. Sennrich	MT – 2018 – 02		1/21
Today's Lecture			Linear Regression				
<ul> <li>linear regression</li> <li>stochastic gradient descent (SGI</li> <li>backpropagation</li> <li>a simple neural network</li> </ul>	D) MT - 2018 - 02	2/21	Parameters: 6	$\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$	Model: <i>h</i> <sub>d</sub>	$\theta(x) = \theta_0 + \theta_1 x$	3/21



Linear Regression	The cost (or loss) function
Parameters: $\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$ Model: $h_{\theta}(x) = \theta_0 + \theta_1 x$	• We try to find parameters $\hat{\theta} \in \mathbb{R}^2$ such that the cost function $J(\theta)$ is minimal: $J: \mathbb{R}^2 \to \mathbb{R}$ $\hat{\theta} = \operatorname*{argmin}_{\theta \in \mathbb{R}^2} J(\theta)$
R. Sennrich MT – 2018 – 02 3/21	R. Sennrich MT – 2018 – 02 4/21
The cost (or loss) function	The cost (or loss) function
• We try to find parameters $\hat{\theta} \in \mathbb{R}^2$ such that the cost function $J(\theta)$ is minimal: $J : \mathbb{R}^2 \to \mathbb{R}$ $\hat{\theta} = \arg \min J(\theta)$	• We try to find parameters $\hat{\theta} \in \mathbb{R}^2$ such that the cost function $J(\theta)$ is minimal: $J : \mathbb{R}^2 \to \mathbb{R}$ $\hat{\theta} = \arg \min J(\theta)$
$\theta \in \mathbb{R}^2$	$ heta \in \mathbb{R}^2$
• Mean Square Error:	$\theta \in \mathbb{R}^2$ • Mean Square Error:

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## The cost (or loss) function

• We try to find parameters  $\hat{\theta} \in \mathbb{R}^2$  such that the cost function  $J(\theta)$  is minimal:

$$J: \mathbb{R}^2 \to \mathbb{R}$$
$$\hat{\theta} = \operatorname*{arg\,min}_{\theta \in \mathbb{R}^2} J(\theta)$$

• Mean Square Error:

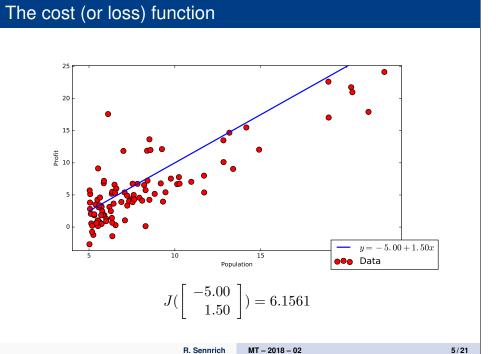
The cost (or loss) function

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} \left( h_{\theta}(x^{(i)}) - y^{(i)} \right)^2$$
$$= \frac{1}{2m} \sum_{i=1}^{m} \left( \theta_0 + \theta_1 x^{(i)} - y^{(i)} \right)^2$$

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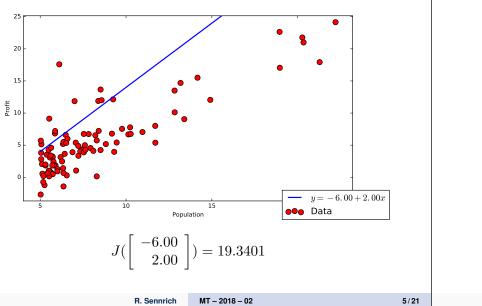
where m is the number of data points in the training set.

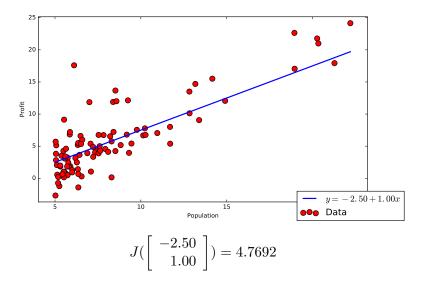
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## The cost (or loss) function

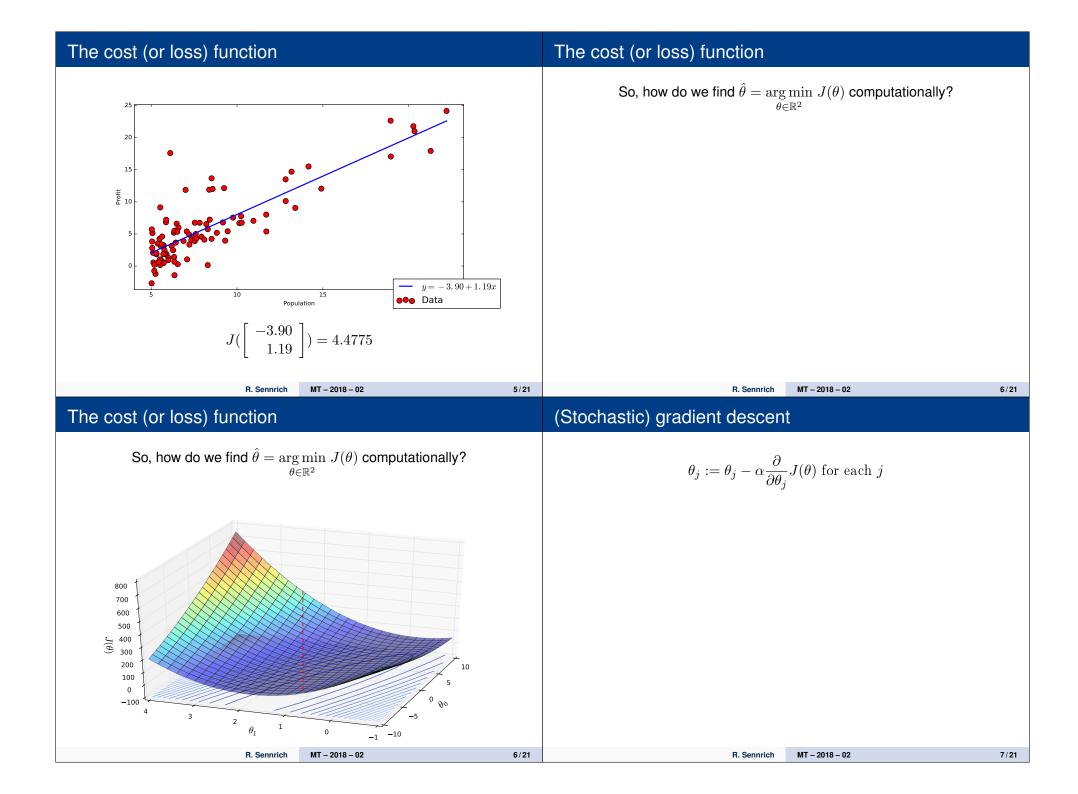
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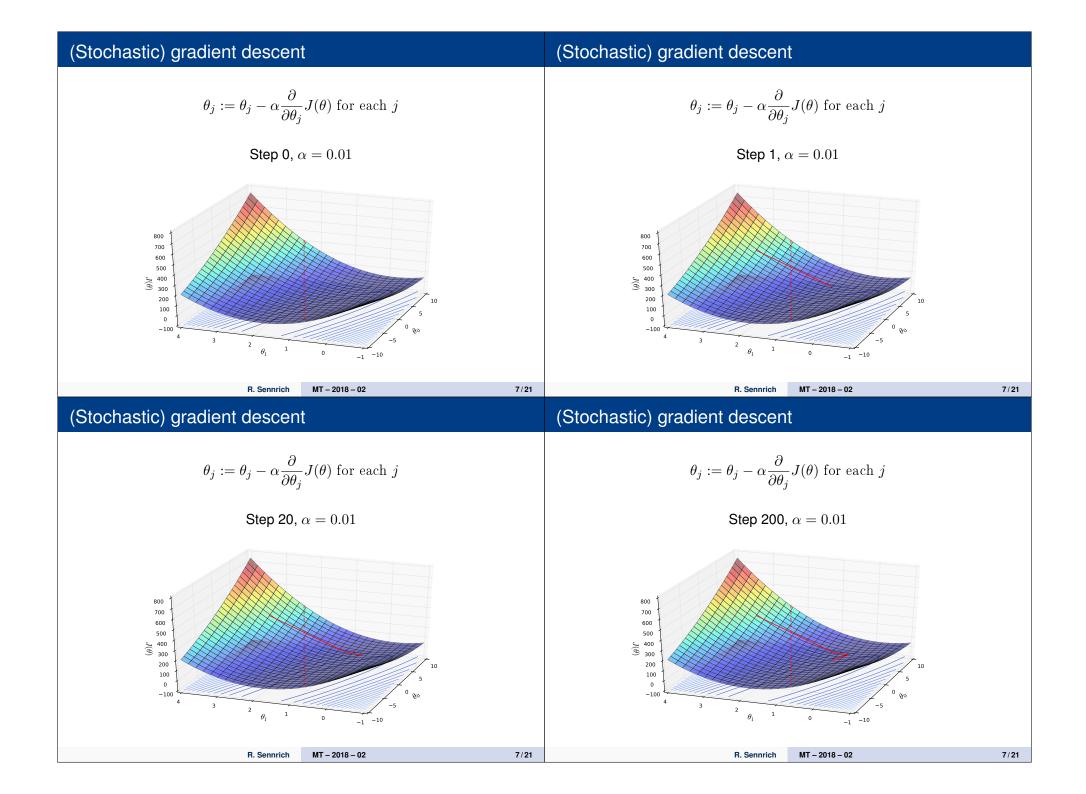


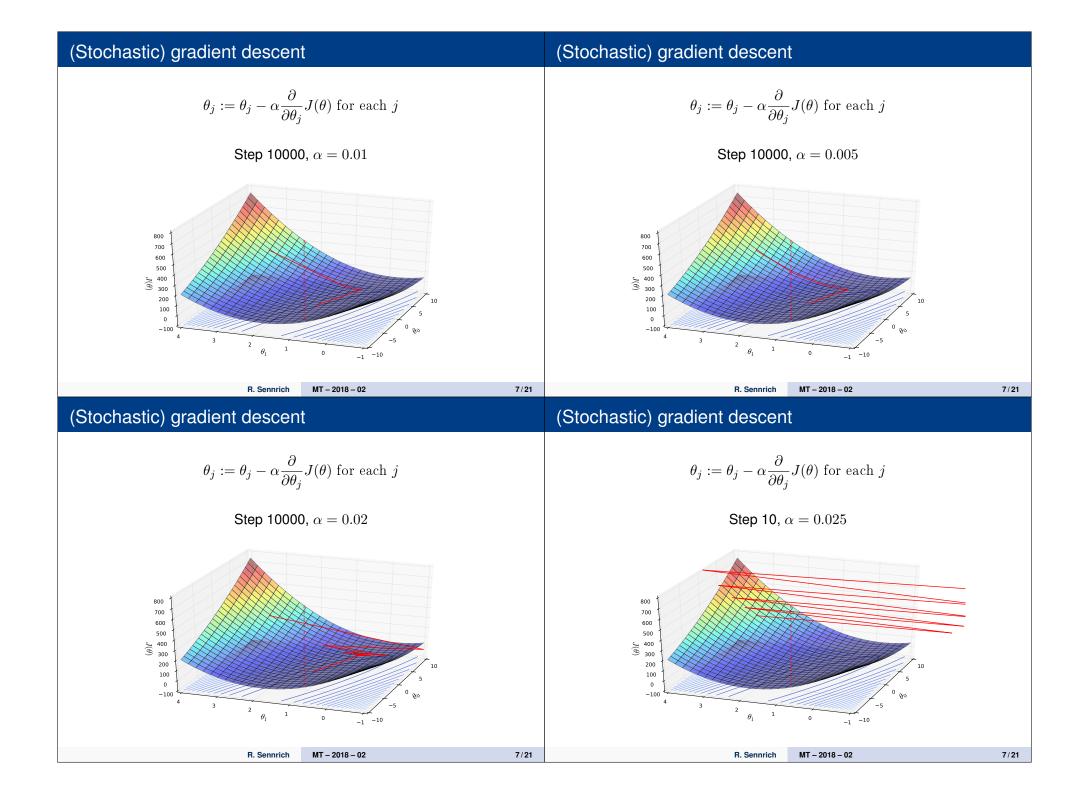


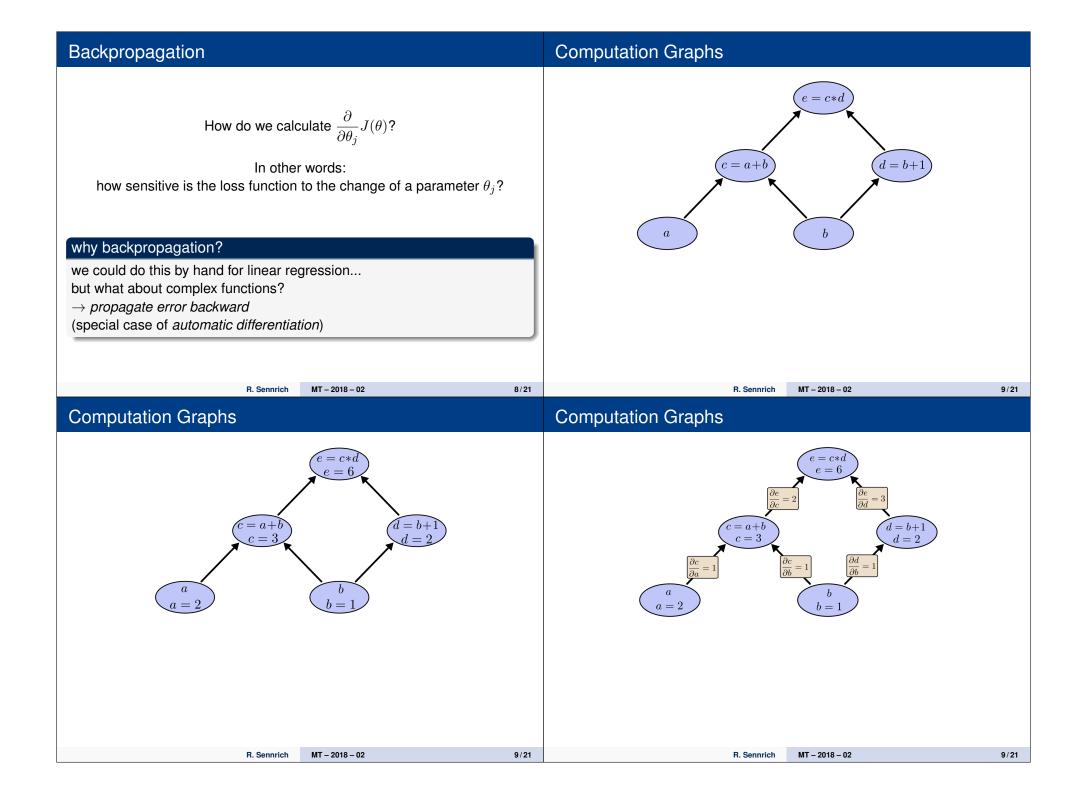
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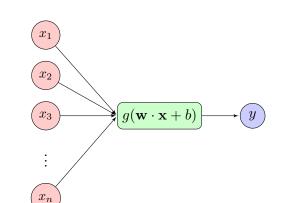


Computation Graphs	Backpropagation
$\frac{\partial e}{\partial c} = 2$ $\frac{\partial e}{\partial c} = 2$ $\frac{\partial e}{\partial d} = 3$ $\frac{\partial e}{\partial d} = 3$ $\frac{\partial e}{\partial d} = 1$ $\frac{\partial e}{\partial d} = 1$ $\frac{\partial e}{\partial b} = \frac{\partial e}{\partial c} \cdot \frac{\partial c}{\partial b} + \frac{\partial e}{\partial d} \cdot \frac{\partial d}{\partial b} = 1 \cdot 2 + 1 \cdot 3 = 5$ next, let's use <i>dynamic programming</i> to avoid re-computing intermediate results	$ \begin{array}{l} &                                   $
R. Sennrich MT – 2018 – 02 9/21	R. Sennrich MT – 2018 – 02 10/21
Backpropagation	To summarize what we have learned
$\frac{\partial e}{\partial c} = 2$ $\frac{\partial e}{\partial d} = 3$ $\frac{\partial e}{\partial d} = 1$ $\frac{\partial e}{\partial b} = 1$ $\frac{\partial e}{\partial b} = 5$	When approaching a machine learning problem, we need:
backward-mode differentiation lets us efficiently compute $\frac{\partial e}{\partial x}$ for all inputs $x$ in one pass $\rightarrow$ also known as <i>error backpropagation</i>	
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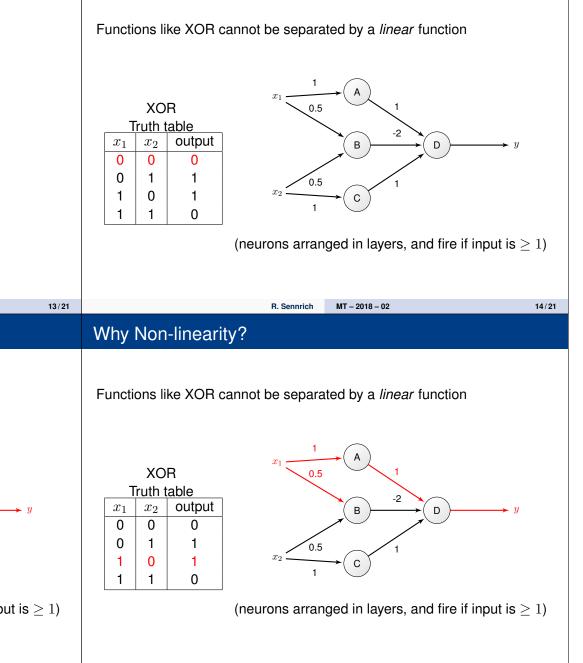
To summarize what we have learned		To summarize what we have learned			
When approaching a machine learning problem, we need: • a suitable model;		<ul> <li>When approaching a machine learning problem, we need:</li> <li>a suitable model;</li> <li>a suitable cost (or loss) function;</li> </ul>			
R. Sennrich MT - 2018 - 02 To summarize what we have learned	11/21	R. Sennrich MT - 2018 - 02 11/21 To summarize what we have learned			
<ul> <li>When approaching a machine learning problem, we need:</li> <li>a suitable model;</li> <li>a suitable cost (or loss) function;</li> <li>an optimization algorithm;</li> </ul>		<ul> <li>When approaching a machine learning problem, we need:</li> <li>a suitable model;</li> <li>a suitable cost (or loss) function;</li> <li>an optimization algorithm;</li> <li>the gradient(s) of the cost function (if required by the optimization algorithm).</li> </ul>			
R. Sennrich MT – 2018 – 02	11/21	R. Sennrich MT – 2018 – 02 11/21			

To summarize what we have learned	What is a Neural Network?		
<ul> <li>When approaching a machine learning problem, we need:</li> <li>a suitable model; (here: a linear model)</li> <li>a suitable cost (or loss) function; (here: mean square error)</li> <li>an optimization algorithm; (here: a variant of SGD)</li> <li>the gradient(s) of the cost function (if required by the optimization algorithm).</li> </ul>	<ul> <li>A complex non-linear function which:</li> <li>is built from simpler units (neurons, nodes, gates,)</li> <li>maps vectors/matrices to vectors/matrices</li> <li>is parameterised by vectors/matrices</li> </ul>		
R. Sennrich MT – 2018 – 02 11/21	R. Sennrich MT – 2018 – 02 12/21		
What is a Neural Network?	What is a Neural Network?		
<ul> <li>A complex non-linear function which: <ul> <li>is built from simpler units (neurons, nodes, gates,)</li> <li>maps vectors/matrices to vectors/matrices</li> <li>is parameterised by vectors/matrices</li> </ul> </li> <li>Why is this useful? <ul> <li>very expressive</li> <li>can represent (e.g.) parameterised probability distributions</li> <li>evaluation and parameter estimation can be built up from components</li> </ul> </li> </ul>	<ul> <li>A complex non-linear function which: <ul> <li>is built from simpler units (neurons, nodes, gates,)</li> <li>maps vectors/matrices to vectors/matrices</li> <li>is parameterised by vectors/matrices</li> </ul> </li> <li>Why is this useful? <ul> <li>very expressive</li> <li>can represent (e.g.) parameterised probability distributions</li> <li>evaluation and parameter estimation can be built up from components</li> </ul> </li> </ul>		
	<ul> <li>relationship to linear regression</li> <li>more complex architectures with <i>hidden</i> units (neither input nor output)</li> <li>neural networks typically use non-linear activation functions</li> </ul>		
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## An Artificial Neuron



## Why Non-linearity?



• x is a vector input, y is a scalar output

• *g* is a (non-linear) *activation function* 

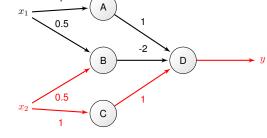
• w and b are the *parameters* (b is a *bias* term)

Functions like XOR cannot be separated by a linear function

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Why Non-linearity?



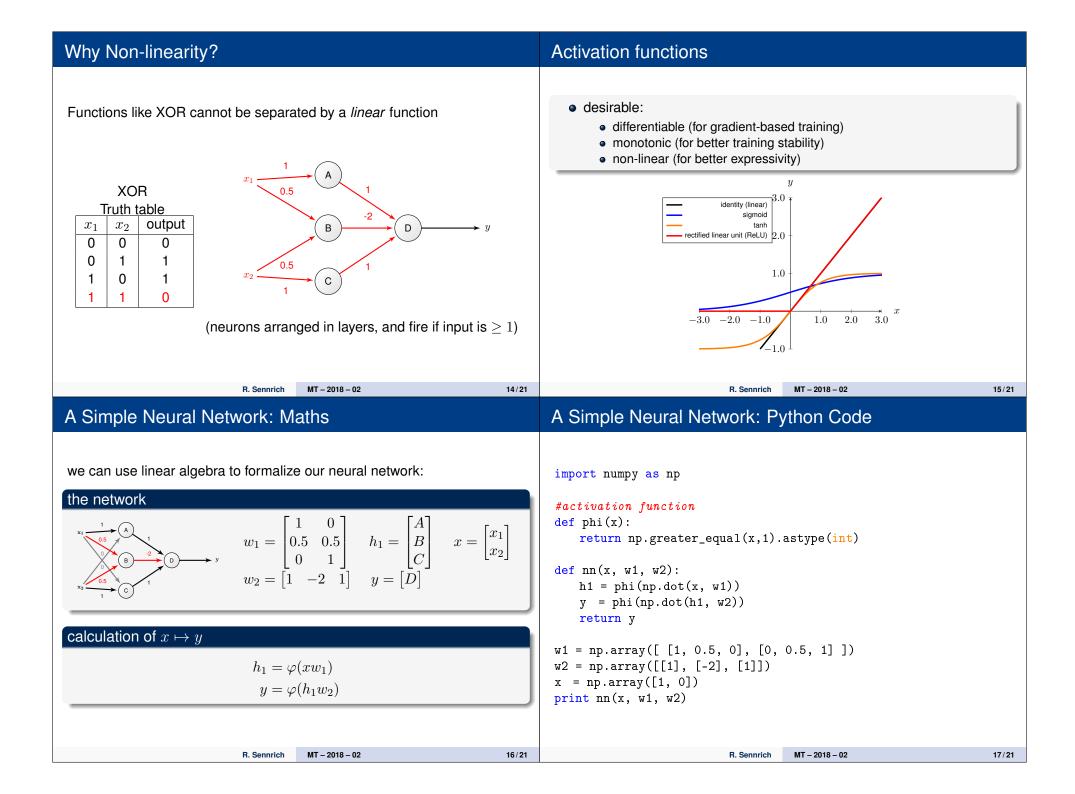
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(neurons arranged in layers, and fire if input is  $\geq 1$ )

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More Complex Archite	ectures	Practical Considerations		
Convolutional	Image: chars:       10       1	<ul> <li>efficiency: <ul> <li>GPU acceleration of BLAS operations</li> <li>perform SGD in mini-batches</li> </ul> </li> <li>hyperparameters: <ul> <li>number and size of layers</li> <li>minibatch size</li> <li>learning rate</li> <li></li> </ul> </li> <li>initialisation of weight matrices</li> <li>stopping criterion</li> <li>regularization (dropout)</li> <li>bias units (always-on input)</li> </ul>		
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Toolkits for Neural Net	tworks	Further Reading		
<ul> <li>What does a Toolkit Provide</li> <li>Multi-dimensional matrices (tensors)</li> <li>Automatic differentiation</li> <li>Efficient GPU routines for tensor operations</li> </ul>		<ul> <li>required reading: Koehn (2017), chapter 13.2-3.</li> <li>further reading on backpropagation: http://colah.github.io/posts/2015-08-Backprop/</li> </ul>		
	orFlow https://www.tensorflow.org/			
theano Thear		eano/		
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Slide Credits		Bibliography I
some slides borrowed from: • Sennrich, Birch, and Junczys-Dow Machine Translation • Sennrich and Haddow (2017): Pra	ctical Neural Machine Translation	Kalchbrenner, N., Grefenstette, E., and Blunsom, P. (2014). A Convolutional Neural Network for Modelling Sentences. In Proceedings of the 52nd Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers).
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